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Self-Consistent Mean-Field Theory for Room-Temperature Ionic Liquids

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1. Introduction

Research in room-temperature ionic liquids (RTILs) has exploded in the last two decades, which are marked by an exponential increase in the number of theoretical and experimental publications in this field. The typically good thermal stability, ionic conductivity, and solvability of RTILs make them superior electrolytes in many electrochemical applications, such as metal electrodeposition and energy storage.(Armand et al., 2009; Endres et al., 2008; Ohno, 2005; Simon & Gogotsi, 2008) The efficiency of RTILs in such applications is determined by a number of factors, one of which is the relationship between the interfacial structure of RTILs and their electrochemical properties. The use of RTILs as solvents in supercapacitors is of particular interest since they can generate significant electrical double-layer (EDL) capacitance due to the formation of thin layer of ions on an Angstrom-scale at RTIL-electrode interfaces.(Atkin & Warr, 2007; Baldelli, 2008; Horn et al., 1988; Mezger et al., 2008; 2009; Rivera-Rubero & Baldelli, 2004; Santos et al., 2006; Yuan et al., 2010) The formation of ultra thin EDL is mainly caused by the absence of any solvation shells around RTILs, which also enhances the accessibility of ions to penetrate nanoporous electrodes, thus increasing their useability in electrochemical applications.(Chmiola et al., 2008; Largeot et al., 2008) The precise form of EDL structure in RTILs has been a point of argument recently. Experimental results from the sum frequency generation spectroscopy suggest a monolayer of ion formed at the interface.(Baldelli, 2008; Rivera-Rubero & Baldelli, 2004) However, a similar study using the surface force apparatus,(Horn et al., 1988) atomic force microscopy,(Atkin & Warr, 2007; Atkin et al., 2009) and x-ray reflectometry (Mezger et al., 2009) indicate that an alternating layer of ions is instead present. Analytical and numerical models also predict the formation of alternating layer of counterions and coions on polar surfaces due to strong steric and electrostatic correlations in RTILs.(Fedorov & Kornyshev, 2008; Feng et al., 2009; Kornyshev, 2007; Lauw et al., 2009; 2010; Oldham, 2008; Reed et al., 2008) Such an alternating layer typically occurs through the so-called charge overcompensation/overscreening mechanism when the electrostatic screening length is practically less than the size of the ion.(Outhwaite et al., 1980; Parsons, 1990; Stillinger & Kirkwood, 1960) In the highly charged system like RTILs, the charge overcompensation

understandably occurs since the ions are rather bulky. At the RTIL-electrode interface, the surface charge would be overscreened by counterions in the Helmholtz layer and the resulting net charge would be further overcompensated by coions in the subsequent layer, and so on.

The formation of the EDL in RTILs at charged interfaces can induce a large electrostatic potential field ($\sim 10^9$ V/m), which would greatly influence the rate of electrochemical reactions at the interface and the overall EDL capacitance values. In general, the EDL capacitance reflects the extent to which the electrostatic potential at the interface is screened by the ions that accumulate there. A better screening is reflected by a higher capacitance value. This parameter contains a valuable information on the thickness of the EDL and the composition and polarization of ions at the interface. A correct analysis of the shape of the EDL capacitance curve in RTILs requires an *a priori* knowledge on the EDL structure as a function of the electrostatic potential field. Analytical model to study the relationship between the EDL structure and capacitance in RTILs has been carried out (Kornyshev, 2007; Oldham, 2008) using Poisson-Fermi equation to model spherical ions with certain excluded volume. (Bazant et al., 2009; Bikerman, 1942; Freise, 1952; Kilic et al., 2007) A similar study has been done using numerical model, such as molecular dynamic simulations, (Fedorov & Kornyshev, 2008; Feng et al., 2009) Monte Carlo simulations, (Trulsson et al., 2010) and the self-consistent mean-field theory (SCMFT). (Lauw et al., 2009; 2010) Numerical modelling techniques are generally more realistic to model RTILs than existing analytical approaches due to their ability to accommodate internal degree of freedoms in RTILs and complicated (non-spherosymmetrical) structures of RTILs. These aspects are typically not accessible in analytical models.

This chapter describes the use of SCMFT to predict the structure of RTILs at electrified interfaces and the corresponding EDL capacitance. Special attention is paid to study the effect of ion-size and specific (non-electrostatic) adsorption of ions on the shape of the EDL capacitance curve. Results from this study is used to shed light on the unusual shape of the differential capacitance curve in RTILs observed in experiments. In general, the capacitance curve in RTILs has a shape of inverse parabola or a camel-like with two maxima around the point of zero charge (pzc), (Alam et al., 2007; 2008; Lockett et al., 2008) which are in contrast to the parabola-shaped capacitance curve typically found in aqueous electrolytes.

In SCMFT, the EDL capacitance is studied based on a detailed molecular model of RTILs and the use of local (effective) dielectric constant. Each ion is modelled as a freely-jointed chain of segments. The local polarization is implemented by assigning a higher relative permittivity to polar (more conductive) components in RTILs and a lower value to less polar (less conductive) components. The effective relative permittivity, which depends on the local distribution of the polar and apolar components, is thus higher at the surface than in the bulk since the polar components of the counterion are accumulated on the electrode's surface. This is the opposite trend to the one typically found in aqueous electrolytes, (James & Healy, 1972; Teschke & de Souza, 1999) in which the ion polarizability is known to decrease in high electrostatic fields. Details of the SCMFT used to model RTILs at electrified interface are given in the following section.

