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## **Gas Well Testing**

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## Abstract

Modeling liquid flow for well test interpretation considers constant values of both density and compressibility within the range of dealt pressures. This assumption does not apply for gas flow case in which the gas compressibility factor is also included for a better mathematical representation. The gas flow equation is normally linearized to allow the liquid diffusivity solution to satisfy gas flow behavior. Depending upon the viscosity-compressibility product, three treatments are considered for the linearization: square of pressure squared, pseudopressure, or linear pressure. When wellbore storage conditions are insignificant, drawdown tests are best analyzed using the pseudopressure function. Besides, since the viscosity-compressibility product is highly sensitive in gas flow; then, pseudotime best captures the gas thermodynamics. Buildup pressure tests, for example, require linearization of both pseudotime and pseudopressure. The conventional straight-line method has been customarily used for well test interpretation. Its disadvantages are the accuracy in determining of the starting and ending of a given flow regime and the lack of verification. This is not the case of the Tiab's Direct Synthesis technique (TDS) which is indifferently applied to either drawdown or buildup tests and is based on features and intersection points found of the pressure and pressure derivative log-log plot.

**Keywords:** *TDS* technique, pseudotime, pseudopressure, rapid flow, viscosity, rate transient analysis, pressure transient analysis

## 1. Introduction

Contrary to liquids, a gas is highly compressible and much less viscous. In general, gas viscosity is about a 100 times lower than the least viscous crude oil. It is important, however, to try to provide the same mathematical treatment to oil and gas hydrocarbons, so interpretation methodologies can easily be applied in a more practical way. Then, the gas flow equation is normally linearized to allow the liquid diffusivity solution to satisfy the gas behavior when analyzing transient test data of gas reservoirs. Depending on the values of reservoir pressure, viscosity, and



© 2017 The Author(s). Licensee InTech. This chapter is distributed under the terms of the Creative Commons Attribution License (http://creativecommons.org/licenses/by/3.0), which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited. [cc] BY gas compressibility factor, the gas flow behavior can be treated as a function of either pressure to the second power or linear pressure with a region which does not correspond to any of these and it is better represented by a synthetic function call pseudopressure. Pseudopressure is a function that integrates pressure, density, and compressibility factor. The gas system's total compressibility highly depends on gas compressibility which for ideal gases changes inversely with the pressure. Then, another artificial function referred as pseudotime is included to further understand the transient behavior of gas flow in porous media. For instance, when wellbore storage conditions are insignificant, drawdown tests are best analyzed using the pseudopressure function. On the other hand, buildup pressure tests require linearization of both pseudotime and pseudopressure.

This chapter will be devoted to provide both fundamental of gas flow in porous media as well as interpretation of pressure and rate data in gas reservoirs. The use of the oil flow equations and interpretation techniques is carefully extended for gas flow so that reservoir permeability, skin factor, and reservoir area can be easily estimated from a gas pressure or gas rate test by using conventional analysis and characteristic points found on the pressure derivative plot (TDS technique). Conventional analysis-the oldest pressure transient test interpretation techniqueis based upon understanding the flow behavior in a given reservoir geometry, so the pressure versus time function is plotted in such way that a linear trend can be obtained. Both slope and intercept of such linear tendency are used to characterize the reservoir. Conventional analysis has two main drawbacks: (1) difficulty of finding a given flow regime and (2) absence of parameter verification. On the other hand, TDS technique-is strongly based on the log-log plot of pressure and pressure derivative versus time curves which provide the best way for flow regime identification; then, it uses the "fingerprints" or characteristic points found in such plot which are entered in practical and direct analytical equations to easily find reservoir parameters. Moreover, the same parameters can be obtained from different sources for verification purposes. Such is the case, for instance, of the reservoir area in elongated systems which can be estimated five times.

The chapter will include both interpretation techniques *TDS* and conventional in two cases: (1) infinite and (2) finite reservoirs. Channels or elongated systems in which reservoir hemilinear, parabolic or linear flow regimes developed once radial flow regime vanishes are reported in Refs [8, 13, 14]. This formation of linear flow regime normally occurs in fluvial deposits (channels), sand lens, parallel faulting, terrace faulting, and carbonate reefs. Then, such systems are worth of transient pressure analysis characterization. Latest researches on the determination of drainage area in constant-pressure-bounded systems using either conventional analysis or *TDS* technique are also reported by Escobar et al. [10].

It is convenient to mention some other important aspects concerning gas well testing which have appeared recently. The first case is the transient rate analysis in hydraulically fractured wells which was presented by [19] for both oil and gas wells. The traditional model for elliptical flow included the reservoir area as a variable. Handling the interpretation using *TDS* Technique may be little difficult for unexperienced interpreters. Therefore, [20] introduced a model excluding the reservoir drainage area and avoiding the necessity of developing pseudosteady-state regime. When a naturally fractured reservoir is subjected to hydraulic fracturing, the interpretation should be performed according to the presented by [21]. [35]

presented the pressure behavior of finite-conductivity fractured wells in gas composite systems. As far a horizontal wells, the recent works by [23] and [24] included off-centered wells for transient-rate or transient-pressure cases, respectively. [29] presented a study of production performance of horizontal wells when rapid flow conditions are given.

Practical exercises will provide in the chapter provide a better understanding and applicability of the interpretation techniques.

The purpose of this chapter is two folded: (1) to present the governing equation for gas flow used in well test interpretation and (2) to use both conventional and *TDS* Techniques as valuable tools for well test interpretation in both transient rate and transient pressure analysis. Some detailed examples will be given for demonstration purposes.

