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# Procedure to Prepare and Model Speed Data Considering the Traffic Infrastructure, as Part of a Cyber-Physical System 

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#### Abstract

This chapter investigates the relationship between traffic control infrastructure (traffic lights and speed bumps) and the vehicles' travel speeds, for certain hours and days of the week. The authors propose the following procedures: (1) street segmentation, (2) clustering and categorization of speed data, (3) histograms' comparison analysis, (4) outlier detection, (5) modeling, and (6) delivering info to the users. Comparing speed histograms, segments with matching infrastructure presented similarities, regardless of the day of the week. Two techniques to model data were employed: polynomial regression and multinomial logistic regression. The algorithms to predict the travel speed category were also developed. The first technique yields on average $91.3 \%$ of data categorized correctly, and the second gets $90.09 \%$. The traffic lights and speed bumps, located on the street segments under consideration, were identified as variables causing different travel speeds. The procedure allows to incorporate more traffic elements and can also be applied to other geographical locations.


Keywords: cyber-physical system, speed bumps, street segments, traffic lights, travel speed

## 1. Introduction

Traffic conditions have a profound effect on population's quality life. The TomTom traffic index states that in 2017, Mexico City had a travel delay of 66\% when compared with normal times of uncongested traffic, placing it as the first in the world rank. The wasted time per day was 59 min , or 227 h per year, with delays in the morning and evening peaks of about $100 \%$. Of the 23 million private cars in Mexico, $72 \%$ correspond to metropolitan areas [1]. As a result, those areas are a suitable choice to analyze traffic behavior. In 2010, with a population of 20,116,842 and 0.3 cars per habitant (about 6,035,052 cars), the Mexico City Valley is the most crowded of the country. The number of operating vehicles in a city reduces the average traveling speed and increases pollution [2,3] and the number of car accidents [4, 5]. The zone under study in this work is located between Mexico City and

Toluca, a region that is part of the Mexico City megalopolis, which makes the area a suitable candidate for analyzing traffic conditions. In this research we developed a procedure to analyze speed tendencies (by comparing histograms) and prepare (set clusters and remove anomalies) and model speed data to be used in an application example: speed prediction. The procedure answers the following question: what is the pathway to generate new information when speed data is available?

Recently, there has been a great effort in studying and analyzing traffic data from different world locations. Travel speed is one way to measure traffic conditions, as is travel time. In [6], the travel time distribution for different kinds of roads is estimated for Beijing. The time intervals to analyze data were set to 15 min , and it was concluded that the best-fitting distribution depends on the congestion level and that the average travel time of all road segments (for all days) can be estimated with acceptable precision using the normal distribution (compared with the log-normal, gamma and Weibull). In [7], travel time prediction is pursued. The variables considered were flow, concentration, and higher order auto-regression, concluding that local linear regression is preferable than global modeling. Characterization of the daily temporal variation of congestion is presented in [8], where a fitted model and live data are combined in a ten-parameter exponential smoothing equation. With the purpose of analyzing historical traffic data, a query processing method with timeline information is proposed in [9], along with an analysis of the congestion dependency along roads. The work presented in [10] estimates the average link speed with vehicles equipped with GPS, and therefore the quantity of equipped vehicles required for estimating the speed was established.

Using traffic data to make predictions is a current challenge, as Google maps traffic and Waze are doing. The purpose in [11] is to use information from Bing Maps to analyze, visualize, and predict traffic jams in Chicago. In addition, a prediction model to correct flow intensities with logistic regression was proposed, where the independent variables were day, hour, street number, and number of pixels (red, yellow, and green). In this work, a tool was developed to extract the roads' traffic intensity from a GIS map service, where colors represent flow intensity: red as congested, green not congested, and yellow in between. In [12], the properties of a community-driven mapping service (Waze) are characterized. Additionally, the authors discuss the use of traffic data to identify traffic accidents and potholes. In [13], a four-phase traffic approach is proposed: (1) data collection and representation, (2) traffic prediction, (3) vehicle selection for re-routing, and (4) alternative route assignment. In our work, we focus our contribution in the first two phases.

The traffic infrastructure elements (such as traffic lights, speed bumps, potholes) involved in driving situations influence driver's behavior, which in turn affects speed and number of accidents. The intention in [14] is the development of statistical models to predict accidents. These models correlate highway characteristics with traffic accidents. The variables considered were classified in groups: section identifiers, cross section related, location, traffic related (e.g., the percentage of trucks on a highway section), alignment, horizontal curvature, and accidents. The regression methods used were Poisson and negative binomial. The statistically significant variables were number of lanes, horizontal curvature, speed limit, tangent length, section length, average annual daily traffic, and peak hour. In addition, accidents are predicted with equations that consider roadway elements such as average daily traffic, commercial and residential units, intersections, speed limits, lane width, and number of lanes.

The work presented in [15] classifies traffic control elements (infrastructure) into three groups according to their effect on accidents. In Group 1 are those elements that reduce the number of accidents, such as speed limit signs,
speed-reducing devices, signalized pedestrian crossings, urban play streets, pedestrian streets, traffic-calming areas, traffic signals at intersections, bus lines and bus stops, parking control, and access control. Group 2 has no statistical effect on accidents: road markings, one-way streets, reversible lanes, traffic control for pedestrians and cyclists, priority control, and yield signs at intersections. Group 3 increases accidents: right turn on red, pedestrian crossing without signs, blinking traffic light, and increasing speed limits. According to [16], the presence of traffic control elements with the purpose to reduce speed or simplify the road users' tasks (e.g., traffic signs) tends to reduce accidents. An obvious consequence of the presence of speed-reducing devices (humps, rumble strips, narrow road width, bollards) is the increase of travel time [17] and the decrease of the average travel speed. One of the conclusions in [15] is that the traffic control elements that reduce accidents also reduce mobility.

Traffic elements such as signals and traffic lights are important in human driving decisions. The work presented in [18] intends to determine the relevance of the static road elements in driving situations using Markov logic networks (MLNs). The information considered to determine the relevance of speed limits and supplementary signs were the position in relation to lanes, vehicle type, date, time, and weather. Then, with first-order logic rules, the relevance of each was inferred. To determine the relevance of traffic lights, the following variables were considered: navigation system, environment perception, spatial relations, and the traffic light state.