2. Self-consistent mean-field theory

The SCMFT is a molecular modelling technique used to study physical and thermodynamic properties of systems at equilibrium. (Fleer et al., 1993; Leermakers et al., 2005) It has been successfully implemented in the past to predict the equilibrium structure in polymeric systems. (Claessens et al., 2004; Lauw et al., 2008; Lauw, 2009; Leermakers et al., 2003; Matsen,

1995; Thompson et al., 2001) Here, it is used to study RTILs by considering a grand canonical ensemble of small systems, in which each system consists of cations and anions adjacent to an electrified solid surface. A periodic boundary condition is applied to all sides perpendicular to the surface and a Neumann boundary condition on the side opposite to the surface to reflect bulk properties. Each ion is modelled as a chain of charged and uncharged segments which formed a tetramer, as shown in Fig. 1. This implies that the charged group is situated at the center and the uncharged segments are located at the arms of the tetramer. For the cation, the positively charged segment P is surrounded by four arms, where each arm is composed of n_A neutral segments A . For the anion, the negatively charged segment N is also surrounded by four arms, comprising n_B neutral segments B per arm. Each segment is identified by its ranking number s , which marks the position of the segment in the tetramer. The density of each segment at any points $\mathbf{r}$ in the system is quantified by its local volume fraction $\varphi(\mathbf{r})$. This relatively simple molecular model is a representation of typical RTILs with a similar ion-size and a well-hidden charged group.

Fig. 1. Schematic of the tetrameric cation (left) and anion (right) used in the SCMFT.

In SCMFT, the total free energy (F_{total}) of a small system is expressed as a sum of its enthalpic, entropic, and electrostatic components,

$$F_{total} = F_{enthalphy} + F_{entropy} + F_{electrostatic} \tag{1}$$

The enthalpic part of the free energy reads,

$$\frac{F_{enthalphy}}{k_B T} = \int \left[\frac{1}{2} \sum_{i,j} \chi_{ij} \varphi_i(\mathbf{r}) \varphi_j(\mathbf{r}) + \delta(\mathbf{r} - \mathbf{r}_S) \sum_i \chi_{iS} \varphi_i(\mathbf{r}) \right] d\mathbf{r} \tag{2}$$

where the first term is the mixing enthalpy based on the Flory-Huggins formulation,(Flory, 1953) and the second term is originated from the specific adsorption. The indices i and j refer to the segment type in the cation and anion, i.e., $\{i, j\} \in \{A, P, B, N\}$; the index S represents the electrode’s surface; χ_{ij} is the Flory-Huggins interaction parameter between segment- i and - j ; $\varphi_i(\mathbf{r})$ and $\varphi_j(\mathbf{r})$ are the volume fraction of segment- i and - j at point $\mathbf{r}$ in the system; $\delta(\mathbf{r} - \mathbf{r}_S)$ is the Dirac delta function at $\mathbf{r} = \mathbf{r}_S$, where $\mathbf{r}_S$ is the position of the electrode’s surface; χ_{iS} is the interaction parameter between segment- i and the surface. A more positive χ_{iS} indicates a more repulsion between segment- i and the electrode’s surface, and alternatively, a more negative χ_{iS} means segment- i has a stronger affinity towards the surface.

The entropic contribution to the total free energy is expressed as a sum of the translational entropy of the cation and anion, local mean-field interactions, and the additional term due to the incompressibility constraint of the system,

$$\frac{F_{entropy}}{k_B T} = \frac{Vf_+}{N_+} \ln \left(\frac{Vf_+}{N_+ Q_+} \right) + \frac{Vf_-}{N_-} \ln \left(\frac{Vf_-}{N_- Q_-} \right) - \int \left[\sum_i w_i(\mathbf{r}) \varphi_i(\mathbf{r}) + \lambda(\mathbf{r}) \left(1 - \sum_i \varphi_i(\mathbf{r}) \right) \right] d\mathbf{r} \quad (3)$$

In Equation 3, the volume of the system is denoted by V ; the indices $+$ and $-$ represent the cation and anion, respectively; f_+ and f_- are the total (volume) fraction of the cation and anion; N_+ and N_- are the total number of segments in the cation and anion; Q_+ and Q_- are the so-called partition function of the cation and anion; $w_i(\mathbf{r})$ is the potential of mean-force of segment- i at $\mathbf{r}$ and $\lambda(\mathbf{r})$ is the Lagrange multiplier at $\mathbf{r}$.

The electrostatic contribution to the free energy is expressed as a sum of all Coulombic interactions in the system as follows,

$$\frac{F_{electrostatic}}{k_B T} = -\frac{1}{2} \int \sum_i e v_i \varphi_i(\mathbf{r}) \psi(\mathbf{r}) d\mathbf{r} \quad (4)$$

where v_i is the valence of segment- i and $\psi(\mathbf{r})$ is the electrostatic potential at $\mathbf{r}$.