## 2. Transient pressure analysis

Transient pressure analysis is performed measuring the bottom-hole pressure while the flow rate is kept constant.

## 2.1. Fluid flow equations

The gas diffusivity equation in oil-field units is given by:

$$\frac{1}{r}\frac{\partial}{\partial r}\left(\frac{P}{\mu(P)Z(P)}r\frac{\partial P}{\partial r}\right) = \frac{\phi}{0.0002637}\frac{\partial}{\partial t}\left(\frac{P}{Z(P)}\right)$$
(1)

Which can be modified to respond for three-phase flow (oil, water, and gas):

$$\frac{1}{r}\frac{\partial}{\partial r}\left(r\frac{\partial P}{\partial r}\right) = \frac{\phi c_t}{0.0002637\lambda_t}\frac{\partial P}{\partial t}$$
(2)

where, the total compressibility,  $c_t$ , and total mobility,  $\lambda_t$ , are given by:

$$c_t \approx c_g s_g + c_o S_o + c_w S_w + c_f$$

$$\lambda_t = \frac{k_g}{\mu_g} + \frac{k_o}{\mu_o} + \frac{k_w}{\mu_w}$$
(3)
(4)

As can be inferred from Eq. (3), the total compressibility varies significantly when dealing with monophasic gas flow since the gas compressibility varies along with the pressure. Agarwal [1] introduced the pseudotime function to alleviate such problem. This function accounts for the time dependence of gas viscosity and total system compressibility:

$$t_a = \int_{t_{ref}}^{t} \frac{dt}{\mu(t)c_t(t)}$$
(5)

Pseudotime is better defined as a function of pressure as a new function given in hr psi/cp:

$$t_a(P) = \int_{P_{ref}}^{P} \frac{(dt/dP)}{\mu(P)c_t(P)} dP$$
(6)

Notice that  $\mu$  and  $c_t$  are now pressure-dependent properties.

As expressed by Eq. (1), viscosity and gas compressibility factor are strong functions of pressure; then, to account for gas flow behavior, Al-Hussainy et al. [2] introduced the pseudopressure function which basically includes the variation of gas viscosity and compressibility into a single function which is given by:

$$m(P) = 2 \int_{P_{ref}}^{P} \frac{P}{\mu(P)Z(P)} dP$$
(7)

After replacing Eqs. (6) and (7) into Eq. (1), it yields:

$$\frac{1}{r}\frac{\partial}{\partial r}\left(r\frac{\partial m(P)}{\partial r}\right) = \frac{\phi}{0.0002637k}\frac{\partial m(P)}{\partial t_a(P)} \tag{8}$$

Contrary to liquid well testing, rapid gas flow has a strong influence on well testing, [32]. As the flow rate increases, so does the skin factor, then:

$$s_a = s + Dq \tag{9}$$

Eq. (9) shows that the apparent skin factor is a function of the mechanical skin factor — which is assumed to be constant during the test — and the product of the flow rate with the turbulence factor or non-Darcy term. This implies that two flow test ought to be run at different flow rates to find mechanical skin factor and the turbulence factor from:

$$(s_a)_1 = s + Dq_1 \tag{10}$$

$$(s_a)_2 = s + Dq_2 \tag{11}$$

Solving the simultaneous equations:

$$D = \frac{(s_a)_1 - (s_a)_2}{q_1 - q_2} \tag{12}$$

$$s = (s_a)_1 - \frac{(s_a)_1 - (s_a)_2}{q_1 - q_2}q_1$$
(13)

where, the skin factors 1 and 2 are estimated from each pressure test. However, there is a need of estimating the turbulence factor by empirical correlations for buildup cases or when a single test exists. Then, the non-Darcy flow coefficient is defined by [26]:

$$D = 2.222 \times 10^{-15} \frac{\gamma_g kh\beta}{\mu_g r_w h_p^2} \tag{14}$$

The above equation is also applied to partially completed or partially penetrated wells.  $h_p$  is the length of the perforated interval. For fully perforated wells,  $h_p = h$ .

Parameter  $\beta$  is called turbulence factor or inertial factor can be found by correlations. The correlation proposed by Geertsma [21] is given by:

$$\beta = \frac{4.851 \times 10^4}{\phi^{5.5} \sqrt{k}}$$
(15)

The consideration on the skin factor effect on gas testing was recognized by Fligelman et al. [25] who provided correction charts to account for apparent skin factor values.

#### 2.2. Conventional analysis

The solution to the transient diffusivity equation, Eq. (8), is given by:

$$m(P)_{D}(1, t_{Da}) = -\frac{1}{2}Ei\left(-\frac{1}{4t_{Da}}\right)$$
(16)

The dimensionless parameters used in this chapter are given below. The rigorous dimensionless time is:

$$t_D = \frac{0.0002637kt}{\phi(\mu c_t) r_w^2}$$
(17)

Including the pseudotime function,  $t_a(P)$ , the dimensionless pseudotime is:

$$t_{Da} = \left(\frac{0.0002637k}{\phi r_w^2}\right) t_a(P) \tag{18}$$

Notice that the viscosity-compressibility product is not seen in Eq. (16) since they are included in the pseudotime function. However, if we multiply and, then, divide by  $(\mu c_t)_i$ , a similar equation to the general dimensionless time expression will be obtained.

$$t_{Da} = \left(\frac{0.0002637k}{\phi(\mu c_t)_i r_w^2}\right) [(\mu c_t)_i \times t_a(P)]$$
<sup>(19)</sup>

