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Thermodynamic Activity-Based Michaelis Constants

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Abstract

The classical approach towards analysing the influence of co-solvents (i.e., cellular molecules that are chemically inert and do not act as reacting agents) on the Michaelis constants of enzyme-catalysed reactions is empirical. More precisely, reaction kinetics is usually mathematically modelled by fitting empirical parameters to experimental concentration vs. time data. In this chapter, a thermodynamic approach is presented that replaces substrate concentrations by thermodynamic activities of the substrates. This approach allows determining activity-based Michaelis constants. The advantage of such activity-based constants K_M^a over their concentration-based counterparts K_M^{obs} is twofold: First, K_M^a is independent of any co-solvent added (while K_M^{obs} is not) as long as it does not directly interfere with the reaction mechanism (e.g., inhibitor or activator). Second, known K_M^a values allow predictions of Michaelis constants for different enzymes and reactions under co-solvent influence. This is demonstrated for a pseudo-one-substrate peptide hydrolysis reaction as well as for more complex two-substrate alcohol dehydrogenase reactions.

Keywords: enzyme kinetics, thermodynamics, activity coefficient, co-solvent, ePC-SAFT

1. Introduction

Understanding the kinetics of enzyme-catalysed reactions is a key aspect not just in the field of biology but also of high relevance for biocatalysis in the industry as enzymes are highly suitable for the production of fine chemicals [1]. The advantage of enzyme catalysis is that high enantioselectivity [2, 3] can often be realised under mild reaction conditions (ambient temperature and pressure).

Key properties for the study of enzyme-catalysed reactions are reaction yield and reaction kinetics. In case of the reaction yield, thermodynamic states an independence of the

equilibrium position from the catalyst involved (as long as the catalyst concentration is low) [4–7]. In contrast, reaction kinetics strongly depends on the catalyst [8, 9]. This means that different enzymes used for the same reaction will cause different kinetic profiles for the considered reaction; this is represented by the experimental (concentration-based) Michaelis constant K_M^{obs} and the catalytic constant k_{cat} . These constants are thus enzyme-specific. Even more, the presence of co-solvents (i.e., chemically inert substances that do not act as metabolites) such as organic and inorganic compounds, salts and polymers might significantly influence such kinetic constants. In literature, the influence of diverse co-solvents on kinetics of a large amount of different enzyme-catalysed reactions is reported [7, 10–13]. It is common practice to empirically describe the co-solvent effects on the kinetic parameters; this requires a co-solvent-dependent consideration of enzyme kinetics. Further, it is discussed whether co-solvent-induced changes on K_M^{obs} are directly related to interactions between co-solvent and the catalytic centre or other parts of the enzyme. These former accepted relations have been recently revised in the publications of Grosch et al. [10], Pleiss [14, 15] and Wangler et al. [7]. These recent works suggested an approach, which is independent of the enzyme itself. In their approach, K_M^{obs} is influenced by co-solvent-substrate interactions caused by co-solvent-induced non-covalent molecular interactions between substrate and reaction medium, which the co-solvent is part of. By changing the perspective from co-solvent-enzyme interactions to co-solvent-substrate interactions, a new activity-based Michaelis constant K_M^a was proposed, which is based on thermodynamic activities of the substrates under co-solvent influence. The advantage of this treatment is that K_M^a is independent of any kind or concentration of co-solvents present in the reaction mixture. This is even more impressive as these recent works neglect co-solvent-enzyme interactions in order to obtain co-solvent independent values for K_M^a . Further, the advantage of such activity-based treatment over the concentration-based approach is to establish a non-empirical method towards predicting and understanding co-solvent effects on the Michaelis constants without the need of experimental kinetic data of reaction mixtures containing co-solvents. This method requires activity coefficients γ of the substrates. These activity coefficients describe the molecular interactions in the reaction mixture, and they can be predicted with different thermodynamic models, e.g., NRTL [16], UNIFAC [17] or ePC-SAFT [18].

In this chapter, an approach is presented to determine K_M^a values based on K_M^{obs} values of the neat (co-solvent-free) reaction system and the activity coefficients of the substrates. The considered reactions are the hydrolysis of N-succinyl-L-phenylalanine-p-nitroanilide (SPNA) catalysed by the enzyme α -chymotrypsin (α -CT) and a two-substrate reaction, namely the reduction of acetophenone (ACP) catalysed by alcohol dehydrogenase 270 (ADH 270) and by alcohol dehydrogenase 200 (ADH 200). Determined K_M^a values under neat conditions were used to predict the co-solvent influence on K_M^{obs} values of the reactions under consideration. These predicted values were finally compared to experimental data to validate this approach.

2. Pseudo-one-substrate reactions

2.1. Theoretical background

2.1.1. Concentration-based approach

Examples for one-substrate reactions are isomerase reactions where one substrate is converted to another without any change to the chemical composition of the molecule. Examples can be found in glycolysis, one being the reversible conversion of 3-phosphoglycerate (substrate S) to 2-phosphoglycerate (product P) catalysed by phosphoglycerate mutase (enzyme E). The general reaction scheme of a one-substrate reaction is given in Eq. (1).

The kinetics of the reaction according to Eq. (2) is commonly described by the Michaelis-Menten equation including the reaction rate v , the maximum reaction rate v_{max} , the Michaelis constant K_M^{obs} and the substrate molality m_S in mol/kg_{water}.

$$v = \frac{v_{max} \cdot m_S}{K_M^{obs} + m_S} \quad (2)$$

Eq. (2) is visualised exemplary by plotting of v over m_S in **Figure 1**.

Figure 1. Qualitative Michaelis-Menten plot of the reaction rate v plotted over the substrate molality m_S according to Eq. (2).