The total free energy F_{total} is extremized with respect to the order parameters ($w_i(\mathbf{r})$ and $\varphi_i(\mathbf{r})$), subject to the incompressibility constraint $\sum_i \varphi_i(\mathbf{r}) = 1$ at all $\mathbf{r}$. The results is a set of governing equations described in details below.

For the cation, the volume fraction of each segment is determined by the corresponding segment-weighting factor $q_+(\mathbf{r}, s)$ and its complementary factor $q'_+(\mathbf{r}, s)$. They quantify the probability to find a given segment in the cation with a ranking number s at point $\mathbf{r}$ in the system. The segment-weighting factor $q_+(\mathbf{r}, s)$ is calculated from the open-end of the arm towards the center of the tetramer, whereas the complementary segment-weighting factor $q'_+(\mathbf{r}, s)$ is calculated from the center of the tetramer towards the open-end of the arm. The overall connectivity of segments is governed by the Edwards diffusion equation, (Edwards, 1965)

$$\frac{\partial q(\mathbf{r}, s)}{\partial s} = \frac{a^2}{6} \nabla^2 q(\mathbf{r}, s) - \delta_{i_+, s} w_{i_+}(\mathbf{r}) q(\mathbf{r}, s) \quad (5)$$

where $q(\mathbf{r}, s)$ refers to either $q_+(\mathbf{r}, s)$ or $q'_+(\mathbf{r}, s)$, a is the size of the segment, $\delta_{i_+, s}$ is a Kronecker delta that equals to one if the segment-ranking number s of the cation is of type $i_+ \in \{A, P\}$ and zero otherwise. Equation 5 is solved numerically subject to the initial and boundary conditions of the system. Since the open-end of the arm is occupied by an uncharged segment A and the center of the tetramer by the charged segment P , the initial condition at the open-end is $q_+(\mathbf{r}, s_0) = \exp(-w_A(\mathbf{r}))$, whereas the initial condition at the center is $q'_+(\mathbf{r}, s_0) = [q_+(\mathbf{r}, s_{n_A})]^3$. The volume fraction $\varphi_{i_+}(\mathbf{r})$ of segment- i_+ in the cation is calculated from the convolution of $q_+(\mathbf{r}, s)$ and its complementary value $q'_+(\mathbf{r}, s)$,

$$\varphi_{i_+}(\mathbf{r}) = \frac{Vf_+}{N_+ Q_+} \int_0^{N_+} \delta_{i_+, s} q_+(\mathbf{r}, s) q'_+(\mathbf{r}, s) ds \quad (6)$$

in which $Q_+ = \int q_+(\mathbf{r}, s) q'_+(\mathbf{r}, s) d\mathbf{r}$ is the partition function of the cation, which is independent to the segment-ranking number.

For the anion, the volume fraction of segment- i_- , where $i_- \in \{B, N\}$, is calculated in a similar manner as its cation counterpart. The corresponding diffusion equation for the chain connectivity of segments in the anion is,

$$\frac{\partial q(\mathbf{r}, s)}{\partial s} = \frac{a^2}{6} \nabla^2 q(\mathbf{r}, s) - \delta_{i_-, s} w_{i_-}(\mathbf{r}) q(\mathbf{r}, s) \quad (7)$$

where $q(\mathbf{r}, s)$ now refers to either $q_-(\mathbf{r}, s)$ or $q'_-(\mathbf{r}, s)$, and $\delta_{i_-, s}$ equals to one if the segment-ranking number s of the anion is of type i_- and zero otherwise. The initial condition at the open-end becomes $q_-(\mathbf{r}, s_0) = \exp(-w_B(\mathbf{r}))$, whereas the initial condition at the center is $q'_-(\mathbf{r}, s_0) = [q_-(\mathbf{r}, s_{n_B})]^3$. The segment volume fraction in anion $\varphi_{i_-}(\mathbf{r})$ now reads,

$$\varphi_{i_-}(\mathbf{r}) = \frac{V f_-}{N_- Q_-} \int_0^{N_-} \delta_{i_-, s} q_-(\mathbf{r}, s) q'_-(\mathbf{r}, s) ds \quad (8)$$

where the partition function of the anion is $Q_- = \int q_-(\mathbf{r}, s) q'_-(\mathbf{r}, s) d\mathbf{r}$.

The free energy formulation in Equations 1-4 implies that the local volume fraction $\varphi(\mathbf{r})$ and the local mean-field potential $w(\mathbf{r})$ are not independent towards one another. However, in a thermodynamical equilibrium the relationship between these two order parameters can be written based on a so-called saddle-point approximation, i.e.,

$$\begin{aligned} w_i(\mathbf{r}) = & \sum_{j \in \{A, P, B, N\}, j \neq i} \chi_{ij} (\varphi_j(\mathbf{r}) - \varphi_j^b) + \chi_{is} \int \delta(\mathbf{r} - \mathbf{r}_s) d\mathbf{r} \\ & + \lambda(\mathbf{r}) + e v_i \psi(\mathbf{r}) - \frac{1}{2} \epsilon_0 (\epsilon_{r,i}(\mathbf{r}) - 1) |\nabla \psi(\mathbf{r})|^2 \end{aligned} \quad (9)$$