The dimensionless pseudopressure and pseudopressure derivatives are:

$$t^* \Delta m(P)_D{}' = \frac{hk[t^* \Delta m(P)']}{1422.52q_{sc}T}$$
(19a)

$$m(P)_D = \frac{hk[m(P_i) - m(P)]}{1422.52qT}$$
(20)

$$t_a(P)^* \Delta m(P)_D{'} = \frac{hk[t_a(P)^* \Delta m(P)']}{1422.52q_{sc}T}$$
(21)

And the dimensionless wellbore storage coefficient is given by:

$$C_D = \begin{pmatrix} 0.8935\\ \overline{\phi}hc_t r_w^2 \end{pmatrix} C$$
(22)  
The dimensionless radii are given:  
$$r_D = \frac{r}{r_w}$$
(23)

$$r_{De} = \frac{r_e}{r_w} \tag{24}$$

For practical purposes, Eq. (16) will end up in a semilog behavior of pseudopressure drops against time. After replacing the respective dimensionless quantities into the mentioned straight-line semilog expression, it is obtained [4]:

$$m(P_i) - m(P_{wf}) = \frac{1.422 \times 10^6 q T}{kh} \left[ 1.1513 \log\left(\frac{kt}{1688\phi(\mu_g c_t)_i r_w^2}\right) + s' + D \right]$$
(25)

$$m(P_i) - m(P_{wf}) = \frac{1.422 \times 10^6 q T}{kh} \left[ 1.1513 \log\left(\frac{kt_a(P)}{1688\phi r_w^2}\right) + s' + D \right]$$
(26)

The above equations are applied during transient or radial flow regime. They are used to find reservoir transmissibility and apparent skin factor from the slope and intercept, respectively, of a semilog plot of well-flowing pressure versus time. After applying the superposition principle, the above equations for the buildup case are converted into:

$$m(P_i) - m(P_{wf}) = \frac{1.422 \times 10^6 qT}{kh} \log\left(\frac{t_p + \Delta t}{\Delta t}\right)$$

$$m(P_i) - m(P_{wf}) = \frac{1.422 \times 10^6 qT}{kh} \log\left(\frac{t_a(P)_p + \Delta t_a(P)}{\Delta t_a(P)}\right)$$
(27)
(28)

From a semilog plot of pseudopressure versus time (or pseudotime), its slope allows calculating the reservoir permeability and the intercept is used to find the pseudoskin factor, respectively:

$$k = \frac{1637.74qT}{mh} \tag{29}$$

$$s' = \left[\frac{m(P_i) - m(P_{1hr})}{m} - \log\left(\frac{k}{\phi(\mu c_t)_i r_w^2}\right) - 3.227 + 0.8686\right]$$
(30)

Notice that for the pseudotime case,  $(\mu c_t)_i$  product in the above equation will be set as the unity. The gas pseudoskin factor is estimated for the buildup case as:

$$s' = \left[\frac{m(P_{1hr}) - m(P_{wf})}{m} - \log\left(\frac{k}{\phi(\mu c_t)_i r_w^2}\right) - 3.227 + 0.8686\right]$$
(31)

The governing dimensionless pressure equation during pseudosteady-state period is given by [28]:

$$m(P)_D = \frac{2t_D}{r_{eD}^2} + \ln r_D - 0.75 + s'$$
(32)

By replacing the dimensionless quantities, changing the log base, the above equation leads to:

$$m(P_i) - m(P_{wf}) = \frac{0.2395qTt}{Ah\phi} + \frac{3263qT}{kh} \left[ \log \frac{0.472r_e}{r_w} + \frac{s'}{2.303} \right]$$
(33)

A Cartesian plot of  $m(P_{wf})$  versus time or pseudotime during pseudosteady state will yield a straight line in which slope,  $m^*$ , is useful to find the well drainage area:

$$A = \frac{0.23395(5.615)qT}{\phi hm^*}$$
(34)

Such deliverability tests as backpressure, isochronal, modified isochronal, and flow after flow are conducted for the purpose of determining the flow exponent n (n = 1 is considered turbulent flow and 0.5 < n < 1 is considered to be rapid flow) and the performance coefficients. They assumed that stabilization is reached during the testing which is not true in most of the cases. Then, they are not included in this chapter but can be found in Chapter 4 of Ref. [4].

#### 2.3. TDS technique

Tiab [33] proposed a revolutionary technique which is very useful to interpret pressure tests using characteristics points found on the pressure and pressure derivative versus time log-log plot. He obtained practical analytical solutions for the determination of reservoir parameters.

$$m(P)_{Dr} = \left(\frac{7.029 \times 10^{-4} kh}{qT}\right) \left(\frac{m(P_i) - m(P_{wf})(t_n)}{q_n}\right) = \frac{1}{2} \left(\ln t_D + 0.80907 + 2s\right)$$
(35)

From a log-log plot of pseudopressure and pseudopressure derivative against pseudotime, **Figure 1**, several main characteristics are outlined:

1. The early unit-slope line originated by wellbore storage is described by the following equation:

$$m(P)_D = \frac{t_{Da}}{C_D} \tag{36}$$

Replacing the dimensionless parameters in Eq. (36), a new equation to estimate the wellbore storage coefficient is obtained:

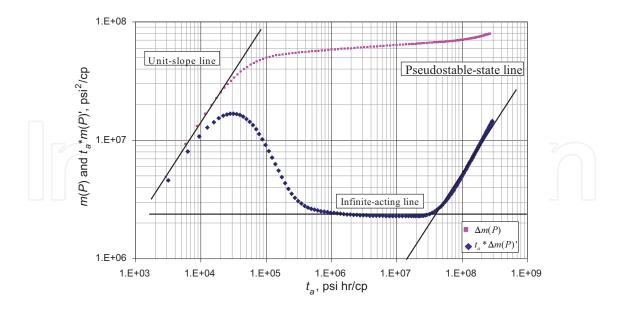


Figure 1. Log-log plot of pseudopressure and pseudopressure derivative versus pseudotime. After Ref. [7].

$$C = (0.419qTc_t) \left(\frac{t_a(P)}{\Delta m(P)}\right)$$
(37)

2. The intersection of the early unit-slope line with the radial horizontal straight line gives:

$$\left(\frac{t_{Da}}{C_D}\right)_i = 0.5\tag{38}$$

From this, an equation to estimate either permeability or wellbore storage is obtained once the dimensionless parameters are replaced.

As presented by Tiab [33], the governing equation for the well pressure behavior during radial flow reformulated by Escobar et al. [7] in terms of pseudofunctions is expressed by:

$$t_a(P)_i = \frac{1695c_tC}{kh} \tag{39}$$

3. According to Ref. [28], another form of Eq. (35) is obtained when wellbore storage and skin factor are included:

$$m(P)_{Dr} = \frac{1}{2} \left\{ \ln\left(\frac{t_{Da}}{C_D}\right)_r + 0.80907 + \ln(C_D e^{2s}) \right\}$$
(40)

From the above equation, the derivative of pseudopressure with respect to the natural log of  $t_{Da}/C_D$  is given by:

$$\left[\frac{t_{Da}}{C_D}m(P)'_D\right]_r = 0.5\tag{41}$$

From Eq. (21), the dimensionless pseudopressure derivative with respect to the natural log of  $\log t_{Da}/C_D$  gives:

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$$\left[\frac{t_{Da}}{C_D}m(P)'_D\right]_r = \left[7.029 \times 10^{-4}\frac{kh}{qT}\right][t_a(P) * m(P)']$$
(42)

Combination of Eqs. (41) and (42) will result into an equation to estimate permeability:

$$k = \frac{711.26qT}{h[t_a(P) * \Delta m(P)']_r}$$
(43)

3. Dividing Eq. (40) by Eq. (41), replacing the dimensionless quantities and, then, solving for the pseudoskin factor will yield:

$$s' = 0.5 \left[ \frac{[\Delta m(P)]_r}{[t_a(P) * \Delta m(P)']_r} - \ln\left(\frac{k(t_a(P))_r}{\phi r_w^2}\right) + 7.4316 \right]$$
(44)

Finally, the pressure derivative during the pseudosteady-state flow regime of closed systems is governed by:

$$t_{Da} * m(P)'_D = 2\pi t_{Da} \tag{45}$$

The intersection point of the above straight line and the radial flow regime straight line is:

$$t_{aDARP_i} = \frac{1}{4\pi} \tag{46}$$

After substituting the dimensionless pseudotime function into Eq. (46), a new equation for the well drainage area is presented:

$$A = \frac{kt_a(P)_{rpi}}{301.77 \,\phi}$$
(47)

Further applications of gas well test can be found in the literature. Escobar et al. [12] introduced the mathematical expressions for interpretation of pressure tests using the pseudopressure and pseudopressure derivative as a function of pseudotime for hydraulically fractured wells and naturally fractured (heterogeneous) formations. Fligelman [30] presented an interpretation methodology using *TDS* technique for finite-conductivity fractured wells. They used pseudopressure and rigorous time. In 2012, Escobar et al. [16] implemented the transient pressure analysis on gas fractured wells in bi-zonal reservoirs. Moncada et al. [31] extended the *TDS* for oil and gas flow for partially completed and partially penetrated wells. As far as horizontal wells, it is worth to mention the work performed in Refs. [11] and [15] on homogeneous and naturally fractured reservoirs.

#### 2.4. Example 1

Chaudhry [4] presented a reservoir limit test for a gas reservoir (example 5-2 of Ref. [4]). However, once the pressure derivative was taken to the test data, no late pseudosteady state regime was observed. Then, the input data given below were used to simulate a pressure test given in **Table 1**.

$S_g = 70\%$	$S_w = 30\%$	<i>q</i> = 6184 MSCF/D
h = 41 ft	<i>k</i> = 44 md	$B_g = 0.00102 \text{ ft}^3/\text{STB}$
$r_w = 0.4271 \text{ ft}$	$\phi$ = 10.04%	$c_t = 0.0002561 \text{ psi}^{-1}$
$\omega_{\rm g}$ = 0.0992 md/cp	$\gamma_g = 0.732$	<i>P<sub>cr</sub></i> = 380.16 psia
$T_{cr} = 645.06 \text{ R}$	<i>T</i> = 710 R	$r_e = 2200$ ft (349 Ac)
$m(P_i) = 340920304.2 \text{ psi}^2/\text{cp}$		
INLEC	MUDE	