The speed changes in the presence of speed bumps were analyzed in [19]. The speed limit on the streets under study is $50 \mathrm{~km} / \mathrm{h}$. The speed results measured at the bump location are as follows: about $30 \%$ of the cases show an 85 th percentile speed higher than the posted limit speed, $26 \%$ lie in the range $45-50 \mathrm{~m} \mathrm{~km} / \mathrm{h}$, and the rest is under $45 \mathrm{~km} / \mathrm{h}$. The 85 th percentile speed (measured after $20-25 \mathrm{~m}$ of the bumps' location, at the crosswalk area) tends to increase in $50 \%$ of the tested sites, similar result for the 50th percentile case ( $45 \%$ ). Nevertheless, for both cases the speed change was not significant, according to the statistical analysis. Another result was obtained comparing the speed at bumps and 100 m away: in most sites, the 85th percentile speed decreases in the range of $1-18 \%$ (with respect to the zone without bumps). The statistical analysis concludes for both percentiles that speed values do not change significantly.

The use of cyber-physical system in traffic is a current topic in the literature. In [20], a simulated vehicular cyber-physical system (VCPS) is designed for delivering warnings to the driver and to avoid accidents. With this end, the predicted vehicle motion/location, the driver behavior and the road geometry were considered. Then, the short-term motion of the objective vehicle and the surrounding vehicles are predicted. With the objective vehicle location and the traveled distance among vehicles, the collision risk is estimated, and the driver is notified. In [21], a perceptual Control Architecture of Cyber-Physical Systems (CPSs) is proposed, taking as example a traffic incident management system. The intelligent behavior of this is characterized by the physical-reflex space and cyber-virtual space. In the physicalreflex space, the sensing actuation of the objective scenario is constructed on four levels of traffic infrastructure. In the cyber-virtual space, the decisions (through Bayesian reasoning network) are defined according to three levels: principles, interrelated factors, and situation assessment. In [22] the potential participation of smartphones (equipped with GPS) is discussed to build a traffic information system (to inform the entire transportation network) that is part of the cyber-physical infrastructure system. In [23] a cloud-based cyber-physical system is presented, with the end to find fast routes for the users. The system is presented in four steps: (1) the GPS on taxis are used as mobile sensors to measure the traffic status in the
physical world; (2) the info generated by the taxis is sent to the cloud (cyber world) and mined, and then knowledge is acquired about the taxis' preferred directions and traffic patterns on the roads; (3) the knowledge in the cloud is sent to the users with the Internet; and (4) the recommendations for a specific user are improved using its driving behavior and preferred routes. In [24], a short-term traffic prediction model (combining fuzzy theory with Markov progress) is presented, which is part of a vehicular cyber-physical system; the prediction results are expressed in terms of traffic flow and speed. A proper discussion about the definition of a cyberphysical system, and its relationship with transportation, is in [25].

From a cyber-physical system point of view, in the procedure presented in this work, the cyber part corresponds to the elements in charge to acquire and mine data for generating knowledge and the process to communicate that Intel to the users. The user (a biological entity) and intelligent devices (e.g., the user smartphone, the vehicle computer) reacting in response of the knowledge correspond to the physical part.

The aim of the present work is to introduce a method for analyzing speed data measured on streets where the traffic infrastructure is assumed to be the cause of low speeds. Then, we develop models and algorithms that, working with our data, allow to make predictions. The procedure presented in this work is summarized in the following steps:

- Street segmentation is performed considering traffic control elements (speed bumps and traffic lights).
- Clustering speed data, validated with the silhouette metric.
- With the Chi-Square distance $\left(\chi^{2}\right)$, the travel speed histograms of weekdays are compared and also the histograms of segments.
- Mahalanobis distance is used to detect outliers.
- Two techniques (polynomial and logistic regression) were used to develop the models that describe speed data. An algorithm for each modeling technique was developed to predict travel speed.
- Communicate the generated knowledge to the users.

This chapter is organized as follows: Section 1 Introduction; Section 2 Method, which includes theoretical frame (data, clusters, histograms, outliers) and procedure (street segmentation, clustering, comparative analysis of histograms, outlier detection, mathematical models, connecting Intel with users); Section 3 Results (with discussion); and Section 4 Conclusions (with future work).

## 2. Method

### 2.1 Theoretical frame

### 2.1.1 Data

The zone under study is comprised of two streets located in Lerma de Villada, Mexico: Av. Miguel Hidalgo and Av. Reolin Barejon. Data was obtained using the Google Maps Directions API. The time for a vehicle to traverse each segment was
recorded every 15 min , after [6]. We found this time interval to be highly efficient for incorporating relevant data while ignoring redundant information. In this way, the average travel speed on each segment was measured. Three weeks ( $w_{1}, w_{2}$, and $w_{3}$ ) of data were considered: $w_{1}$ from Dec 27, 2016 to Jan 03, 2017; $w_{2}$ from Jan 03, 2017 to Jan 10, 2017; and $w_{3}$ from Jan 20, 2017 to Jan 27, 2017. The time interval to acquire data was from $6 \mathrm{a} . \mathrm{m}$. to $11: 59 \mathrm{p} . \mathrm{m}$. (an interval of 18 h per day) and only in weekdays, i.e., between Monday and Friday.

### 2.1.2 Clusters

The $k$-means technique [26] was selected (because it is easy to implement and is commonly used in distinct traffic problems [27-29]) to cluster the speed data of any of the 3 weeks; since these are close in time, it is expected a similar travel speed from 1 week to another, and then we select $w_{1}$. In simple terms, the $k$-means technique consists in calculating the centroid of each cluster as the mean of the data in the corresponding cluster and is recalculated until convergence.

We apply the $k$-means technique selecting a number of clusters in the range 3-6; for each case we calculate the silhouette score [30], given in Eq. (1), where $a(i)$ is the average distance from $i$ with the data in the same cluster, $b(i)$ is the minimum average distance from $i$ with the data of each other's cluster, and $i$ is the data index. The silhouette score is in the range -1 to +1 ; a value close to 1 indicates that the speed data is well matched in the selected clusters, while a value close to -1 indicates the opposite situation:

$$
\begin{equation*}
s s(i)=\frac{b(i)-a(i)}{\max \{a(i), b(i)\}} \tag{1}
\end{equation*}
$$

### 2.1.3 Histograms

Analyzing the speed frequency, by comparing speed histograms of certain locations (special selection) and certain time (temporal selection), we expected to find spatial and temporal relationship about the weekdays when the speed is similar (dissimilar) and the segments where the speed is similar (dissimilar).