where the Flory-Huggins parameter χ_{ij} in the first term represents the magnitude of the mean-field interaction between segment- i and - j . A more positive χ_{ij} indicates a more repulsive interaction. The parameter φ_j^b is the volume fraction of segment- j in the bulk. The local electrostatic potential $\psi(\mathbf{r})$ in the fourth term is obtained from the Poisson law, $\epsilon_0 \nabla (\epsilon_r(\mathbf{r}) \nabla \psi(\mathbf{r})) = -\sum_i e v_i \varphi_i(\mathbf{r})$. The last term of Equation 9 is a contribution from the polarization charges. (Feynman et al., 1964) Here, the permittivity of RTIL is considered a function of the collective permittivity of its constituent segments. (Bohmer et al., 1990; Reis et al., 2009) The local relative permittivity of the system is thus calculated from a linear combination of the local composition of its components, i.e., $\epsilon_r(\mathbf{r}) = \sum_i \epsilon_{r,i} \varphi_i(\mathbf{r})$, where $i \in \{A, P, B, N, S\}$. This involves a heuristic approach to assign a specific value of the relative permittivity $\epsilon_{r,i}$ to each segment- i in the system under a constraint that the overall (bulk) relative permittivity of the RTIL still mimics experimental values. (Koeberg et al., 2007; Krossing et al., 2006)

A complete self-consistent mean-field (SCMF) calculation consists of the following four steps: (i) a set of initial potential of segments is randomly generated; (ii) the corresponding volume fraction of all segments are obtained from Equations (6) and (8) after solving the chain propagators in Equations (5) and (7) by using the Scheutjens-Fleer scheme; (Scheutjens & Fleer, 1979; 1980) (iii) the Poisson equation is used to calculate the value of local electrostatic potential; (iv) a new set of segment potentials is calculated from Equation 9. Steps (i)-(iv) are then repeated until the difference between the volume fraction from the previous two iterations at any point $\mathbf{r}$ is less than 10^{-7} , which indicates that the free energy is extremized and the order parameters are self-consistent. Multiple independent calculations were performed with random initial segment potentials to ensure the results satisfy the ergodicity condition.

3. EDL structure and capacitance in RTILs

To study the shape of EDL capacitance curve for RTIL with the same ion size and without non-electrostatic (specific) affinity towards the electrode's surface, a series of SCMF calculation is performed using a tetrameric model of cation and anion (cf. Fig. 1) with $n_A = n_B = 4$.¹ For simplicity, the volume fraction of ions is assumed to vary only in the direction perpendicular to the electrode's surface. This means that the volume fraction of ions are homogeneous throughout each plane parallel to the surface. The size of all segments are set equal to 3 Å, which is of a similar order of magnitude to an ethyl chain or a heterocyclic polar group in typical RTILs, such as pyrrolidinium and imidazolium rings. The system size is chosen large enough such that the bulk properties are reached within the boundaries of the modelled system. The relative permittivity of segments and electrode's surface used in the calculation are $\epsilon_{r,A} = \epsilon_{r,B} = 10$, $\epsilon_{r,P} = \epsilon_{r,N} = 30$, and $\epsilon_{r,S} = 10$. These values are chosen such that the relative permittivity of the modelled RTIL in the bulk is similar to the real value, which is ~ 11 -12. (Koeberg et al., 2007; Krossing et al., 2006) The interaction parameter $\chi_{AB} = 1$ is used to represent an adequate repulsion between uncharged segment-A of cation and -B of anion.

Fig. 2. (a) Full line: plot of the surface charge (σ_0) as a function of the surface potential (ψ_0). Dashed line: plot of the corresponding differential capacitance curve (C). The black and the blue curves are generated with and without the use of an effective dielectric constant, respectively. (b) Plot of the differential capacitance curve (black) compared to the integral capacitance curve (blue).

The surface charge (σ_0) and the differential capacitance (C) are plotted as functions of the surface potential (ψ_0) in Fig. 2a. For comparison, the differential and integral capacitance curves are depicted together in Fig. 2b. The differential capacitance is calculated from the first derivative of the surface charge (σ_0) with respect to ψ_0 , i.e., $C = \frac{\partial \sigma_0}{\partial \psi_0}$. The integral capacitance is obtained by dividing the surface charge with the surface potential, i.e., $K = \frac{\sigma_0}{\psi_0}$. Note that the value of differential capacitance based on an equilibrium model like SCMF can only be related to that obtained from impedance spectroscopy at very low frequencies. Figure 2a shows that the bell-shaped differential capacitance curve is obtained when a uniform dielectric constant of segments is used. In this case, the value used is $\epsilon_{r,A} = \epsilon_{r,P} = \epsilon_{r,B} = \epsilon_{r,N} = 11$. When the effective dielectric constant is taken into account, the differential capacitance curve has a camel-like shape with two maxima. This is also the case for the integral capacitance (cf.

¹ The detailed version of this part can be found in (Lauw et al., 2009).