<i>t,</i> hr	P, psi	t, hr	P, psi
0	3965	1.2713	3677.2527
0.001	3960.629	1.6005	3670.3779
0.002	3956.4313	2.0148	3663.602
0.003	3952.3774	2.5365	3656.8388
0.004	3948.4516	3.1933	3650.1477
0.005	3944.6431	4.0202	3643.5144
0.006	3940.9438	5.0107	3637.2126
0.007	3937.3469	6.0107	3632.0323
0.008	3933.8466	7.0107	3627.6664
0.009	3930.4382	8.0107	3623.8936
0.0113	3922.8277	9.0107	3620.5718
0.0143	3913.8402	10.0107	3617.6047
0.018	3903.2573	12.0107	3612.4479
0.0226	3891.1325	21.0107	3596.5482
0.0285	3877.5006	30.0107	3586.4447
0.0358	3862.4816	39.0107	3579.0231
0.0451	3846.2054	48.0107	3573.1536
0.0568	3829.2592	57.0107	3568.2967
0.0715	3812.1329	66.0107	3564.1453
0.09	3795.2335	75.0107	3560.4805
0.1133	3779.2686	84.0107	3557.2312
0.1271	3771.7594	93.0107	3554.3136
0.16	3757.7512	102.0107	3551.6672
0.2015	3745.1803	179.5107	3535.5164
0.2537	3734.0438	269.5107	3523.5847
0.3193	3724.1258	359.5107	3514.1663
0.402	3715.1658	449.5107	3505.545
0.5061	3706.8112	539.5107	3497.2804

t, hr P, psi		P, psi	<i>t</i> , hr	P, psi		
0.6372	0.6372 3698.9669		629.5107		3489.1576	
0.8021		3691.489	719.5	719.5107		
1.0098		3684.2741	809.5107		3473.056	
<i>t<sub>a</sub>(P)</i> , psi-hr/cp	$\Delta m(P)$ , psi <sup>2</sup> /cp	$t_a(P)^* \Delta m(P)'$ , psi <sup>2</sup> /cp	<i>t<sub>a</sub>(P)</i> , psi-hr/cp	$\Delta m(P)$ , psi <sup>2</sup> /cp	$t_a(P)^* \Delta m(P)'$ , psi <sup>2</sup> /cp	
0	0	-0	45802.414	1870739.384	17533667.77	
37.7745	270218.7615	265698.0159	57569.7648	1838960.003	17954428.54	
75.5167	518758.6126	520866.1041	72365.7851	1815682.598	18369258.28	
113.2278	751325.0471	767304.1906	90970.2467	1799003.726	18783428.06	
150.9089	968476.5902	1005966.456	114363.6923	1786548.918	19193297.17	
188.561	1172014.904	1237504.102	143779.3051	1774358.756	19599754.75	
226.185	1362245.214	1462410.249	178978.2667	1766967.699	19986008.75	
263.7817	1544967.139	1681099.321	214477.474	1764620.952	20303606.64	
301.352	1713052.797	1893921.256	249946.7071	1752899.594	20571329.92	
338.8966	1876882.193	2101169.292	285390.4587	1717299.587	20802733.84	
426.2923	2225474.894	2563944.683	320812.0523	1692510.182	21006509.26	
536.1368	2605002.302	3110507.871	356214.0473	1681851.999	21188553.27	
674.1563	3004035.218	3754179.95	426967.5286	1725356.98	21505009.16	
847.5255	3404366.431	4491744.317	744772.1706	1759676.341	22480949.29	
1065.235	3781729.348	5321159.089	1061858.072	1799660.974	23101515.46	
1338.5511	4101068.915	6235191.645	1378463.16	1769298.728	23557564.54	
1681.5934	4335396.363	7226023.963	1694705.511	1759287.154	23918367.9	
2112.0768	4462372.666	8257991.514	2010656.317	1770713.335	24217012.8	
2652.2558	4463511.759	9301323.123	2326363.101	1736601.944	24472345.81	
3330.0995	4300906.005	10331215.57	2641858.765	1709368.012	24697796.42	
4180.8019	4056795.12	11304325.65	2957168.15	1701504.59	24897723.65	
4684.3808	3917486.951	11762181.87	3272311.76	1711704.512	25077261.23	
5880.9567	3569692.658	12616571.14	3587306.105	1744436.565	25240114.57	
7383.6218	3191507.548	13383609.83	6295436.794	1821464.183	26234973.81	
9271.202	2873762.477	14063387.95	9432920.282	2036512.441	26970809.17	
11642.9004	2591188.809	14668995.81	12564795.27	2355209.644	27552034.83	
14623.503	2366500.199	15216145.54	15691965	2740929.323	28084374.29	
18369.9003	2197999.347	15726460.2	18814758.13	3212985.03	28594968.02	
23079.3518	2076483.39	16205683.18	21933329.44	3695740.205	29097073.99	
28999.9239	1985415.325	16662774.49	25047755.95	4195533.855	29595671.37	
36443.5374	1918507.605	17104058.59	28158083.33	4703995.72	30093194.56	

 Table 1. Pressure, pseudopressure, time, and pseudotime data for example 1.

Estimate permeability, skin factor, and drainage area by both conventional analysis and *TDS* technique.