The metric employed to compare a pair of histograms is the Chi-Square ( $\chi^{2}$ ) histogram distance [31], given in Eq. (2), where P and $Q$ are the histograms to be compared and $P_{i}$ and $Q_{i}$ contain the speed frequency of the $i$ bin ( $i$ is the bin index, the selected bin width is 1 ):

$$
\begin{equation*}
\chi^{2}(\mathrm{P}, \mathrm{Q})=\frac{1}{2} \sum_{i} \frac{\left(P_{i}-Q_{i}\right)^{2}}{\left(P_{i}+Q_{i}\right)} \tag{2}
\end{equation*}
$$

This metric has the advantage of reducing the importance of the result when bins with large count are compared, as in many natural histograms, the difference of bins with high values is less important [31]. If the metric gets a 0 result, then there is no difference between the compared histograms; as the result value becomes larger, the difference in terms of the speed frequency also becomes higher.

### 2.1.4 Outliers

We filtered the speed data using the Mahalanobis distance (MD) [32] to detect outliers, i.e., atypical speed not belonging to normal driving behavior, since we are not interested in including this data for modeling. The MD is presented in Eq. (3),
where $x_{i}$ is a vector containing the time and speed, $\bar{x}$ is a vector with the means, and $C_{x}^{-1}$ is the covariance matrix:

$$
\begin{equation*}
M D_{i}=\sqrt{\left(x_{i}-\bar{x}\right)^{T} C_{x}^{-1}\left(x_{i}-\bar{x}\right)} \tag{3}
\end{equation*}
$$

### 2.2 Procedure

### 2.2.1 Street segmentation

The avenues under study were divided into segments: each segment is denoted $s_{k}$, with $k$ as the segment index. On each segment, we have number of speed bumps $c_{1}$, number of traffic lights $c_{2}$, and landmarks $c_{3}$. A segment's length $l$ is set to approximately 500 m , and then on each segment there are specific traffic elements: $s_{k}=\left\{c_{1}, c_{2}, c_{3}, l\right\}$, as shown in Table 1.

### 2.2.2 Clustering

The silhouette score, considering three clusters, is better evaluated, with $s s=0.7360$. For four, five, and six clusters, we calculated a $s s=0.7331, s s=0.7194$, and $s s=0.7105$, respectively. As we were interested in communicating in a simple way the speed category at which is possible to travel, three options (as slow, medium, and normal) seem adequate. A similar approach in Google Maps (traffic option), where the speed is represented considering four options, from fast to slow.

The resultant average speed (in $\mathrm{km} / \mathrm{h}$ ) range of each cluster (or category) is category 1 (5.4112-18.1455), category 2 (18.1455-23.4234), and category 3 (23.4234-36.0750). For $w_{2}$ and $w_{3}$, values smaller than 5.4112 fall into category 1, and those larger than 36.0750 fall into category 3.

The percentage of a segment's speed data (from $w_{1}$ ) in a cluster is shown in Table 2. It is interesting to note that for all segments, there is a specific cluster that

|  | $c_{1}$ |  | $c_{3}$ | $l(\mathrm{~m})$ | GPS start coordinate | GPS end coordinate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s_{0}$ | 2 | 0 | None | 501 | $\begin{gathered} 19.284512 \\ -99.500927 \end{gathered}$ | $\begin{gathered} 19.285725 \\ -99.505498 \end{gathered}$ |
| $s_{1}$ | 2 | 0 | School, museum, gas station, government offices | 500 | $\begin{gathered} \text { 19.285725, } \\ -99.505498 \end{gathered}$ | $\begin{aligned} & 19.286330 \\ & -99.510221 \end{aligned}$ |
| $s_{2}$ | 0 | 1 | Banks, center square, school, fast-food restaurants | 500 | $\begin{aligned} & \text { 19.286330, } \\ & -99.510221 \end{aligned}$ | $\begin{gathered} \text { 19.286711, } \\ -99.514964 \end{gathered}$ |
| $s_{3}$ | 3 | 2 | Cultural center, hospital, school offices, kindergarten | 501 | $\begin{gathered} \text { 19.286711, } \\ -99.514964 \end{gathered}$ | $\begin{gathered} 19.286477 \\ -99.519630 \end{gathered}$ |
| $s_{4}$ | 3 | 0 | Telecom company offices, shopping mail | 499 | $\begin{gathered} \text { 19.286477, } \\ -99.519630 \end{gathered}$ | $\begin{gathered} 19.285784 \\ -99.514944 \end{gathered}$ |
| $s_{5}$ | 2 | 1 | Hospital, government offices, cultural forum | 500 | $\begin{gathered} \text { 19.285784 } \\ -99.514944 \end{gathered}$ | $\begin{gathered} 19.284943 \\ -99.510282 \end{gathered}$ |
| $s_{6}$ | 4 | 1 | School, supermarket, hospital | 500 | $\begin{aligned} & \text { 19.284943, } \\ & -99.510282 \end{aligned}$ | $\begin{aligned} & 19.284500 \\ & -99.505561 \end{aligned}$ |
| $s_{7}$ | 2 | 0 | None | 481 | $\begin{aligned} & \text { 19.284500, } \\ & -99.505561 \end{aligned}$ | $\begin{aligned} & 19.284403 \\ & -99.500993 \end{aligned}$ |

Table 1.
Segments' characteristics.

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| Segment | Cluster 1 (\%) | Cluster 2 (\%) | Cluster 3 (\%) |
| :---: | :---: | :---: | :---: |
| $s_{0}$ | 0.55 | 9.9 | 89.53 |
| $s_{1}$ | 11.84 | 80.71 | 7.43 |
| $s_{2}$ | 88.98 | 11.01 | 0 |
| $s_{3}$ | 93.66 | 6.33 | 0 |
| $s_{4}$ | 14.04 | 85.95 | 0 |
| $s_{5}$ | 79.61 | 20.38 | 0 |
| $s_{6}$ | 83.47 | 16.52 | 0 |
| $s_{7}$ | 4.13 | 3.85 | 92.01 |
| Table 2. |  |  |  |
| Percentage of speed data in a cluster. |  |  |  |

contains a high percentage of data (at least 79.61\%), which validates our clustering results.

### 2.2.3 Comparative analysis of histograms

First, we consider all segments as a single road, and then the histograms of the speed frequency (from 6 a.m. to 11:59 p.m.) happening on weekdays (in $w_{1}$ ) are compared in pairs, with the Chi-Square metric presented in Eq. (2). The results are shown in Table 3, starting with the lowest $\chi^{2}$ value, i.e., the similar histograms among weekdays, with $\mathrm{D}_{1}=$ Monday, $\mathrm{D}_{2}=$ Tuesday, and so on.