As can be seen from Eq. (2) and **Figure 1**, the reaction rate follows a hyperbolic curve over increasing substrate concentrations. Further, K_M^{obs} defines the shape of the curve as it is the concentration of substrate at which the reaction velocity becomes half of its maximal value $0.5 v_{max}$. Based on this, the importance of K_M^{obs} becomes obvious. If the value of K_M^{obs} is low compared to m_S required to reach $v = v_{max}$, it can be deduced that the cellular concentration of the substrates will also be close to K_M^{obs} as a significant increase in m_S (e.g., fivefold) will never increase v more than by a factor of 2 [9]. Thus, the knowledge of K_M^{obs} is of high importance for biology and for technical applications of enzyme-catalysed reactions.

Unfortunately, the majority of enzyme-catalysed reactions are not one-substrate reactions; in such cases, the reaction scheme increases in complexity. However, it is often still possible to apply pseudo-one-substrate reaction conditions given that the molality of one substrate is much higher than the molality required to obtain v_{max} . These conditions are obtained if substrate simultaneously presents the reaction solvent, which is the case for hydrolysis reactions. A general scheme for a two-substrate reaction is given in Eq. (3).

In Eq. (3), substrates are labelled as S_1 and S_2 ; the reaction mechanism (ordered or random) shall not be discussed at this point. In this case, the Michaelis-Menten equation changes to Eq. (4), which contains the Michaelis constants for substrate 1 K_{MS1}^{obs} and substrate 2 K_{MS2}^{obs} as well as the inhibition constant K_{iS1}^{obs} , which defines the reaction mechanism [8, 9].

$$v = \frac{v_{max} \cdot m_{S1} \cdot m_{S2}}{K_{iS1}^{obs} \cdot K_{MS2}^{obs} + K_{MS1}^{obs} \cdot m_{S2} + K_{MS2}^{obs} \cdot m_{S1} + m_{S1} \cdot m_{S2}} \quad (4)$$

In the case of a hydrolysis reaction taking place in water as reaction solvent, the molality of substrate 2 m_{S2} (water) is usually two to three orders of magnitude higher than the molality of substrate 1, which gets cleaved by the enzyme. Rearranging Eq. (4) leads back to the Michaelis-Menten equation under this assumption shown in Eqs. (5)–(7).

$$v = \frac{v_{max} \cdot m_{S1}}{\frac{(K_{iS1}^{obs} \cdot K_{MS2}^{obs})}{m_{S2}} + K_{MS1}^{obs} + K_{MS2}^{obs} \cdot \frac{m_{S1}}{m_{S2}} + m_{S1}} \quad (5)$$

$$m_{S1} \gg m_{S2} \text{ and } m_{S1} \gg K_{iS1}^{obs} \cdot K_{MS2}^{obs} \quad (6)$$

$$v = \frac{v_{max} \cdot m_{S1}}{K_{M1}^{obs} + m_{S1}} \quad (7)$$

To be able to compare reactions from different research groups and further for different enzymes catalysing the same reaction, the Michaelis-Menten equation has to be normalised to the total enzyme concentration m_E according to Eq. (8).

$$\frac{d \frac{m_P}{m_E}}{dt} = \frac{dm_P}{dt} \cdot \frac{1}{m_E} = v' = \frac{k_{cat} \cdot m_S}{K_M^{obs} + m_S} \quad (8)$$

The determination of k_{cat} and K_M^{obs} is usually performed by measuring reaction rates for different substrate concentrations as shown in **Figure 1**. While this approach is common, it also poses a lot of difficulties and causes high uncertainties. The determination of k_{cat} requires that the solubility of the substrate has to be higher than the molality m_S that is required for reaching k_{cat} . Lowering the enzyme concentration and thus the required molality m_S often causes diffusion limitations that might lead to highly uncertain kinetic constants. Another possible issue is contrary, as a reaction might require high concentrations of an expensive substrate to determine k_{cat} . To overcome these possible limitations, the Lineweaver-Burk equation is commonly applied for the determination of the kinetic constants [19].

$$\underbrace{\frac{1}{v'}}_y = \underbrace{\frac{K_M^{obs}}{k_{cat}}}_m \cdot \underbrace{\frac{1}{m_S}}_x + \underbrace{\frac{1}{k_{cat}}}_b \quad (9)$$

Through this linearization, a plot of $(v')^{-1}$ over m_S^{-1} yields the kinetic constants: The slope (*Sl*) and the ordinate (*Or*) of the obtained linear fit can be used to determine K_M^{obs} and k_{cat} as given in Eqs. (10) and (11).

$$Sl = \frac{K_M^{obs}}{k_{cat}} \quad (10)$$

$$Or = \frac{1}{k_{cat}} \quad (11)$$

2.1.2. Activity-based approach

As presented in Section 2.1.1, the Michaelis constant is determined based on the molality m_S . If co-solvents are added to the neat reaction mixtures, the experimental procedure has to be performed also for the changed conditions. From the perspective of process design, this poses a huge cost-intensive and time-consuming approach towards finding suitable co-solvents for the desired application.

To be able to predict co-solvent influences on pseudo-one-substrate reactions, a thermodynamic co-solvent-independent Michaelis constant, further referred to as K_M^a , has to be determined. K_M^a is a constant value, which does not depend on co-solvent given that the co-solvent does not disturb the reaction mechanism (e.g., co-solvent acts as inhibitor or activator) and that the co-solvent has no denaturing effect on the enzyme. K_M^a can be determined under neat (co-solvent-free) conditions by replacing the molality m_S in Eq. (9) with thermodynamic activities of the substrate a_S . The latter are accessible by multiplying the concentration of a substrate by the respective concentration-based activity coefficient (molality-based γ_S^m , mole-fraction-based γ_S^x or molarity-based γ_S^c) as shown in Eq. (12) [20–22]:

$$a_S[-] = x_S \cdot \gamma_S^x = m_S \cdot \gamma_S^m = c_S \cdot \gamma_S^c \quad (12)$$