Fig. 2b) although compared to the differential capacitance the maxima are reached at slightly larger potential values and the decrease in capacitance at both potential wings is less steep. The curve of surface charge in Fig. 2a comprises two regimes, namely a quasi-linear regime at low electrostatic potentials ($-0.63 \text{ V} < \psi_0 < 0.63 \text{ V}$) and a non-linear regime at high potentials ($|\psi_0| > 0.63 \text{ V}$). The term quasi-linear is used here since within this region the relationship between the surface charge and the surface potential appears to be linear, yet from the capacitance curve it is clear that the surface charge has a point of inflection at the pzc, which in this case is located at $\psi_0 = 0$. In the quasi-linear regime, the electrode's surface is still not yet fully saturated by counterions, whereas the counterions saturate the electrode's surface and accumulate further away towards the bulk in the non-linear regime, as illustrated by the set of volume fraction profile of cation and anion in Fig. 3. Note that the fluctuation of electrostatic potential at the interface at various applied potentials (cf. Fig. 4a) indicates that the charge overscreening takes place in both quasi-linear and non-linear regimes.

Fig. 3. Profile of the volume fraction of cation and anion at the interface at different surface potential values. The abscissa z indicates the distance from the electrode's surface.

Figure 2 shows that the capacitance curve has a camel-like shape, which is symmetric with respect to the pzc and reaches maxima at $|\psi_0| = 0.63 \text{ V}$. It is worth noting that the camel-shaped capacitance curve is not unique to RTILs. It was first observed decades ago in the study of aqueous solutions of NaI, NaF, KPF_6 , and KBF_4 on Au or Ag electrodes, where specific adsorptions occur (Clavilier & Huong, 1977; Grahame, 1947; Hamelin & Stoicoviciu, 1987; Valette, 1981). In aqueous electrolytes, the hump on the capacitance curves is typically a direct consequence of non-homogeneous polarization in the EDL (MacDonald, 1954; MacDonald & Barlow Jr., 1962; Parsons, 1961). Arguably, the primary cause for such a capacitance curve in RTILs may be different. The camel-shaped capacitance curves can be obtained using theoretical models, in which ions are considered to have finite sizes. This approach goes beyond typical Poisson-Boltzmann approximation which assumes ions as point charges. In SCMFT, the excluded volume effect is incorporated by modelling ions as segmented dendrimers with a sufficient repulsion between uncharged segments A and B in the branches of each cation and anion. It is apparent from Figure 2a that the excluded volume is not the only effect causing the camel-shaped capacitance curve. By considering the effective dielectric constant of RTILs as a function of the local segment density, it is shown that the polarizability of ions at the interface turns out to be another key factor. The camel-shaped capacitance curve can be analysed based on the potential-dependence of the structure of RTILs at the interface. This structure-property relationship is elaborated further as follows:

a) Within the quasi-linear regime ($|\psi_0| < 0.63$ V), the capacitance increases with the surface potential. Following the trend of the volume fraction profiles of ions shown in Fig. 3, one can conclude that at the points where the capacitance reaches its maximum values ($|\psi_0| = 0.63$ V), the electrode's surface is saturated with counterions. Between these two points, some coions can still be found at the surface. The alternating layer of ions can be considered as a series of capacitors with the corresponding capacitance value is obtained from $1/C = \sum_l 1/C_l$, where C_l is the capacitance of layer- l . Based on this representative formula, the capacitance of the EDL in RTILs is determined by a non-trivial balance between the thinning/thickening of each layer and the decreasing/increasing polarization. A higher capacitance value can be a result of thinner layers and/or a larger interfacial polarization. Results from SCMFT indicate that the thickness and periodicity of each alternate layer throughout the quasi-linear regime is relatively the same, whereas the local dielectric constants ϵ_r differ following the local distribution of molecular segments (cf. Fig. 4b for the case of $\psi_0 = -0.3$ V and -0.5 V). Therefore, an increasing capacitance in the quasi-linear regime is likely to be driven by an increasing polarization of RTILs at the interface.

b) Within the non-linear regime ($|\psi_0| > 0.63$ V), the surface charge is less than a linear function of the surface potential and the capacitance decreases with increasing surface potential. The physical interpretation is that the energy needed to bring one counterion from the bulk to the surface increases more than linearly with an increasing surface charge. In this regime, the interface is already saturated with counterions such that the EDL thickness grows with an increasing surface potential, as shown in Fig. 3 for $\psi_0 = -1$ V and -3 V. Moreover, the charged segment of the counterions is primarily located at the electrode's surface, causing a higher dielectric constant value there (cf. Fig. 4b). A thicker EDL overcomes the effect of an increasing polarization at the interface to lower the capacitance. The scaling of the capacitance in the non-linear regime is $C \propto |\psi_0|^{-0.82}$. As a comparison, the scaling for the bell-shaped capacitance curve is $C \propto |\psi_0|^{-0.60}$, which indicates that the effective dielectric constant plays an important role in determining the scale of the capacitance at the electrostatic potential wings.

Fig. 4. (a) Profile of the diffuse electrostatic potential at the interface at different surface potentials. (b) Profile of the corresponding local dielectric constant (ϵ_r).

In aqueous electrolyte solutions, an increasingly charged electrode leads to a more effective screening of the electrostatic potential. The screening effect intensifies as the interface is more densely populated by counterions which replace electroneutral water molecules. As a result, the curvature of $\sigma_0(\psi_0)$ goes beyond linear. At a first glance, the overall capacitance

curve of the EDL in aqueous electrolytes seems to differ from that in RTILs. The capacitance curve in aqueous electrolytes usually reaches a minimum at pzc and increases monotonically with surface potential, whereas the capacitance curve in RTILs has a camel-like shape. Nevertheless, under similar premises both curves would have the same camel-like shape if similar potential limits could be attained. This means that the maxima of the capacitance curve in aqueous electrolytes occur at potentials beyond the electrochemical window of water, such that one never observed this camel-shaped capacitance curve in reality.