Second, the speed data throughout weekdays, but individual segments, was used to conform the histograms of the speed frequency happening on each segment for 5 days (the weekdays of $w_{1}$ ). These histograms were compared in pairs with the $\chi^{2}$. Table 4 shows the results starting with the lowest $\chi^{2}$. We found that if the compared segments share similar traffic elements, the speed frequency also is similar, and therefore a low $\chi^{2}$ is obtained.

| $\mathrm{D}_{2}-\mathrm{D}_{3}$ | $\mathrm{D}_{4}-\mathrm{D}_{5}$ | $\mathrm{D}_{3}-\mathrm{D}_{4}$ | $\mathrm{D}_{2}-\mathrm{D}_{4}$ | $\mathrm{D}_{1}-\mathrm{D}_{3}$ | $\mathrm{D}_{1}-\mathrm{D}_{2}$ | $\mathrm{D}_{1}-\mathrm{D}_{5}$ | $\mathrm{D}_{3}-\mathrm{D}_{5}$ | $\mathrm{D}_{2}-\mathrm{D}_{5}$ | $\mathrm{D}_{1}-\mathrm{D}_{4}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 7.77 | 10.758 | 10.936 | 11.139 | 14.097 | 15.168 | 16.347 | 16.827 | 17.609 | 20.653 |

Table 3.
Chi-Square distance between histograms with weekdays' data.

| $s_{2}-s_{5}$ | $s_{3}-s_{6}$ | $s_{5}-s_{6}$ | $s_{1}-s_{4}$ | $s_{2}-s_{6}$ | $s_{0}-s_{7}$ | $s_{2}-s_{3}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 20.37 | 34.17 | 39.01 | 45.57 | 46.05 | 73.75 | 88.591 |
| $s_{3}-s_{5}$ | $s_{4}-s_{5}$ | $s_{4}-s_{6}$ | $s_{1}-s_{5}$ | $s_{2}-s_{4}$ | $s_{3}-s_{4}$ | $s_{1}-s_{6}$ |
| 98.59 | 167.65 | 185.37 | 198.5 | 212.47 | 220.04 | 226.01 |
| $s_{1}-s_{2}$ | $s_{0}-s_{1}$ | $s_{1}-s_{3}$ | $s_{1}-s_{7}$ | $s_{0}-s_{4}$ | $s_{4}-s_{7}$ | $s_{6}-s_{7}$ |
| 238.39 | 269.15 | 271.36 | 303.87 | 321.89 | 337.16 | 337.43 |
| $s_{2}-s_{7}$ | $s_{5}-s_{7}$ | $s_{0}-s_{5}$ | $s_{0}-s_{6}$ | $s_{0}-s_{2}$ | $s_{3}-s_{7}$ | $s_{0}-s_{3}$ |
| 339.58 | 340.24 | 342.78 | 344.59 | 346.80 | 350.76 | 356.21 |

Table 4.
Chi-Square distance between histograms with segments data.


Figure 1.
Dissimilar histograms ( $s_{0}$ and $s_{3}$ ).


Figure 2.
Similar histograms ( $s_{2}$ and $s_{5}$ ).
Figure 1 shows the most dissimilar histograms, $s_{0}$ and $s_{3}$. Table 1 shows that $s_{0}$ has two speed bumps and no traffic lights, while $s_{3}$ has three speed bumps and two traffic lights; because the traffic lights on $s_{3}$, we will expect a lower speed in this segment, and this conclusion can be corroborated by looking at Figure 1.

Figure 2 shows the most similar histograms, $s_{2}$ and $s_{5}$. Segments $s_{2}$ and $s_{5}$ share the same number of traffic lights; however, there are two speed bumps in $s_{5}$ and 0 in $s_{2}$, then a slight superior speed is expected in $s_{2}$ (see Figure 2).

Tables 3 and 4 show that comparing histograms with the speed frequency of individual days (and all segments) are evaluated with a lower $\chi^{2}$ (the lower value is 7.77, the higher is 20.653) than the observed comparing histograms with the speed frequency of individual segments (and all days), where the lower value is 20.37 and the higher is 356.21 . Then, it appears that the travel speed is weakly influenced by the day of the week, since the traffic control elements of the whole road, from day to day, are the same. However, it seems that the segment strongly influences the travel speed, since the traffic control elements, which characterize each segment, modify the speed at which is possible to travel.

To corroborate the abovementioned statement, we use the speed frequency of $w_{2}$. Figure 3 shows the histograms of the speed frequency of each day (and all segments), where it can be observed the histograms' similarity. Figure 4 shows the histograms of the speed frequency of each segment (and all days), where it can be observed the histograms' dissimilarities.

### 2.2.4 Outlier detection

To put an example, the speed data of $s_{0}$ and $w_{1}$ is presented in Figure 5. We calculate the MD of this data (Figure 5), and then the probability density of the MD is presented in Figure 6, which has mean $=1.2331$ and standard deviation $S D=0.6894$. From Figure 6, a point with value MD $>\left(2^{*} S D+\right.$ mean $)=2.6119$ corresponds to a red point in Figure 5 and is considered an atypical point. The inequality value, i.e., ( $2^{*} \mathrm{SD}+\mathrm{mean}$ ), was established through trial and error.

The speed data from $w_{1}$ and $w_{2}$, for all segments, is filtered the same way as the example. The data used in the polynomial regression satisfy MD $<=\left(2^{*} \mathrm{SD}+\right.$ mean $)$ and in the logistic regression $\mathrm{MD}<=\left(3^{*} \mathrm{SD}+\right.$ mean $)$.


Figure 3.
Seed frequency of days.


Figure 4.
Speed frequency of segments.


Figure 5.
Time vs. speed: Data of $s_{0}$ and $w_{1}$.

### 2.2.5 Mathematical models

Polynomial: The data of each segment, with time as the independent variable and travel speed as the dependent variable, is modeled with a five-degree polynomial, enabling four-speed trend changes (the common requirement from the observations). The coefficients are calculated with the least-squares regression technique.