In the following, molality-based γ_S^m will be used to analyse the data. Replacing molalities in Eq. (9) with activities leads to an activity-based Lineweaver-Burk equation:

$$\frac{1}{\nu'} = \frac{K_M^a}{k_{cat}} \cdot \frac{1}{a_S} + \frac{1}{k_{cat}} \quad (13)$$

To determine K_M^a , the experimental $(\nu')^{-1}$ values, which were determined for different m_S^{-1} values, are further plotted over the reciprocal substrate activity a_S^{-1} . It is noteworthy that this procedure does not change the value of k_{cat} [7, 23]. Under the assumption that the addition of a co-solvent only changes non-covalent interactions between the substrate and the other components in the reaction mixture, K_M^a is assumed to be a constant value. That is, any observed change in K_M^{obs} is directly reflected in γ_S^m . With this knowledge, a prediction of K_M^{obs} under co-solvent influence becomes possible. For this, two hypothetical molalities of the substrate m_S^{hyp} are chosen randomly. Afterwards, activity coefficients of the substrate in the co-solvent system are predicted and the respective activities are calculated. Further, a random value of k_{cat} (e.g., value of the neat reaction) is chosen. Note that k_{cat} is a factor that cancels out during the linearization to determine K_M^{pre} (see Eq. (13)). In the next step, the predicted activities together with K_M^a and k_{cat} are used to predict $(\nu')^{-1}$ according to Eq. (13). Predicted $(\nu')^{-1}$ values are afterwards plotted over the chosen reciprocal molalities $(m_S^{hyp})^{-1}$. In the final step, the predicted concentration-based Michaelis constant K_M^{pre} is determined according to Eq. (9). The process to determine K_M^{pre} is illustrated in **Scheme 1**.

As can be seen, the major aspect for the prediction of the Michaelis constants is the ability to predict the substrate activity coefficients. For this, a physically sound model, namely the electrolyte perturbed-chain statistical associating fluid theory (ePC-SAFT) was used in this work. This model has already been applied successfully to complex mixtures containing low-soluble molecules [24], PEG and salts [25] and electrolytes [20] while also being applied

Scheme 1. Steps for the prediction of the concentration-based Michaelis constant K_M^{pre} under the influence of co-solvents. Predictions are based on the determined activity-based Michaelis constant K_M^a .

simultaneously to mixtures with up to eight components [4], and thus, it provides a reliable model basis for this work.

The ePC-SAFT equation of state is based on PC-SAFT, developed and proposed by Gross and Sadowski [26] and extended for electrolyte systems by Cameretti et al. [18] ePC-SAFT provides an expression for the residual Helmholtz energy a^{res} calculated from different contributions as shown in Eq. (14):

$$a^{res} = a^{hc} + a^{disp} + a^{assoc} + a^{ion} \quad (14)$$

In Eq. (14), the reference system is seen as a chain of hard spheres, which is represented by the contribution a^{hc} . The perturbations to this hard-chain reference system are accounted for in ePC-SAFT by the molecular dispersive interactions, characterised by the Van der Waals energy incorporated in a^{disp} and by the associative hydrogen bonding forces represented in a^{assoc} . As an addition for electrolyte systems, the Coulomb interactions based on the Debye-Hückel equation are expressed by a^{ion} . Based on a^{res} , fugacity coefficients φ can be calculated which allow determining the activity coefficients γ_s^x using Eq. (15).

$$\gamma_s^x = \frac{\varphi_i(T, p, \vec{x})}{\varphi_{0i}(T, p, x_i = 1)} \quad (15)$$

In Eq. (15), $0i$ denotes the pure component, which is the reference state at the same temperature T and pressure p as the actual solution of the composition $\vec{x}$. This means that activity coefficients can be estimated independent of the amount of components, temperature and pressure of the solution regarded. Eq. (15) is finally used with Eq. (12) to obtain the molality-based γ_s^m .

2.2. Kinetic assays

In this work, a pseudo-one-substrate reaction is presented using the hydrolysis of SPNA catalysed by the enzyme α -CT. The reaction mechanism is given in **Scheme 2**.

The kinetic measurements have been discussed already in [7] and are briefly summarised here. Lyophilized powder of α -CT was used as catalyst, and trimethylamine N-oxide (TMAO) and urea were used as co-solvents. Measurements were carried out in Tris-HCl buffer (100 mmol/kg_{water} tris(hydroxymethyl)aminomethane, pH 8.0). The kinetic measurements of the neat and co-solvent reaction mixtures of the SPNA hydrolysis reactions were performed in a stopped-flow system (HPSF-56 of Hi-Tech Scientific) [27, 28]. In a first step, the substrate stock solution

Scheme 2. Reaction scheme for the hydrolysis of SPNA catalysed by α -chymotrypsin. Products of the hydrolysis reaction are N-(3-carboxypropanoyl)phenylalanine and p-nitroaniline, respectively.

containing SPNA and the respective co-solvent in a 100 mol/kg_{water} Tris-HCl buffer at pH 8 and the enzyme stock solution containing the respective co-solvent in a 100 mol/kg_{water} Tris-HCl buffer at pH 8 were prepared and loaded for injection in the measurement cell. After simultaneous injection, the measurement cell was constantly monitored for the extinction at 410 nm wavelength, allowing the determination of the time-dependent change in the 4-NA concentration. The pH values of the stock solutions were measured directly before the start of the reaction to ensure no pH effect on K_M^{pre} ; a pH electrode was used from Mettler Toledo with an uncertainty of ± 0.01 . The measured systems presented in this work are given in **Table 1**.

2.3. Results and discussion

In a first step, the concentration-based Michaelis constant K_M^{obs} was determined under neat conditions. The respective Lineweaver-Burk plot is given in **Figure 2**.