#### 2.4.1. Solution by conventional analysis

**Figure 2** presents a semilog pressure of pseudopressure versus pseudotime. The slope and intercept of the radial flow regime straight line in such plot are given below:

$$m = -3995147.42 \text{ (psi}^2/\text{cp})/(\log \text{hr} - \text{psi}/\text{cp})$$
  
 $m(P)_{1 \text{hr}} = 342125555.5 \text{ psi}^2/\text{cp}$ 

Use of Eqs. (27) and (28) allows finding reservoir permeability and pseudoskin factor, respectively:

$$k = \frac{1637.74qT}{mh} = \frac{1637.74(6184)(710)}{(3995147.42)(41)} = 43.45 \text{ md}$$
$$s' = \begin{bmatrix} \frac{340920304.25 - 342125555.5}{-3995147.42} \\ -\log\left(\frac{43.45}{(0.1004)(0.4271^2)}\right) - 3.227 + 0.8686 \end{bmatrix} = -0.5172$$

To find the well drainage area, the Cartesian plot given in **Figure 3** was built. Its slope,  $m^* = 0.0914 \text{ (psi}^2/\text{cp)}/(\text{hr}-\text{psi}/\text{cp})$ , is plugged into Eq. (34):

$$A = \frac{0.23395qT}{\phi hm^*} = \frac{0.23395(6184)(710)}{(0.1004)(41)(0.0914)(43560)} = 336.4 \text{ Ac}$$

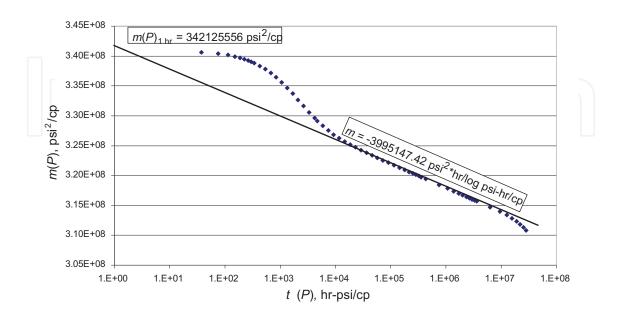


Figure 2. Semilog plot for example 1.

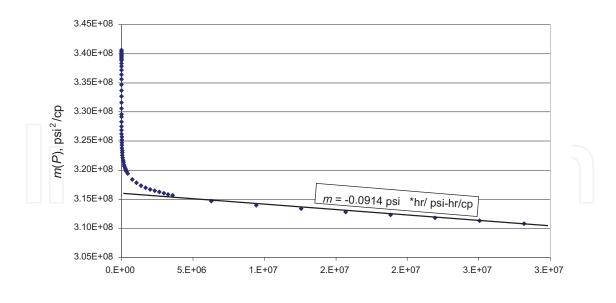


Figure 3. Cartesian plot for example 1.

### 2.4.2. Solution by TDS technique

**Figure 4** presents the pseudopressure and pressure derivative versus pseudotime log-log plot in which wellbore storage, radial flow regime, and late pseudosteady-state regimes are clearly observed. The following characteristic points were read from **Figure 4**:

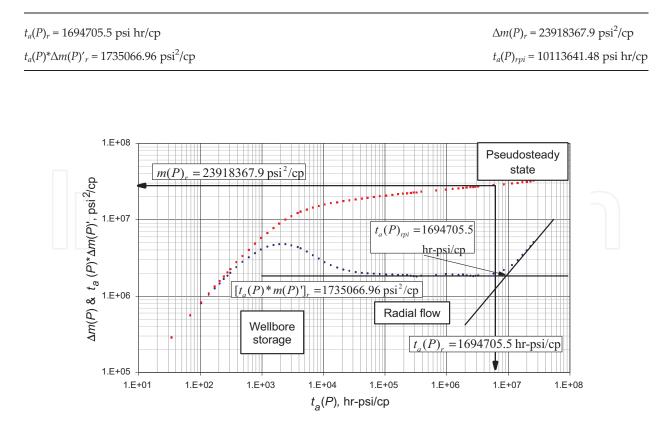


Figure 4. Pseudopressure drop and pseudopressure derivative versus time log-log plot for example 1.

Permeability and pseudoskin factor are respectively estimated from Eqs. (42) and (44),

$$k = \frac{711.26qT}{h[t_a(P) * \Delta m(P)']_r} = \frac{711.26(6184)(710)}{(41)(1735066.96)} = 43.9 \text{ md}$$

$$s' = 0.5 \left[ \frac{23918367.9}{1735066.96} - \ln\left(\frac{43.9(1694705.5)}{(0.1004)(0.4271^2)}\right) + 7.4316 \right] = -0.454$$
and well drainage area is found with Eq. (47):
$$A = \frac{kt_a(P)_{rpi}}{301.77 \phi} = \frac{(43.9)(10113641.48)}{301.77 (0.1004)} = 336.4 \text{ Ac}$$

Finally, the inertial factor and the non-Darcy flow coefficient are estimated with Eqs. (14) and (15):

$$\beta = \frac{4.851 \times 10^4}{\phi^{5.5} \sqrt{k}} = \frac{4.851 \times 10^4}{(0.1004)\sqrt{43.9}} = 2265091235.63 \text{ ft}^{-1}$$
$$D = 2.222 \times 10^{-15} \frac{(0.732)(41)(43.9)(2265091235.63)}{(0.0992)(0.4271)(41^2)} = 9 \times 10^{-5} \text{ D/Mscf}$$

The true skin factor is found with Eq. (9):

$$s_a = s + Dq = -0.454 + 9 \times 10^{-5} (6184) = 1.42$$

It can be seen that the simulated parameters closely match the results obtained from the examples.

## 3. Transient rate analysis

Transient rate analysis is performed by recording the continuous changing flow rate under a constant bottom-hole pressure condition. This procedure is normally achieved in very low gas formations and shale gas systems.