Figure 6.
Mahalanobis distance vs. probability density.
The following terminology is used to describe the model: the data size of all segments is $N=\sum_{k=0}^{k=7} N_{k}$, with $N_{k}$ referring the data size of the $k$ segment. The observed $i$ speed is denoted by $y(i)$, while time is $t(i)$. The speed model of segment $k$ and week $q$ is denoted by $M_{k}^{q}(i)$, with $k=\{0,1,2,3,4,5,6,7\}$ and $q=\{1,2\}$. The model is presented in Eq. (4), where coefficients $\varphi_{1} \ldots \varphi_{6}$ were calculated with speed data of the corresponding week $(q)$ and segment $(k)$ :

$$
\begin{equation*}
M_{k}^{q}(i)=\varphi_{1}+\varphi_{2} t(i)+\varphi_{3} t(i)^{2}+\varphi_{4} t(i)^{3}+\varphi_{5} t(i)^{4}+\varphi_{6} t(i)^{5} \tag{4}
\end{equation*}
$$

Multinomial logistic: The number of speed bumps and traffic lights (see
Table 1) are used to explain the speed. With multinomial logistic regression [33], we obtained the logistic model presented in Eq. (5), with $\psi=\{a, b\}$ :

$$
\begin{equation*}
E_{\psi}^{q}(i)=\psi_{1}+\psi_{2} v_{1}(i)+\psi_{3} v_{2}(i)+\psi_{4} v_{3}(i)+\psi_{5} v_{4}(i)+\psi_{6} v_{5}(i) \tag{5}
\end{equation*}
$$

The coefficients are denoted by $\psi_{1} \ldots \psi_{6}$, and $q=\{1,2\}$ refers again to the data from $w_{1}$ and $w_{2}$, respectively. The explanatory variables are $v_{1}=$ day weight, $v_{2}=$ number of speed bumps, $v_{3}=$ number of traffic lights, $v_{4}=$ segment weight, and $v_{5}=$ time. The weight of a specific day is calculated as the day average speed (of the speed measured from 6 a.m. to $11: 59$ p.m.) divided by the sum of the speed average of each weekday. A segment's weight is calculated as the segment's average speed (during weekdays) divided by the sum of the speed average of each segment.

In Eq. (5), $E_{a}^{q}$ calculates the relative risk of being in cluster 1 vs. cluster 3 (the reference), and $E_{b}^{q}$ calculates the same but for cluster $2 v$ s. cluster 3 . The conversion to probability is given in Eqs. (6)-(8), where $R_{j}^{q}$ is the probability belonging to the $j$ category, with $j=\{1,2,3\}$ :

$$
\begin{gather*}
R_{1}^{q}(i)=e^{E_{a}^{q}(i)} /\left(1+e^{E_{a}^{q}(i)}+e^{E_{b}^{q}(i)}\right)  \tag{6}\\
R_{2}^{q}(i)=e^{E_{b}^{q}(i)} /\left(1+e^{E_{a}^{q}(i)}+e^{E_{b}^{q}(i)}\right)  \tag{7}\\
R_{3}^{q}(i)=1-\left(R_{1}^{q}(i)+R_{2}^{q}(i)\right) \tag{8}
\end{gather*}
$$

### 2.2.6 Connecting Intel with users

With the developed procedure, knowledge is acquired about the speed at which is expected to travel on the segments under the study. The architecture design (and the implementation) to connect the Intel with the users is out of the scope in this work (planned as future work); nevertheless we present in this section the basic idea.

The algorithms developed (in Appendix A and Appendix B) were programmed in a regular computer; according the procedure presented, the data acquired (from the zone under study) is modeled, and the models are used in the algorithms to generate knowledge. The link between this knowledge and the users could be established through a cell phone app (via the Internet). When a driver is in the proximity of a street segment, the cell phone (with GPS) detects the current location and acquires information for the driver, as the number of bumps and traffic lights, and also the expected travel speed calculated with the proposed algorithms; this info is presented to the driver in a proper way to not distract him, and then the driver can decide the more convenient route. A more challenging design is to communicate the cell phone with the vehicle (assuming that an intelligent system is part of it and can control some functions) and, for example, when the vehicle is approaching a speed bump, it automatically decelerates (if the driver is not reacting adequately).

The program running in a computer, in charged to acquire and mine data for generating knowledge and to establish communication with the responsive elements, conforms the "cyber" part of the system. The elements reacting with intelligence to the Intel delivered, as the driver, the cell phone, and the vehicle, conform the "physical" part of the system. Finally, the cyber and physical parts combined conform a cyber-physical system.

## 3. Results

### 3.1 Polynomial regression model and Algorithm 1

The error between the modeled data, with Eq. (4), and the observed data, was calculated with the mean absolute error (MAE) (see Eq. (9)) [34]. Here, $n=N_{k}$, $y(i)$ and $\hat{y}(i)$ are the observed and modeled data, respectively. Table 5 shows the

|  | $M_{k}^{1}$ |  |  | $M_{k}^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| Segment | MAE (km/h) | SD (km/h) | MAE (km/h) | SD (km/h) |
| $s_{0}$ | 0.8269 | 0.6802 | 0.7895 | 0.6321 |
| $s_{1}$ | 1.0101 | 0.9630 | 1.1939 | 0.9916 |
| $s_{2}$ | 0.9523 | 0.7622 | 1.1754 | 1.0670 |
| $s_{3}$ | 0.6198 | 0.4628 | 0.6701 | 0.5917 |
| $s_{4}$ | 0.8435 | 0.6882 | 0.9765 | 0.7416 |
| $s_{5}$ | 0.8971 | 0.6826 | 0.9234 | 0.7408 |
| $s_{6}$ | 0.8438 | 0.7297 | 0.7737 | 0.6680 |
| $s_{7}$ | 0.9376 | 1.0762 | 0.7894 | 0.6653 |

Table 5.
MAE and SD.

MAE, and its standard deviation (SD), with the data of $w_{1}$ and $w_{2}$, and the respective modeled equations:

$$
\begin{equation*}
M A E=\frac{1}{n} \sum_{i=1}^{n}|y(i)-\hat{y}(i)| \tag{9}
\end{equation*}
$$

An algorithm (Appendix A, Algorithm 1) is designed to predict the speed of $w_{3}$ using the modeled equations ( $M_{k}^{1}$ and $M_{k}^{2}$ ) and historical data, i.e., the data available from $w_{3}$ before the current time. The error between the observed (from $w_{3}$ ) and predicted (with Algorithm 1) travel speeds is calculated with Eq. (9). The MAE, SD, and hits (percentage of data categorized correctly) for $w_{3}$, using Algorithm 1, are shown in Table 6.

Figure 7 shows, as example, the observed speed data (in black circles) of $w_{3}$ and segment $s_{0}$, the modeled data with $w_{1}$ (model $M_{0}^{1}$, in blue dots) and $w_{2}$ (model $M_{0}^{2}$, in green dots), and the estimated speed with Algorithm 1 (in red plus signs).