The effects of different ion-size and specific adsorption of ions to the EDL capacitance in RTILs are discussed in the following two sections. The complete version of these sections can be found in (Lauw et al., 2010).

3.1 Effect of different ion-size

Results from the SCMFT described above were based on a uniform dendrimeric model of cation and anion, without taking into account ions of different size. In most RTILs, the anions are relatively smaller than the cations. Here, three size ratios of cation and anion are used to study the effect of ion-size on capacitance. This is achieved by varying the length of each arm in the anion while keeping the cation size the same. Three ratios of the arm's length used in this study are $n_A : n_B = 4:4$, $4:3$, and $4:2$. The differential capacitance curve for the three size ratios of cation and anion are plotted in Fig. 5a. Each differential capacitance curve has a camel-shaped feature, which is symmetric for RTIL with the same ion-size ($n_A:n_B = 4:4$) and asymmetric for ions with unequal size ($n_A:n_B = 4:3$ and $4:2$). The asymmetry is caused by the deviation in the corresponding $\sigma_0(\psi_0)$ curves at positive applied potentials, as shown in Fig. 5a. The comparison between the differential and integral capacitance curves for unequal ion-size is shown in Fig. 5b. Although in principle the shape of both curves are similar, the integral capacitance curve is non-continuous at $\psi_0 = 0$.

Fig. 5. (a) Plot of the differential capacitance (left) and the corresponding surface charge (right) as functions of the surface potential of the modelled RTIL with different ratios of $n_A:n_B$, as indicated. (b) Plot of the differential capacitance curve (black) and the integral capacitance curve (blue) for the case of $n_A:n_B = 4:3$.

It is known that the minimum differential capacitance is typically reached at the pzc, where the electrode's surface charge is practically zero. As described in the previous section, the quasi-linear regime is located around the pzc. For the modelled RTIL with $n_A:n_B = 4:4$, this regime is located within $-0.63 \text{ V} < \psi_0 < 0.63 \text{ V}$. It expands further for RTILs with unequal ion-size, i.e., $-0.73 \text{ V} < \psi_0 < 0.83 \text{ V}$ for $n_A:n_B = 4:3$, and $-0.83 \text{ V} < \psi_0 < 1.19 \text{ V}$ for $n_A:n_B = 4:2$. The complete list of the pzc, location of both maximum potential values ($\psi_0^{\text{max-}}$

and $\psi_0^{\text{max}+}$), and the extrema of the capacitance curves (C_{pzc} , $C_{\text{max-}}$, and $C_{\text{max+}}$) are shown in Table 1. Here, the indices max- and max+ indicate values at the maximum capacitance on the left-hand and right-hand sides of pzc, respectively. Parameters α_- and α_+ are the exponents from the scaling of the capacitance with respect to each surface potential wing in the non-linear regime, i.e., $C \propto |\psi_0|^{\alpha_-}$ for $\psi_0 < \psi_0^{\text{max-}}$ and $C \propto |\psi_0|^{\alpha_+}$ for $\psi_0 > \psi_0^{\text{max+}}$.

$n_A:n_B$	pzc (mV)	$\psi_0^{\text{max-}}$ (V)	$\psi_0^{\text{max+}}$ (V)	C_{pzc} ($\mu\text{F}/\text{cm}^2$)	$C_{\text{max-}}$ ($\mu\text{F}/\text{cm}^2$)	$C_{\text{max+}}$ ($\mu\text{F}/\text{cm}^2$)	α_-	α_+
4:4	0	-0.63	0.63	23.30	24.85	24.85	-0.82	-0.82
4:3	-6	-0.73	0.83	22.46	24.40	26.42	-0.82	-1.04
4:2	-12	-0.83	1.19	21.60	23.80	29.39	-0.82	-1.32

Table 1. List of critical values and scaling parameters for differential capacitance curves in Fig. 5a.

Figure 5 indicates that the impact of smaller anions on capacitance becomes more significant with an increasingly positive potential, as also shown by a more prominent deviation of $\sigma_0(\psi_0)$ there. It is also apparent that the shape of capacitance curve is strongly influenced by the the size of counterion, whereas the effect of coion size seems to be limited. In general, smaller ions have a larger packing density and screen electrostatic potential more effectively. For smaller anions, these two factors cause a positive shift in $\psi_0^{\text{max+}}$ and, to a lesser extent, a negative shift in $\psi_0^{\text{max-}}$. The positive shift is needed to accommodate the increasing number of anions required to saturate the Helmholtz layer, whereas the negative shift would counter the increase in screening effect of anions at the interface. A slightly negative pzc found for smaller anions is a result of the size mismatch between anion and cation, which leads to a population imbalance of ions near the surface. At zero surface charge (pzc), this imbalance results in a slightly non-zero (negative) excess charge in the Helmholtz layer, which is then overcompensated by opposite charges in subsequent layers. Besides causing the shift in critical potentials, less bulky anions raise the capacitance value at $\psi_0 > 0.63$ V and lower it in -0.83 V $< \psi_0 < 0.63$ V. The former occurs due to the formation of more compact alternate layers by smaller anions, as illustrated in Fig. 6a; the latter is a result of less polarized alternate layers, as the screening effect of smaller anions dampens the potential field more effectively. To illustrate the last point, the mole fraction profile of ions at this region ($\psi_0 = -0.6$ V) is shown in Fig. 6b. The changes in capacitance described here are in a good agreement with those from spectroscopic study of RTILs composed of imidazolium-based cations and Cl or BF₄ anions on glassy carbon, gold, or mercury electrodes.(Alam et al., 2007; 2008; Lockett et al., 2008)