As can be seen from **Figure 2**, a linear relation between the reciprocal molality of the substrate m_{SPNA}^{-1} and the reciprocal normalised reaction rate $(\nu')^{-1}$ can be observed. This relation allowed the determination of K_M^{obs} ; as a result, a value of 1.76 ± 0.12 mmol/kg_{water} [7] was obtained for the SPNA hydrolysis. The activity-based Michaelis constant K_M^a was then obtained with activity coefficients of SPNA, which were predicted for each substrate molality with ePC-SAFT. The pure component and binary interaction parameters used for the ePC-SAFT prediction are listed in **Tables 2** and **3**.

Note that in a first step, mole-fraction-based activity coefficients were obtained with ePC-SAFT. Eq. (12) was used to convert these into molality-based activity coefficients; these were used throughout this work. In the next step, a plot of the determined $(\nu')^{-1}$ over the predicted reciprocal a_{SPNA}^{-1} was created. Based on this plot, K_M^a was determined in analogy to the determination of K_M^{obs} as shown in **Figure 2**, resulting in a value of $K_M^a = 0.0686$. This value was used as input value for the prediction of co-solvent influence on K_M^{obs} according to **Figure 2**. The comparison between this prediction and the experimental K_M^{obs} values is shown in **Figure 3** and **Table 4**.

Co-solvent	$m_{co-solvent}$ (mol/kg _{water})	m_{SPNA} (mmol/kg _{water})
Neat	—	0.125–1
TMAO	0.5	0.125–1
Urea	1	0.250–1
DMSO	2.1	0.250–1
DMSO	4.2	0.125–1

Enzyme concentration was 8 μ mol/kg_{water} in all kinetic assays.

Table 1. Overview of the measured systems to determine concentration-based Michaelis constants K_M^{obs} , adapted from [7], including the co-solvent and its concentration and the initial SPNA concentration range regarded.

Figure 2. Lineweaver-Burk plot for the determination of the concentration-based Michaelis constant of SPNA K_M^{obs} at $T = 25^\circ\text{C}$, $p = 1$ bar and $\text{pH} = 8$ in Tris-HCl buffer [7]. The plot shows experimental data points of the neat measurements (squares) which are obtained from the inverse turnover frequency $(\nu')^{-1}$ over the inverse substrate molality of SPNA $m_{SPNA}^{-1} \cdot K_M^{obs}$ was obtained by linear regression of the experimental data and extrapolation to the abscissa as shown.

Component	m_i (–)	σ_i (Å)	$\frac{u_i}{k_B}$ (K)	N_i^{assoc}	$\frac{\epsilon_i B_i}{k_B}$ (K)	$\kappa^{A_i B_i}$ (–)
Water [29]	1.204	[A]	353.95	1:1	2425.7	0.0451
DMSO [29]	2.922	3.28	355.69	1:1	0	0.0451
Urea [29]	4.242	2.45	368.23	1:1	3068.7	0.0010
TMAO [30]	8.93	2.25	245.44	1:1	0	0.0451
SPNA [7]	13.500	4.00	249.95	2:2	4351.0	0.0090

[A] $\sigma_i = 2.7927 + 10.11 \cdot \exp(-0.01775 \cdot T) - 1.417 \cdot \exp(-0.01146 \cdot T)$, T in Kelvin.

Table 2. ePC-SAFT pure-component parameters from [7, 29, 30].

As can be seen in **Figure 3** and **Table 4**, an accurate prediction of the co-solvent-induced changes in K_M^{obs} is possible. For both DMSO concentrations, predictions are even quantitatively correct within the experimental uncertainties. This is of special importance for the hydrolysis reaction under investigation since DMSO has the strongest impact on K_M^{obs} . The big advantage of K_M^a over K_M^{obs} is that it is a constant value independent of the co-solvent. This fact further

Mixture	k_{ij} (-)
Water-DMSO [30]	-0.065
Water-urea [30]	-0.044
Water-TMAO [30]	-0.149
Water-SPNA [7]	-0.132
DMSO-SPNA [7]	-0.117
Urea-SPNA [7]	-0.203
TMAO-SPNA [7]	-0.220

Table 3. ePC-SAFT binary interaction parameters [7, 29, 30].

Figure 3. Comparison between experimental concentration-based Michaelis constants K_M^{obs} (light grey bars) at $T = 25^\circ\text{C}$, $p = 1$ bar and $\text{pH} = 8$ in Tris-HCl buffer and the predicted Michaelis constants K_M^{pre} (dark grey bars). For the predictions, a constant K_M^a value of 0.0686 was used and the activity coefficients were predicted with ePC-SAFT based on the parameters from Tables 2 and 3. Reprinted from [7].

allows predicting K_M^{obs} without the need for additional experimental data. This proves the validity of the proposed modelling approach for pseudo-one-substrate reactions and validates the assumption that co-solvent-substrate interactions are responsible for the dependence of K_M^{obs} on co-solvents. Thus, this indirectly disproves that enzyme-co-solvent effects are responsible for such changes of K_M^{obs} . However, as enzyme-catalysed reactions are mostly multi-substrate reactions with two substrates of low concentrations, the following section presents the transfer of the gained insight and methods to two-substrate reactions.

Co-solvent	$m_{co-solvent}$ (mol/kg _{water})	K_M^{obs} (mmol/kg _{water})	K_M^{pre} (mmol/kg _{water})
TMAO	0.5	1.93 ± 0.19	2.38
Urea	1	2.50 ± 0.21	3.51
DMSO	2.8	3.08 ± 0.54	3.48
DMSO	4.2	5.96 ± 0.95	6.45

K_M^{pre} were predicted using K_M^a determined from experimental $K_M^{obs} = 1.76$ mmol/kg_{water} of the neat reaction [7].

Table 4. Comparison between the experimental K_M^{obs} with the respective predicted values K_M^{pre} under the influence of the co-solvents TMAO, urea or DMSO at $T = 25^\circ\text{C}$, $p = 1$ bar and pH = 8 in Tris-HCl buffer.