### 3.1. Basic flow and dimensional equations

The Laplace domain, the rate of solution for a well producing against a constant bottom-hole well-flowing pressure was given by [34]:

$$q_D = \frac{1}{uK_0(\sqrt{u})} \tag{48}$$

The solution for a bounded reservoir was presented by [5]:

$$\overline{q}_{D} = \frac{I_{1}(r_{eD}\sqrt{u})K_{1}(\sqrt{u}) - K_{1}(r_{eD}\sqrt{u})I_{1}(\sqrt{u})}{\sqrt{u}[I_{0}(\sqrt{u})K_{1}(r_{eD}\sqrt{u}) + K_{0}(\sqrt{u})I_{1}(r_{eD}\sqrt{u})]}$$
(49)

For considerable longer times, Ref. [27] showed that the  $q_D$  function in Eq. (48) may be approximated by:

$$\frac{1}{q_D} = \frac{1}{2} \left[ \ln t_D + 0.80907 \right] \tag{50}$$

where the dimensionless reciprocal rate and reciprocal rate derivative are given by:

$$1/q_D = \frac{kh \,\Delta m(P)}{1422.52 \,Tq}$$
(51)  
$$t_D * (1/q_D)' = \frac{kh \left[t * \Delta m(P)'\right]}{1422.52 \,Tq}$$
(52)

Including pseudoskin effects in Eq. (49),

$$\frac{1}{q_D} = \frac{1}{2} [\ln t_D + 0.80907 + 2s']$$
(53)

#### 3.2. Conventional analysis

After replacing the dimensionless quantities and changing the logarithm base, it yields:

$$\frac{1}{q} = \frac{1.422 \times 10^6 qT}{kh\Delta m(P)} \left[ 1.1513 \log\left(\frac{kt_a(P)}{1688\phi r_w^2}\right) + s' \right]$$
(54)

As for the case of pressure transient analysis, from a semilog plot of pseudopressure versus time (or pseudotime), its slope allows calculating the reservoir permeability and the intercept is used to find the pseudoskin factor, respectively:

$$k = \frac{1637.74T}{mh \ \Delta m(P)} \tag{55}$$

$$s' = \left[\frac{(1/q)_{1hr}}{m} - \log\left(\frac{k}{\phi(\mu c_t)_i r_w^2}\right) - 3.227 + 0.8686\right]$$
(56)

Considering approximation for large time to the analytical Laplace inversion of Eq. (49), the following expression is obtained:

$$q_D = \frac{1}{\ln r_{eD} - 0.75} \exp\left[\frac{-2t_D}{r_{eD}^2(\ln r_{eD} - 0.75)}\right]$$
(57)

For  $t_D \ge t_{Dpss}$ , this flow period is known as the exponential decline period.  $t_{Dpss}$  is the time required for the development of true pseudosteady state at the producing well for constant rate production case. Eq. (57) concerns only the circular reservoir. The solution can be generalized for other reservoir shapes by using the Dietz shape factor [6],  $C_A$ ,

$$q_D = \frac{2}{\ln\left(\frac{4A_D}{\gamma C_A}\right)} \exp\left[\frac{-4\pi t_D}{A_D \ln\left(\frac{4A_D}{\gamma C_A}\right)}\right]$$
(58)

where,  $A_D$  (dimensionless area) and  $r_{eD}$  (dimensionless radius) are given by:

$$A_D = \frac{A}{r_w^2}$$
(59)  
$$r_{eD} = \frac{r_e}{r_w e^{-s}} = \frac{r_e}{r_{weff}}$$
(60)

Eq. (58) suggests that a plot of log(q) versus time will yield a straight line with negative slope  $M_{decline}$ ,

$$M_{decline} = \frac{2(0.0002637)k}{r_{eD}^2(\ln r_{eD} - 0.75)\phi\mu c_t r_w^2}$$
(61)

and intercept at (t = 0):

$$q_{\rm int} = \frac{kh\Delta m(P)}{1637.74B\mu(\ln r_{eD} - 0.75)}$$
(62)

The reservoir area can be determined by solving the Eq. (62) for  $r_{eD}$ :

$$r_{eD} = \exp\left(\frac{1637.74B\mu}{kh\Delta m(P)(\ln r_{eD} - 0.75)}q_{\rm int} + 0.75\right)$$
(63)

#### 3.3. TDS technique

Escobar et al. [9] extended the *TDS* Technique for gas well in homogeneous and naturally fractured formations using rigorous time. The equations they presented for wellbore storage coefficient and permeability are given below:

$$C = 0.4196 \frac{Tq \ t_N}{\mu \ \Delta m(P)_N} = 0.4198 \frac{T}{\mu \ \Delta m(P)} \left[ \frac{t}{t * (1/q)'} \right]_N$$
(64)  
$$k = 711.5817 \frac{T}{h \ \Delta m(P)[t \times (1/q)']_r}$$
(65)

Using a procedure similar to the pressure transient case, Escobar et al. [9] found an expression to estimate the pseudoskin factor:

$$s' = 0.5 \left\{ \frac{(1/q)_r}{[t \times (1/q)']_r} - \ln\left(\frac{kt_r}{\phi \,\mu \, c_t r_w^2}\right) + 7.43 \right\}$$
(66)

For the estimation of reservoir area, Escobar et al. [9] also presented an equation that uses the starting time of the pseudosteady-state period,  $t_{spss}$ .