The scaling of differential capacitance in RTILs with applied potential at both potential wings is a good indication of the extent of the compression of ions due to a high electrostatic field (electrostriction) in the EDL. For the case of $n_A : n_B = 4:4$, the scale is identical in the first non-linear regime ($\psi_0 < \psi_0^{\text{max-}}$) and the second non-linear regime ($\psi_0 > \psi_0^{\text{max+}}$), which is $C \propto |\psi_0|^{-0.82}$. For asymmetric capacitance curves, this scale persists in the first non-linear regime and becoming more pronounced in the second regime, in which the scaling is $C \propto |\psi_0|^{-1.04}$ for $n_A : n_B = 4:3$, and $C \propto |\psi_0|^{-1.32}$ for $n_A : n_B = 4:2$. Each scaling exponent corresponds to the change in thickness of alternate layers with electrostatic potential since the capacitance in the non-linear regime is mainly determined by the size of these layers. In principle, less bulky anions are geometrically more susceptible to variation in potential field by forming thicker (thinner) alternate layers at a more (less) positive applied potential. This

Fig. 6. Profile of the mole fraction (x) of cation and anion at the interface with different ratios of $n_A:n_B$ at $\psi_0 = 3$ V (a), and $\psi_0 = -0.6$ V (b).

explains a more rapid decay of the capacitance in the second non-linear regime for smaller anions. It is interesting to note that all scaling exponents obtained here are considerably less than -0.5 , which is the value predicted analytically based on the Poisson-Fermi distribution of spherical ions at a charged interface. (Kornyshev, 2007) This discrepancy is originated from different underlying assumptions in the analytical and SCMFT model. The analytical model incorporated the excluded volume by introducing a fixed lattice saturation parameter into the Boltzmann distribution of ions. In SCMFT, the lattice saturation parameter would not be homogeneous throughout the system since the ions are modelled as flexible chain molecules and their compression or relaxation within the EDL would depend on the local electrostatic potential field. This makes the EDL structure more responsive to the applied potential, which results in a more rapid decay of $C(\psi_0)$ than analytically predicted.

3.2 Effect of specific adsorption

Asymmetric capacitance curves in RTILs do not only occur when the corresponding ions have different size. They also occur for same-size ions with different specific affinity towards the electrode's surface. In aqueous electrolytes, specific adsorption is strongly related to the solvation shell of ions. A steric hindrance provided by a thick solvation shell prevents the ions from forming chemical bonds with the surface. For ions with thin-enough solvation shells, the solvent molecules would be removed from the surface to accommodate adsorption of more ions. This eventually leads to a redistribution of local charges on the surface, changes the surface dipole, and induces a partial charge transfer. (Lipowski et al., 1998; Lorenz & Salie, 1977; Magnussen, 2002) In the absence of any solvation shells surrounding RTILs, the specific adsorption of ions would arguably occur more strongly than in aqueous electrolytes. (Aliaga & Baldelli, 2006; Gale & Osteryoung, 1980) An example of specific adsorption in pure RTILs has been reported for 1-butyl-3-methylimidazolium dicyanamide RTIL on Pt-electrode. (Aliaga & Baldelli, 2006)

To study the effect of specific adsorption to the capacitance in RTILs, the affinity of anion towards the electrode's surface is systematically varied, while the size of the cation and anion is kept the same at $n_A : n_B = 4:4$. Three different sets of interaction parameters used here are $\chi_{BS} = \chi_{NS} = 0, -1$, and -2 . The more negative interaction parameter indicates a stronger specific affinity of anion towards the surface. The values of interaction parameter used here are within the typical limit of adsorption energy due to specific interactions, which

is in the order of few $k_B T$ for each adsorbed ion.(Lamperski, 1997; Lyklema, 1995; Nikitas, 1994; Parsons, 1955)

Fig. 7. (a) The differential capacitance curves of the modelled RTIL with $n_A:n_B = 4:4$ and $\chi_{BS} = \chi_{NS} = 0, -1,$ and -2 . (b) Similar curves with $\chi_{AS} = \chi_{PS} = 0, -1,$ and -2 . In both cases, the impact of specific adsorption is limited in the ψ_0 -zone marked by the arrow. It is apparent that the curve is asymmetric with respect to the pzc when the specific adsorption is present.