3. Two-substrate reactions

3.1. Theoretical background

3.1.1. Concentration-based approach

As presented in Section 2.1.1 ('pseudo') one-substrate reactions occur seldom in enzyme catalysis. Enzyme catalysis often requires co-substrate that is present in a limiting concentration (e.g., NADH, ATP, GTP). A two-substrate reaction can be described by Eq. (16), which cannot be simplified further:

$$v' = \frac{k_{cat} \cdot m_{S1} \cdot m_{S2}}{K_{iS1}^{obs} \cdot K_{MS2}^{obs} + K_{MS1}^{obs} \cdot m_{S2} + K_{MS2}^{obs} \cdot m_{S1} + m_{S1} \cdot m_{S2}} \quad (16)$$

Two-substrate reactions can have a specific binding order attached to them. To account for this, the inhibition constant of S1 K_{iS1}^{obs} based on the Haldane relation was accounted for in this work; if K_{iS1}^{obs} is lower than $K_{M,S1}^{obs}$, an ordered mechanism is present in which S1 has to bind first [8, 31]. The Lineweaver-Burk linearization of Eq. (16) leads to Eq. (17):

$$\underbrace{\frac{1}{v'}}_y = \underbrace{\left(\frac{K_{iS1}^{obs} \cdot K_{MS2}^{obs}}{k_{cat} \cdot m_{S2}} + \frac{K_{MS1}^{obs}}{k_{cat}} \right)}_m \cdot \underbrace{\frac{1}{m_{S1}}}_x + \underbrace{\left(\frac{K_{MS2}^{obs}}{k_{cat} \cdot m_{S2}} + \frac{1}{k_{cat}} \right)}_b \quad (17)$$

Note that Eq. (17) does not show any direct relation between the Michaelis constants and the ordinate, slope or the abscissa of the linearization. In the case of two-substrate reactions, a two-step linearization process is suggested. For this, the molality of one of the substrates, in this case m_{S2} , is chosen to be at least 50 times higher than m_{S1} . Under this assumption, a so-called *primary plot* can be created. For this, different levels of m_{S2} that are regarded to be constant over the short reaction time are chosen for varying m_{S1} ; then, a family of straight lines are obtained as shown exemplarily in **Figure 4**.

Each of the straight lines in **Figure 4** has its own slope (Sl^{prim}) and ordinate (Or^{prim}); both, Sl^{prim} and Or^{prim} are a function of m_{S2} as shown in Eqs. (18) and (19).

Figure 4. Exemplary *primary plot* for a two-substrate reaction obtained from plotting the inverse turnover frequency $(v')^{-1}$ over the inverse substrate molality of substrate 2 m_{S2}^{-1} for different pseudo-constant molalities of substrate 1 m_{S1} . Molalities m_{S1} increase in the order of $m_{S1, \text{squares}} > m_{S1, \text{circles}} > m_{S1, \text{triangles}}$.

$$Sl^{prim} = \frac{K_{iS1}^c \cdot K_{MS2}^c}{k_{cat}} \cdot \frac{1}{m_{S2}} + \frac{K_{MS1}^c}{k_{cat}} \quad (18)$$

$$Or^{prim} = \frac{K_{MS2}^c}{k_{cat}} \cdot \frac{1}{m_{S2}} + \frac{1}{k_{cat}} \quad (19)$$

Eqs. (18) and (19) again show a linear correlation between Sl^{prim} and m_{S2}^{-1} as well as between Or^{prim} and m_{S2}^{-1} , respectively. This allows for another linearization step represented in two *secondary plots* in **Figure 5**.

Figure 5. Exemplary *secondary plot* for Or^{prim} (left) and Sl^{prim} (right) over the reciprocal pseudo-constant molalities of m_{S1}^{-1} derived from the *primary plot* given in **Figure 4**.

SI_{SI}^{sec} , Or_{SI}^{sec} , SI_{Or}^{sec} and Or_{Or}^{sec} obtained from the *secondary plots* are defined according to Eqs. (20)–(23):

$$SI_{SI}^{sec} = \frac{K_{iS1}^{obs} \cdot K_{MS2}^{obs}}{k_{cat}} \quad (20)$$

$$Or_{SI}^{sec} = \frac{K_{MS1}^{obs}}{k_{cat}} \quad (21)$$

$$SI_{Or}^{sec} = \frac{K_{MS2}^{obs}}{k_{cat}} \quad (22)$$

$$Or_{Or}^{sec} = \frac{1}{k_{cat}} \quad (23)$$

The relations shown in Eqs. (20)–(23) are finally used to determine K_{MS1}^{obs} , K_{MS2}^{obs} , k_{cat} and K_{iS1}^{obs} .

3.1.2. Activity-based approach

The determination of activity-based Michaelis constants $K_{M,S1}^a$ and $K_{M,S2}^a$ for two-substrate reactions is analogous to pseudo-one-substrate reactions. As for the pseudo-one-substrate reaction, molalities in Eq. (17) are replaced with activities as shown in Eq. (24):

$$\underbrace{\frac{1}{v'}}_y = \underbrace{\left(\frac{K_{iS1}^a \cdot K_{M,S2}^a}{k_{cat} \cdot a_{S2}} + \frac{K_{MS1}^a}{k_{cat}} \right)}_m \cdot \underbrace{\frac{1}{a_{S1}}}_x + \underbrace{\left(\frac{K_{MS2}^a}{k_{cat} \cdot a_{S2}} + \frac{1}{k_{cat}} \right)}_b \quad (24)$$

From Eq. (24), a *primary plot* is created as described in Section 3.1.1 in which $(v')^{-1}$ is plotted over a_{S1}^{-1} . Afterwards, the two *secondary plots* are created by plotting the Or^{prim} and SI^{prim} of the *primary plot* over a_{S1}^{-1} to finally obtain the activity-based kinetic constants K_{iS1}^a , K_{MS1}^a and K_{MS2}^a as described for the concentration-based approach in Section 3.1.1.