### 3.2 Multinomial logistic regression model and Algorithm 2

Algorithm 2 (see Appendix B) is used to predict the speed category of the observed data from $w_{3} . H_{1}(i)$ and $H_{2}(i)$ are two data sets obtained from $w_{1}$ and $w_{2}$, respectively. These sets save the associated category of the average speed in a time interval from $t(i)-0.5$ to $t(i)+0.5(0.5 \mathrm{~h}=30 \mathrm{~min})$ and centered on $t(i)$, of the day and segment under evaluation. $H_{3}(i)$ is the category speed of $w_{3}$ (which is only available for previous data, i.e., prior to ( $i$ ), with $i . . . N$ being the data index. The probability most likely to occur is $P_{q}(i)=\max \left\{R_{1}^{q}(i), R_{2}^{q}(i), R_{3}^{q}(i)\right\}=R_{x}^{q}(i)$ and the category is stored in $S_{q}(i)=x$, where subindex $q=\{1,2\}$ refers to the week. A threshold value, selected through trial and error, is used to discard the result in $S_{q}(i)$ if $P_{q}(i)<$ threshold. Algorithm 2 predicts the speed category for $w_{3}$, which is stored in $S_{3}(i)$. Choosing threshold $=0.9$ gives $90.09 \%$ of correct evaluations. This percentage is the summation of cases, where $S_{3}(i)$ was categorized correctly divided by the total data N .

Afterward, we attempted to predict the speed category of the observed speed in $w_{3}$ under the assumption that set $H_{2}(i)$ is composed only with the average speed of each segment, and not including $H_{1}$. The optimum result was found if threshold $=\sim 0.85$, with $85.62 \%$ of correct predictions. If the threshold value is reduced, the positive prediction decreases (because the model fails to predict accurately with that threshold value). Similarly, if the threshold is increased, it becomes more

| Segment | MAE (km/h) | SD (km/h) | Hits (\%) |
| :---: | :---: | :---: | :---: |
| $s_{0}$ | 0.7757 | 0.7142 | 92.4 |
| $s_{1}$ | 0.9353 | 1.0061 | 85.2 |
| $s_{2}$ | 0.8641 | 0.7537 | 89.5 |
| $s_{3}$ | 0.7749 | 0.7658 | 94.8 |
| $s_{4}$ | 1.0053 | 1.0903 | 85.2 |
| $s_{5}$ | 0.8051 | 0.7942 | 93.5 |
| $s_{6}$ | 0.6968 | 0.6639 | 96.5 |
| $s_{7}$ | 0.7994 | 0.9391 | 93.5 |

Table 6.
Algorithm 1 prediction results: MAE, SD, and hits.


Figure 7.
Time vs. speed: data of $s_{0}$ and $w_{3}$.
difficult to satisfy the condition $P_{q}(i) \geq$ threshold, and then the positive prediction also drops because now the set $H_{2}(i)$ (with the limitation mentioned before) contributes more. Table 7 shows the percentage of speed data categorized correctly with different threshold values.

### 3.3 Discussion

A series of steps are employed in a numerical example that, in combination, constitute a new method for speed prediction. The first step, street segmentation, divides an avenue in such a way that distributes different traffic elements on different segments. These elements are number of speed bumps, traffic lights, and landmarks, which in turn leads to different speed behavior on each segment. The second step, clustering, selects intervals which better fit the travel speed observed, resulting in three categories. Depending on the segment, most of the speed data (approximately at least 80\%) is within a specific cluster (category). For example, we infer that the speed behaviors in $s_{2}$ and $s_{5}$ are similar, since most of the speeds for both fall inside cluster 1 . Moreover, speed behaviors of $s_{0}$ and $s_{3}$ are dissimilar, since most of the speeds belong to different clusters ( 3 and 1, respectively). In the third step, comparative analysis of histograms, we corroborate that for each segment, the

| Threshold | Prediction (\%) |
| :--- | :---: |
| 0.75 | 81.69 |
| 0.80 | 83.10 |
| 0.85 | 85.62 |
| 0.90 | 84.24 |
| 0.95 | 83.97 |

Table 7.
Algorithm 2: threshold values and $w_{3}$ prediction results.
speed behavior is related to the traffic elements involved. It was observed that the speed histograms of two segments get a low Chi-Square distance if the segments share approximately the same number of speed bumps, traffic lights, and landmarks, independent of the day of the week. A high Chi-Square distance implies the opposite situation, i.e., segments with different number of traffic elements. The fourth step, outlier detection, removes atypical speed behavior, e.g., a vehicle circulating slower or faster than the usual. In step five, mathematical models, the models explain the speed. From steps 2 and 3, it is already known that on each segment, speed behaves according to the traffic elements involved, and hence the speed data of each segment is modeled independently with a polynomial model, with time as the independent variable. The multinomial logistic model uses as independent variables the number of speed bumps, traffic lights, the time, and two weights. The weights are calculated based on the average of the measured travel speeds considering segments and days. Finally, in step 6, connecting Intel with users, the drivers are properly informed about the travel speed expected on the surrounding segments, helping them to continuously adjust their route.

## 4. Conclusions

The procedure presented in this chapter proposes street segmentation; on each segment, there are traffic elements that we infer may be related with the observed speed frequency. By comparing speed histograms, we found that the speed frequency of all segments is similar among weekdays, and then the speed frequency of a specific segment is similar regarding the day. Considering the speed frequency of all weekdays, and individual segments, the segments with different traffic elements (speed bumps, traffic lights, and landmarks) yield dissimilar traveling speeds. From this observation, two techniques were considered for modeling speed: (1) polynomial regression, where the data of each segment is modeled independently, using time as the independent term, and (2) logistic regression, with several independent variables-number of speed bumps and traffic lights, time, and two weights (from the observed speeds on street segments and weekdays). The models were implemented in algorithms, which use the modeled and historical data. With the polynomial model and Algorithm 1, it was possible to categorize correctly the travel speed in the range from 85.2 to $96.5 \%$, depending on the segment. The multinomial logistic model and Algorithm 2 correctly predict the speed category in 90.09\% of the evaluated cases. With these results, we conclude that the proposed procedure is suitable to prepare and model speed data and then to predict the speed category at a low computer processing cost. The procedure is useful to establish the relationship between traffic infrastructure and travel speed.

### 4.1 Future work

We contemplate as future work the development of the architecture to communicate the expected travel speed (obtained with the proposed procedure) with the users, as well as convert this knowledge in suggestions and decision-making.