The differential capacitance curves of the aforementioned system are plotted in Fig. 7a. For comparison, a series of differential capacitance curves for the case of specific adsorption of cation is shown in Fig. 7b. These curves are understandably the mirror image of those obtained when the specific adsorption of anion is present. The critical values for the capacitance curves in Fig. 7a are listed in Table 2. It appears that a stronger specific adsorption of anion increases the capacitance value at $-1.2\text{ V} < \psi_0 < -0.3\text{ V}$ and decreases it at $-0.3\text{ V} < \psi_0 < 1.2\text{ V}$. The trend is reversed when the specific adsorption of cation is stronger (cf. Fig. 7b). The physical interpretation of these trends is that the amount of energy to bring one counterion from the bulk to the surface would be either reduced by the presence of specifically adsorbed coion, or increased when some counterion is already specifically adsorbed on the surface.

$\chi_{BS} = \chi_{NS}$	pzc (mV)	$\psi_0^{\text{max-}}$ (V)	$\psi_0^{\text{max+}}$ (V)	C_{pzc} ($\mu\text{F}/\text{cm}^2$)	$C_{\text{max-}}$ ($\mu\text{F}/\text{cm}^2$)	$C_{\text{max+}}$ ($\mu\text{F}/\text{cm}^2$)
0	0	-0.63	0.63	23.30	24.85	24.85
-1	-52	-0.66	0.61	22.27	26.45	23.67
-2	-95	-0.77	0.60	20.76	27.86	23.03

Table 2. List of critical values for differential capacitance curves in Fig. 7a.

The impact of specific adsorption is typically confined within a limited range of applied potential from the pzc.(Graves, 1970) This ψ_0 -zone is located in $-1.2\text{ V} < \psi_0 < 1.2\text{ V}$ for capacitance curves depicted in Fig. 7. As discussed above, specifically adsorbed ions tend to increase the gradient of $C(\psi_0)$ in the ψ_0 -zone. Such a steep capacitance curve is typically caused by partial charge transfers at a non-ideally polarized surface, which can be induced by specifically adsorbed ions.(Lipowski et al., 1998; Lorenz & Salie, 1977; Magnussen, 2002; Parsons, 1981) Beyond the ψ_0 -zone, the long-range electrostatic interaction overcomes the short-range effect of specific adsorption to diminish the amount of adsorbed anion on the

Fig. 8. Plot of the volume fraction of anion on the electrode’s surface (φ_{anion}) as a function of applied potential. There is a significant amount of anion on the electrode’s surface even at negative potentials due to the specific adsorption.

surface (φ_{anion}) at negative potential, as shown in Fig. 8. There are two additional trends observed by increasing the specific affinity of anion. Firstly, the φ_{anion} curve shifts to the left, indicating an increasing presence of anion on a negatively charged surface. Secondly, the pzc and both saturation limits (ψ_0^{max-} and ψ_0^{max+}) shift to more negative values since, in principle, a more negative surface is needed to counter the increasing amount of specifically adsorbed anion.

Fig. 9. Plot of the pzc as a function of the strength of specific adsorption of ion. For $\chi_{BS} = \chi_{NS} < 0$, the anion is adsorbed specifically to the surface, whereas for $\chi_{BS} = \chi_{NS} > 0$, the cation is specifically adsorbed.

The pzc is a robust parameter to detect the existence of specific adsorption in RTILs. The shift of pzc due to specific adsorption is relatively larger than that for unequal ion-size (cf. Tables 1 and 2). The relationship between the pzc and the strength of specific adsorption is shown in Fig. 9. The pzc varies steadily in the α -zone ($|\chi_{BS}| = |\chi_{NS}| < 6$) and goes to asymptotic values at the limit of extreme adsorption in the β -zone ($|\chi_{BS}| = |\chi_{NS}| > 6$). The gradient of the pzc curve in the α -zone is $\sim 2k_B T$ per ion for each unit of interaction parameter ($\chi_{BS} = \chi_{NS}$). In the β -zone, the gradient is close to zero, indicating the saturation of Helmholtz layer by specifically adsorbed ions.

4. Concluding remarks

The interfacial structure and capacitance in RTILs are studied by the SCMFT. Each ion is modelled as a tetramer composed of polar and apolar segments. The results show that the alternating layer of ions is formed at charged interfaces and the corresponding capacitance curve has a camel-shaped feature. The latter is caused by a combination of the excluded volume and ion polarizability effects in the EDL. The introduction of unequal ion-size leads to asymmetric capacitance curves. The shape of these curves is strongly determined by the size of counterion and only weakly influenced by coion size. In general, smaller ions have a higher packing density and screen the electrostatic potential more effectively. These two factors cause a shift in critical values of the capacitance curves. The presence of a specific affinity of ions towards the electrode's surface also leads to asymmetric capacitance curves. The impact occurs only within a limited range of applied potential from the pzc. Besides changing the capacitance values, specifically adsorbed ions shift the pzc and both saturation limits of the capacitance curves to one direction, depending on the type of their charge and the strength of specific adsorption.

The change in the pzc can be used as a qualitative tool to predict, e.g., the type of RTIL-metal species specifically adsorbed on the electrode's surface during metal electrodeposition, provided that each species has a distinct size but similar affinity towards the surface. The trends in capacitance curve and pzc presented in this study are generally useful to assist in the choice of RTILs for specific electrochemical applications, and in the design of new RTILs with tailored electrochemical properties.

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