Predictions for the co-solvent influence on K_{MS1}^{obs} and K_{MS2}^{obs} are performed in analogy to pseudo-one-substrate reactions: Two molalities of S1 m_{S1}^{hyp} for two molalities of S2 m_{S2}^{hyp} have to be chosen; then, the required activity coefficients have to be predicted in order to create a predicted *primary plot*; the *secondary plots* are then constructed by plotting Or^{prim} and SI^{prim} over the chosen reciprocal molalities $(m_{S2}^{hyp})^{-1}$. In a final step, the predicted Michaelis constants K_{MS1}^{pre} and K_{MS2}^{pre} are obtained from the *secondary plots*. The prediction process is illustrated in **Scheme 3**.

3.2. Materials and methods

In this work, the reduction of acetophenone by two different enzymes, ADH 270 and ADH 200, was investigated as model reaction for a two-substrate reaction. The reaction scheme is given in **Scheme 4**. Kinetic data for the ADH 270 were taken from [23].

Scheme 3. Steps for the prediction of the concentration-based Michaelis constants K_{MS1}^{pre} and K_{MS2}^{pre} under the influence of co-solvents. Predictions are based on the determined activity-based Michaelis constants K_{MS1}^a and K_{MS2}^a .

Scheme 4. Reaction scheme for the reduction of acetophenone to 1-phenylethanol with the co-substrate nicotinamide adenine dinucleotide in its protonated form (NADH+H⁺) and its deprotonated form (NAD⁺) catalysed by two different genetically modified alcohol dehydrogenases recombinant from *E. coli* (evo-1.1.270; evo-1.1.200).

3.2.1. Chemicals

2-[4-(2-hydroxyethyl)piperazin-1-yl]ethanesulfonic acid (HEPES) and polyethylene glycol 6000 (PEG 6000) were purchased from VWR. Acetophenone (ACP) and NADH were purchased from Sigma Aldrich. Sodium hydroxide was purchased from Bernd Kraft GmbH. The genetically modified enzyme alcohol dehydrogenase 200 (evo-1.1.20) expressed recombinant in *E. coli* was purchased from Evoxx. All chemicals were used without further purification, and all samples were prepared using Millipore water from the Milli-Q provided by Merck Millipore as stated in the chemical provenance (Table 5). Kinetic results using the genetically modified enzymes alcohol dehydrogenase 270 (evo-1.1.270) were taken from [23].

Compound	Purity	CAS	Supplier
2-[4-(2-hydroxyethyl)piperazin-1-yl]ethanesulfonic acid (HEPES)	>99%	7365-459	VWR
Polyethylene glycol 6000	—	25322-68-3	VWR
Acetophenone (ACP)	>99%	98-86-2	S
NADH	>97%	606-68-8	S
Sodium hydroxide	>98%	1310-73-2	BK
Alcohol dehydrogenase 200 (evo-1.1.200)	30%	evo-1.1.200	E

S = Sigma Aldrich Chemie GmbH; VWR = VWR International GmbH; BK = Bernd Kraft GmbH; E = Evonx technologies GmbH.

Table 5. Chemical provenance table for the components measured in this work.

3.2.2. Kinetic assays

Reactions were carried out in an HEPES buffer (0.1 mol/kg_{water}) at pH 7. The pH of the buffer and each sample was measured using a pH electrode from Mettler Toledo (uncertainty ± 0.01) and adjusted with sodium hydroxide when required. For measurements of the co-solvent influence, 17 wt.% of PEG 6000 was added to the buffer. In the first step, the substrate solutions of ACP were prepared in equal number to the different NADH concentrations measured. Buffer was added to 5 ml Eppendorf cups, and ACP was added gravimetrically afterwards using the XS analytical balance provided by Mettler Toledo (uncertainty ± 0.01 mg). Eppendorf cups were filled to the maximum capacity in order to decrease losses of ACP to the vapour phase. The ACP stock solutions were preheated in an Eppendorf ThermoMixer C at 25°C. ACP concentrations of the neat reaction were 20, 30 and 40 mmol/kg_{water} and 60, 80 and 100 mmol/kg_{water} for the PEG 6000 measurements, respectively. NADH was added gravimetrically to the ACP solution after preheating. Each sample was prepared directly before measurements due to reported long-term instability of NADH in solution [32]. NADH concentrations were chosen to be 0.15, 0.2, 0.25, 0.3, 0.35 and 0.4 mmol/kg_{water}. The enzyme stock solution was prepared by gravimetrically adding 1 wt.% of enzyme to 2 ml of buffer with direct storage on ice for the period of all measurements to ensure enzyme stability and activity. To initiate the kinetic measurements, 20 mg of the enzyme solution was transferred into a quartz cuvette SUPRASIL TYP 114-QS from Helma Analytics which was preheated to 25°C while being placed in an Eppendorf Biospectrometer. After addition of 1 g of the substrate solution containing ACP and NADH, the measurement of the extinction over time at 340 nm wavelength was initiated.

3.3. Results and discussion

3.3.1. ADH 270

In a first step, the *primary plot* for the ACP reduction catalysed by ADH 270 was determined under neat conditions. For this, $(\nu')^{-1}$ is plotted over m_{NADH}^{-1} for pseudo-constant m_{ACP} levels of 20, 30 and 40 mmol/kg_{water} in **Figure 6**.

Figure 6. Primary plot based on Eq. (17) for the ACP reduction catalysed by ADH 270 under neat conditions at $T = 25^\circ\text{C}$, $p = 1$ bar and $\text{pH} = 7$ in HEPES buffer [23]. The reciprocal turnover frequency normalised to the total enzyme concentration $(v')^{-1}$ is plotted over the reciprocal initial molality of NADH m_{NADH}^{-1} for ACP molalities of 20 (triangles), 30 (squares) and 40 $\text{mmol/kg}_{\text{water}}$ (circles). Lines represent the respective fit lines required for further data analysis.