## Appendix A

In Algorithm 1, if $i \leq$ deep (line 3), the modeled speed of $w_{1}$ and $w_{2}$ contributes the same (each multiplied by 0.5 ). The case $i \geq$ deep +1 (line 6) enables the
estimation of $\bar{y}(i-1)$ and $\bar{y}(i)$ with known data from $w_{3}$. Variables $h_{1}$ and $h_{2}$ (see lines from 9 to 14) store the average of the absolute difference between historical and modeled data, from $w_{1}$ and $w_{2}$, respectively. $h_{3}$ (line 15) stores the absolute difference of the historical and estimated data, from $w_{3}$ and index $i-1$. The condition in line 16 verifies that the $y(i-3)$ to $y(i-1)$ speeds are nonempty, i.e., available. $h_{1} \ldots h_{3}$ are normalized and converted to weights, named $W_{1} \ldots W_{3}$. Because $h$ carries the error, a greater $h$ results in a smaller $W$, and so forth. In line 18, the predicted speed is calculated using the weights, the modeled speed with $w_{1}$ and $w_{2}$, and the estimation with previous data of $w_{3}$. If the condition in line 16 is not true, then in line 21 the speed prediction is calculated with the modeled data and new weights, without the $w_{3}$ data.

## Algorithm 1

Initial conditions: deep $=3$;

1. for $k=0$ to $k=7$
2.for $i=1$ to $i=N_{k}$
3.if $i \leq$ deep
2. $\hat{y}(i)=M_{k}^{1}(i) * 0.5+M_{k}^{2}(i) * 0.5$
5.end if
6.if $i \geq$ deep +1
3. $\bar{y}(i-1)=y(i-2)+(y(i-2)-y(i-3))$
$8 . \bar{y}(i)=y(i-1)+(y(i-1)-y(i-2))$
4. $h_{1}=0 ; h_{2}=0$;
10.for $j=1$ to $j=$ deep
5. $h_{1}=h_{1}+\left|y(i-j)-M_{k}^{1}(i-j)\right|$
6. $h_{2}=h_{2}+\left|y(i-j)-M_{k}^{2}(i-j)\right|$
13.end for
7. $h_{1}=h_{1} /$ deep $; h_{2}=h_{2} /$ deep
8. $h_{3}=|y(i-1)-\bar{y}(i-1)|$
16.if $y(i-1) \notin \varnothing \wedge y(i-2) \notin \varnothing \wedge y(i-3) \notin \varnothing$
9. $h_{1}=\frac{h_{1}}{h_{1}+h_{2}+h_{3}} ; h_{2}=\frac{h_{2}}{h_{1}+h_{2}+h_{3}} ; h_{3}=\frac{h_{3}}{h_{1}+h_{2}+h_{3}} ; W_{1}=\frac{1-h_{1}}{1-h_{1}+1-h_{2}+1-h_{3}} ;$
$W_{2}=\frac{1-h_{2}}{1-h_{1}+1-h_{2}+1-h_{3}} ; \quad W_{3}=\frac{1-h_{3}}{1-h_{1}+1-h_{2}+1-h_{3}}$
10. $\hat{y}(i)=M_{k}^{1}(i) * W_{1}+M_{k}^{2}(i) * W_{2}+\bar{y}(i) * W_{3}$
19.else
11. $h_{1}=\frac{h_{1}}{h_{1}+h_{2}} ; h_{2}=\frac{h_{2}}{h_{1}+h_{2}} ; W_{1}=1-h_{1} ; W_{2}=1-h_{2} ;$
12. $\hat{y}(i)=M_{k}^{1}(i) * W_{1}+M_{k}^{2}(i) * W_{2}$
22.end if
23.end if
24.end for
25.end for

## Appendix B

From Algorithm 2, in lines 3 to 10 it is compared the modeled and historical speed category (from $w_{1}$ and $w_{2}$ ), with the historical from $w_{3}$, to determine which is
the accurate. The number of hits of the model and the historical (for weeks 1 and 2) is stored in score with sub-index from 1 to 4, for the four cases. In line 12, if the probability $P_{2}(i)$ is greater or equal than the selected threshold and, if score $_{2} \geq$ score $_{1}$, then $S_{2}(i)$ is the predicted speed category. In line 14, if $P_{1}(i) \geq$ threshold and, if score $_{1} \geq$ score $_{2}$, then the predicted speed category is $S_{1}(i)$. If previous conditionals (line 12 and 14) are not evaluated to true, in lines from 16 to 18, the historical with the greater score, $H_{2}$ or $H_{1}$, is the selected to predict the speed category.

## Algorithm 2


threshold $\in[0.75,0.95]$;
1.for $i=1$ to $i=N$
2.if $i>1$
3.if $H_{3}(i-1)==S_{1}(i-1)$
4. score ${ }_{1}++$; end if
5.if $H_{3}(i-1)==S_{2}(i-1)$
6.score $2++$; end if
7. if $H_{3}(i-1)==H_{1}(i-1)$
8. score $3++$; end if
9. if $H_{3}(i-1)==H_{2}(i-1)$
10. score $_{4}++$; end if
11.end if
12.if $\left(P_{2}(i) \geq\right.$ threshold $\wedge \quad\left(\right.$ score $_{2} \geq$ score $\left._{1}\right)$
13. $S_{3}(i)=S_{2}(i)$; else
14. if $\left(P_{1}(i) \geq\right.$ threshold $\wedge \quad\left(\right.$ score $_{1} \geq$ score $\left._{2}\right)$
15. $S_{3}(i)=S_{1}(i)$; else
16.if score $_{4} \geq$ score $_{3}$
17. $S_{3}(i)=H_{2}(i)$; else
18. $S_{3}(i)=H_{1}(i)$; end if
19.end if
20.end if
21. end for