A linear correlation of $(v')^{-1}$ over m_{NADH}^{-1} can be observed from **Figure 6**. As described in Section 3.1.1, this correlation is used for the creation of the *secondary plots* shown in **Figure 7**.

Figure 7 shows the required linear correlation between Or^{prim} and Sl^{prim} over m_{ACP}^{-1} required for the determination of the Michaelis constants $K_{M,\text{NADH}}^{\text{obs}}$ and $K_{M,\text{ACP}}^{\text{obs}}$ according to Eqs. (20)–(23). Applying the relations given in Eqs. (20)–(23), the Michaelis constant of NADH

Figure 7. Secondary plots based on Eqs. (18) and (19) for the ACP reduction catalysed by ADH 270 under neat conditions at $T = 25^\circ\text{C}$, $p = 1$ bar and $\text{pH} = 7$ in HEPES buffer [23]. Left: Ordinates Or^{prim} of the fit lines resulting from the primary plot are plotted over the reciprocal initial molality of ACP m_{ACP}^{-1} . Right: Slopes Sl^{prim} of the fit lines resulting from the primary plot are plotted over the reciprocal initial molality of ACP m_{ACP}^{-1} . Lines represent the respective fit lines required for further data analysis.

$K_{M,NADH}^{obs} = 0.37 \pm 0.09 \text{ mmol/kg}_{water}$ and of ACP $K_{M,ACP}^{obs} = 18.56 \pm 3.23 \text{ mmol/kg}_{water}$ were determined [23]. Afterwards, activity coefficients for NADH and ACP were predicted for the respective molalities; these ePC-SAFT predictions are based on the pure-component and binary interaction parameters listed in **Tables 6** and **7**. Based on the activities of NADH a_{NADH} and ACP a_{ACP} , the respective *primary* and *secondary* plots were created.

In analogy to the concentration-based approach, activity-based Michaelis constants were determined (Section 3.1.2) to be $K_{M,NADH}^a = 5.649 \cdot 10^{-8}$ and $K_{M,ACP}^a = 0.640$. As can be seen, activity-based Michaelis constants can be completely different from their concentration-based pendants; they even do not have any unit due to the definition of the activity as shown in Eq. (12). In the next step, a prediction of the co-solvent influence of 17 wt.% of PEG 6000 on $K_{M,ACP}^{obs}$ and $K_{M,NADH}^{obs}$ was performed as described in Section 3.2.1. These predictions were compared to experimental results given in **Figure 8** and **Table 8**.

As can be seen from **Figure 8** and **Table 8**, predictions of the co-solvent influence of 17 wt.% of PEG on $K_{M,NADH}^{obs}$ and $K_{M,ACP}^{obs}$ of the ACP reduction catalysed by ADH 270 are in very good agreement with experimental data. Upon addition of 17 wt.% PEG 6000, $K_{M,NADH}^{obs}$ decreased by a factor of two, while $K_{M,ACP}^{obs}$ increased by a factor of 2.5. Both trends were predicted

Component	m_i (–)	σ_i (Å)	$\frac{u_i}{k_B}$ (K)	N_i^{assoc}	$\frac{\epsilon_{A_i B_i}}{k_B}$ (K)	$\kappa^{A_i B_i}$ (–)
Water [29]	1.204	[A]	353.95	1:1	2425.7	0.0451
ACP [4]	3.40	3.65	322.00	1:1	0	0.0451
NADH [33]	27.27	2.21	260.72	8:8	358.2	0.0001
PEG [25]	$M_{PEG} \cdot 0.05$	2.90	204.60	4:4	1799.8	0.020
Na ⁺ [34]	1	2.82	230	–	–	–
OH [–] [34]	1	2.02	650.00	–	–	–

$$[A] \sigma_i = 2.7927 + 10.11 \cdot \exp(-0.01775 \cdot T) - 1.417 \cdot \exp(0.01146 \cdot T).$$

Table 6. ePC-SAFT pure-component parameters.

Binary pair	k_{ij} (–)
Water-ACP [4]	0.0330
Water-NADH [33]	–0.0585
Water-PEG [25]	[A]
Water-Na ⁺ [34]	[B]
Water-OH [–] [34]	–0.25
Na ⁺ -OH [–] [34]	0.649

$$[A] k_{ij}(T) = -0.135 + 0.0023439 \cdot (T[K] - 298.15).$$

$$[B] k_{ij}(T) = 0.00045485 - 0.007981 \cdot (T[K] - 298.15).$$

Table 7. ePC-SAFT binary interaction parameters k_{ij} .

Figure 8. Comparison between the experimentally measured Michaelis constants K_M^{obs} of ACP and NADH under neat reaction conditions (white bars) and under the influence of 17 wt.% PEG 6000 (striped bars) for the reduction of ACP catalysed by ADH 270 at $T = 25^\circ\text{C}$, $p = 1$ bar and $\text{pH} = 7$. The grey bars present the prediction of the respective K_M^{pre} based on the determined activity-based K_M^a from the experimental neat data [23]. Required activity coefficients were calculated with ePC-SAFT based on the parameters from **Tables 6** and **7**.

	$K_{M,NADH}^{obs} \left[\frac{\text{mmol}}{\text{kg}_{\text{water}}} \right]$	$K_{M,NADH}^{pre} \left[\frac{\text{mmol}}{\text{kg}_{\text{water}}} \right]$	$K_{M,ACP}^{obs} \left[\frac{\text{mmol}}{\text{kg}_{\text{water}}} \right]$	$K_{M,ACP}^{pre} \left[\frac{\text{mmol}}{\text{kg}_{\text{water}}} \right]$
Neat	0.79 ± 0.08	—	7.67 ± 0.37	—
17 wt.% PEG 6000	0.377 ± 0.09	0.372	18.56 ± 3.23	23.00

Activity coefficients required for the prediction were calculated with ePC-SAFT based on the parameters from **Tables 6** and **7**.

Table 8. Overview of the Michaelis constants under neat reaction conditions and the comparison between predicted K_M^{pre} and experimentally determined Michaelis constants K_M^{obs} [23] for the reduction of ACP catalysed by ADH 270 at $T = 25^\circ\text{C}$, $p = 1$ bar and $\text{pH} = 7$.

accurately with ePC-SAFT. This shows that the influence of PEG 6000 on the K_M^{obs} values is caused by non-covalent molecular interactions between the co-solvent and the substrates instead of co-solvent-enzyme interactions.

3.3.2. ADH 200 and comparison to ADH 270

To further validate this approach, the ACP reduction was also investigated with ADH 200 as catalyst. This step is important to support the hypothesis that co-solvent-substrate interactions determine the co-solvent influence on $K_{M,ACP}^{obs}$ and $K_{M,NADH}^{obs}$. However, it becomes obvious from **Table 9** that ADH 200 shows a completely different kinetic profile under neat conditions.

Figure 9. Comparison between the experimentally measured Michaelis constants K_M^{obs} for ACP and NADH from this work under neat reaction conditions (white bars) and under the influence of 17 wt.% PEG 6000 (striped bars) for the reduction of ACP catalysed by ADH 200 at $T = 25^\circ\text{C}$, $p = 1$ bar and $\text{pH} = 7$. The grey bars present the predicted values for K_M^{pre} based on the determined activity-based K_M^a from the experimental neat data. Required activity coefficients were predicted with ePC-SAFT based on the parameters from **Tables 6** and **7**.

Enzyme	$K_{M,NADH}^{obs} \left[\frac{\text{mmol}}{\text{kg}_{\text{water}}} \right]$	$K_{M,NADH}^a [-]$	$K_{M,ACP}^{obs} \left[\frac{\text{mmol}}{\text{kg}_{\text{water}}} \right]$	$K_{M,ACP}^a [-]$
ADH 270 [23]	0.79 ± 0.08	$5.65 \cdot 10^{-8}$	7.67 ± 0.37	0.640
ADH 200 [this work]	0.086 ± 0.027	$1.16 \cdot 10^{-8}$	4.08 ± 1.03	0.749

Table 9. Comparison between the Michaelis constants of NADH and ACP for the reduction of ACP for neat reaction conditions at $T=25^\circ\text{C}$, $p=1$ bar and $\text{pH}=7$ in HEPES buffer. Two different enzymes were used as catalyst, ADH 270 and ADH 200. Activity coefficients required for the prediction of K_M^a were calculated with ePC-SAFT based on the parameters from **Table 6** and **Table 7**.

Table 9 shows that $K_{M,NADH}^{obs}$ ($K_{M,ACP}^{obs}$) using ADH 200 are 9 times (2 times) lower than $K_{M,NADH}^{obs}$ ($K_{M,ACP}^{obs}$) using ADH 270 for identical conditions. Nevertheless, this is an expected behaviour. It can be further observed from **Table 9** that also the activity-based Michaelis constants $K_{M,NADH}^a$ and $K_{M,ACP}^a$ are different for ADH 200 and ADH 270 for the ACP reduction at same conditions. The prediction results of the influence of 17 wt.% PEG 6000 on K_M^{obs} of the reaction catalysed by ADH 200 are given in **Figure 9**.

Figure 9 shows that ePC-SAFT is able to predict the change of $K_{M,NADH}^{obs}$ and $K_{M,ACP}^{obs}$ under the influence of 17 wt.% of PEG 6000 for ADH 200 in good agreement with experimental data. The same ePC-SAFT parameters were used as for the prediction of the same reaction catalysed by ADH 270. This is a further validation of our approach as it shows that predictions are possible independent of the enzyme catalysing the reaction. For both enzymes, ADH 200 and ADH 270, the co-solvent influences on the substrate activities were the key for predicting the change in K_M^{obs} .

4. Conclusion

In this work, it was found that experimental Michaelis constants K_M^{obs} of a pseudo-one-substrate and a two-substrate reaction were strongly dependent on the co-solvent present in the reaction mixture. This co-solvent effect was assumed to be introduced by the thermodynamic non-ideality caused by molecular interactions. These are expressed as activity coefficients of the substrate(s), which were predicted by the equation of state ePC-SAFT. By accounting for the activity coefficients of the substrate(s), the concentration-based Michaelis constants K_M^{obs} were expressed as activity-based values K_M^a . This approach focused on investigating enzyme-independent interactions between co-solvent and the substrate(s) of the reaction; this has the advantage that K_M^a is a constant value independent of kind or concentration of co-solvent, while the experimentally observed K_M^{obs} values depend on co-solvent. The availability of K_M^a then allowed predicting co-solvent-induced changes in K_M^{obs} and therewith (1) proved the hypothesis that substrate-co-solvent interactions are responsible for changes of K_M^{obs} upon co-solvent addition and (2) enzyme-co-solvent interactions do not play a role for the observed changes in K_M^{obs} . Based on these findings, we could suggest that K_M^a should be considered instead of K_M^{obs} for investigations of enzyme-catalysed reactions in order to significantly reduce experimental effort and to gain new insight and understanding of the co-solvent-substrate-enzyme interactions present in more complex reaction mixtures, approaching *in cellulo* reaction conditions. We showed the feasibility of this by accurately predicting the influence of co-solvents (e.g., DMSO, urea or TMAO) on the Michaelis constants of a pseudo-one-substrate reaction as well as of a two-substrate ADH reaction. For the latter, the predictions were accurate for two different enzymes (ADH 200 and ADH 270) under investigation. This can be seen as another validation of the hypotheses (1) and (2).

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Conflict of interest

The authors declare no conflict of interest. Note that reference [23] is still under second review.

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