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## References

[1] ONU-Hábitat. Reporte Nacional de Movilidad Urbana en México 2014-2015. 2015
[2] Marr LC, Grogan LA, Wöhrnschimmel H, Molina LT, Molina MJ, Smith TJ, et al. Vehicle traffic as a source of particulate polycyclic aromatic hydrocarbon exposure in the Mexico city metropolitan area. Environmental Science \& Technology. 2004;38(9): 2584-2592
[3] Jiang M, Marr LC, Dunlea EJ, Herndon SC, Jayne JT, Kolb CE, et al. Vehicle fleet emissions of black carbon, polycyclic aromatic hydrocarbons, and other pollutants measured by a mobile laboratory in Mexico City. Atmospheric Chemistry and Physics. 2005;5(12): 3377-3387
[4] Híjar M, Vazquez-Vela E, ArreolaRisa C. Pedestrian traffic injuries in Mexico: A country update. Injury Control and Safety Promotion. 2003;10 (1-2):37-43
[5] Ramos A, Silva E, Aguirre A. Fatal car accidents in the metropolitan zone of Mexico City: A geographical and temporal perspective. Papeles de Poblacion. 2015;21(86):253-282
[6] Li R, Chai H, Tang J. Empirical study of travel time estimation and reliability. Mathematical Problems in Engineering. 2013;2013:1-9
[7] Rupnik J, Davies J, Fortuna B, Duke A, Clarke SS. Travel time prediction on highways. In: Computer and Information Technology; Ubiquitous Computing and Communications; Dependable, Autonomic and Secure Computing; Pervasive Intelligence and Computing (CIT/IUCC/DASC/PICOM), 2015 IEEE International Conference on. 2015. pp. 1435-1442
[8] Chacon S, Kornhauser AL. Analysis, Characterization, and Visualization of Freeway Traffic Data in Los Angeles. 2012
[9] Imawan A, Indikawati F, Kwon J, Rao P. Querying and extracting timeline information from road traffic sensor data. Sensors. 2016;16(9):1340
[10] Long Cheu R, Xie C, Lee D-H. Probe vehicle population and sample size for arterial speed estimation. ComputerAided Civil and Infrastructure Engineering. 2002;17(1):53-60
[11] Tostes AIJ, de LP Duarte-Figueiredo F, Assunção R, Salles J, Loureiro AAF. From data to knowledge: City-wide traffic flows analysis and prediction using Bing maps. In: Proceedings of the 2nd ACM SIGKDD International Workshop on Urban Computing. 2013. p. 12
[12] Silva TH, de Melo POSV, Viana AC, Almeida JM, Salles J, Loureiro AAF. Traffic condition is more than colored lines on a map: Characterization of Waze alerts. In: International Conference on Social Informatics. 2013. pp. 309-318
[13] Pan J, Popa IS, Zeitouni K, Borcea C. Proactive vehicular traffic rerouting for lower travel time. IEEE Transactions on Vehicular Technology. 2013;62(8): 3551-3568
[14] Milton J, Mannering F. The relationship among highway geometrics, traffic-related elements and motor-vehicle accident frequencies. Transportation. 1998;25(4):395-413
[15] Kinderyte-Poškiene J, Sokolovskij E. Traffic control elements influence on accidents, mobility and the environment. Transport. 2008;23(1): 55-58. Available from: http://www.tandf
online.com/doi/abs/10.3846/
1648-4142.2008.23.55-58
[16] Peden M, Scurfield R, Sleet D, Mohan D, Hyder AA, Jarawan E, et al. World Report on Road Traffic Injury Prevention. Geneva: World Health Organization; 2004
[17] Baum HM, Wells JK, Lund AK. Motor vehicle crash fatalities in the second year of 65 mph speed limits. Journal of Safety Research. 1990; 21(1):1-8
[18] Nienhüser D, Gumpp T, Zöllner JM. Relevance estimation of traffic elements using Markov logic networks. In: Intelligent Transportation Systems (ITSC), 2011 14th International IEEE Conference on. 2011. pp. 1659-1664
[19] Pau M, Angius S. Do speed bumps really decrease traffic speed? An Italian experience. Accident; Analysis and Prevention. 2001;33(5):585-597
[20] Wu C, Peng L, Huang Z, Zhong M, Chu D. A method of vehicle motion prediction and collision risk assessment with a simulated vehicular cyber physical system. Transportation Research Part C: Emerging Technologies. 2014;47:179-191
[21] Wang Y, Tan G, Wang Y, Yin Y. Perceptual control architecture for cyber-physical systems in traffic incident management. Journal of Systems Architecture. 2012;58(10): 398-411
[22] Work DB, Bayen AM. Impacts of the mobile internet on transportation cyberphysical systems: Traffic monitoring using smartphones. In: National Workshop for Research on High-Confidence Transportation CyberPhysical Systems: Automotive, Aviation, \& Rail. 2008. pp. 18-20
[23] Yuan J, Zheng Y, Xie X, Sun G. Driving with knowledge from the
physical world. In: Proceedings of the 17th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining. 2011. pp. 316-324
[24] Chen C, Liu X, Qiu T, Sangaiah AK. A short-term traffic prediction model in the vehicular cyber-physical systems. Future Generation Computer Systems. 2017. In press
[25] Jianjun S, Xu W, Jizhen G, Yangzhou C. The analysis of traffic control cyber-physical systems. Procedia - Social and Behavioral Sciences. 2013;96:2487-2496
[26] Jain AK. Data clustering: 50 years beyond K-means. Pattern Recognition Letters. 2010;31(8):651-666
[27] Montazeri-Gh M, Fotouhi A. Traffic condition recognition using the k-means clustering method. Scientia Iranica. 2011;18(4):930-937
[28] Fotouhi A, Montazeri-Gh M. Tehran driving cycle development using the k means clustering method. Scientia Iranica. 2013;20(2):286-293
[29] Saunier N, Sayed T. Clustering vehicle trajectories with hidden Markov models application to automated traffic safety analysis. In: The 2006 IEEE International Joint Conference on Neural Network Proceedings. 2006. pp. 4132-4138
[30] Rousseeuw PJ. Silhouettes: A graphical aid to the interpretation and validation of cluster analysis. Journal of Computational and Applied Mathematics. 1987;20:53-65
[31] Pele O, Werman M. The quadraticchi histogram distance family. In: Daniilidis K, Maragos P, Paragios N, editors. Computer Vision - ECCV 2010: 11th European Conference on Computer Vision, Heraklion, Crete, Greece, September 5-11, 2010, Proceedings, Part

Procedure to Prepare and Model Speed Data Considering the Traffic Infrastructure, as Part... DOI: http://dx.doi.org/10.5772/intechopen. 88280
II. Berlin, Heidelberg: Springer Berlin Heidelberg; 2010. pp. 749-762
[32] De Maesschalck R, Jouan-Rimbaud D, Massart DL. The Mahalanobis distance. Chemometrics and Intelligent Laboratory Systems. 2000;50(1):1-18
[33] Hutcheson G. The Multinomial Logistic Regression Model. Manchester: Sage Publications; 2009
[34] Willmott CJ, Matsuura K.
Advantages of the mean absolute error (MAE) over the root mean square error
(RMSE) in assessing average model performance. Climate Research. 2005; 30(1):79-82