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$$r_e^2 = \left(\frac{0.0015k \, t_{spss}}{\phi \mu \, c_t}\right)^{1/2} \tag{67}$$

As treated in pressure transient analysis, Eq. (41), the reciprocal rate derivative takes a value of 0.5 during radial flow. The intercept of this with the reciprocal rate derivative of Eq. (57) will provide:

$$t_{D_{rpi}} = \frac{1}{2} r_{eD}^{2} [\ln(r_{eD}) - 0.75]$$
(68)  
in which numerical solution gives:  
$$r_{eD} = 1.0292 \ t_{D_{rpi}}^{0.4627}$$
(69)

After replacing the dimensionless quantities, we obtain:

$$r_e = 22.727 \times 10^{-3} r_{weff} \left(\frac{k}{\phi \,\mu \, c_t r_{weff}^2}\right)^{0.4627} t_{rpi}^{0.4627} \tag{70}$$

Refs. [13] and [14] presented rate transient analysis for long homogeneous and naturally fractured oil reservoirs using *TDS* technique and conventional analysis, respectively. Equations can be easily translated to gas flow.

#### 3.4. Example 2

Escobar et al. [9] presented an example for a homogeneous bounded reservoir. **Figure 5** and **Table 2** present the reciprocal rate and reciprocal rate derivative versus rigorous time for this exercise. Other relevant data for this example are given below:

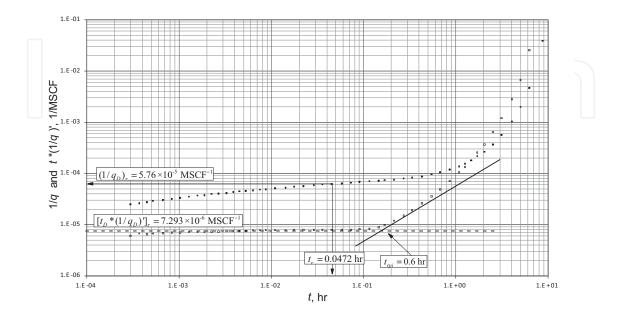


Figure 5. Reciprocal rate and reciprocal rate derivative for example 2-homogeneous bounded reservoir. After Ref. [9].

h = 80 ft	<i>k</i> = 25 md	$r_w = 0.3 \text{ ft}$
$\phi = 25\%$	$c_t = 0.00187 \text{ psi}^{-1}$	$\mu_{\rm g}$ = 0.0122 md/cp
$\gamma_g = 0.85$	<i>T</i> = 670 R	$r_e = 30$ ft (0.065 Ac)
$\Delta m(P) = 340920304.2 \text{ psi}^2/\text{cp}$	$\Delta P = 580 \text{ psi}$	

Find reservoir permeability,	skin factor,	and drainage	e radius for this	example usi	ng the TDS
Technique.					

<i>t</i> , hr	1/ <i>q</i> , MSCF <sup>-1</sup>	$t^*(1/q)'$ , MSCF <sup>-1</sup>	<i>t</i> , hr	1/q, MSCF <sup>-1</sup>	$t^*(1/q)', MSCF^{-1}$
		$t(\Pi q)$ , wistr			
3.11E-04	43189.24959	179751.1071	4.72E-02	17360.95346	135561.954
3.89E-04	40834.91569	162199.4397	6.09E-02	16811.48278	135417.1412
4.67E-04	39060.52002	163534.7645	7.58E-02	16365.45213	135450.8332
5.45E-04	37655.94848	160065.4877	0.094767643	15935.44127	134654.7122
7.01E-04	35537.19664	157149.8777	0.122175588	15464.07533	130033.9989
8.72E-04	33849.9472	154708.1815	0.152075165	15058.4209	120446.6934
1.07E-03	32361.46026	152593.8776	0.176991479	14766.60107	110524.7186
1.35E-03	30871.32659	150543.0499	0.224830802	14266.98732	91414.11215
1.66E-03	29601.36073	148839.1511	0.284629956	13699.34978	71972.81156
1.97E-03	28617.55908	147555.5061	0.354395635	13079.44168	55862.58323
2.36E-03	27646.46771	146325.5009	0.450074281	12279.66271	41400.85561
2.80E-03	26785.03603	145257.0868	0.569672588	11348.65545	30197.97654
3.42E-03	25823.21027	144105.0598	0.709203946	10349.64392	22079.63438
4.04E-03	25068.84401	143224.7896	0.900561238	9119.41797	15300.5905
4.73E-03	24398.17164	142461.4954	1.139757852	7783.903591	10316.16432
5.54E-03	23753.19888	141745.6607	1.315168702	6930.721305	7965.441894
6.63E-03	23056.85049	140996.5214	1.522472435	6043.090594	6009.327954
7.87E-03	22423.58559	140330.625	1.801535152	5027.292996	4239.056471
9.12E-03	21908.28203	139803.0353	2.120463971	4077.321632	2935.619806
1.15E-02	21141.51732	139045.8455	2.630750081	2923.310968	1712.191843
1.49E-02	20332.18915	138280.5426	3.28455416	1917.14852	909.5234175
1.86E-02	19683.45322	137688.6861	4.241340618	1040.993708	385.7970016
2.34E-02	19065.59817	137131.4759	5.261912839	543.216581	162.6885651
3.02E-02	18406.42719	136508.2532	6.569520997	230.4829168	41.88651512
3.77E-02	17872.96521	135981.9447	9.12095155	27.98082076	0.548915189

 Table 2. Reciprocal rate, reciprocal rate derivative versus time data for example 2.

### 3.4.1. Solution

The following characteristic points were read from **Figure 5**:

$t_r = 4.72 \times 10^{-2} \mathrm{hr}$	$[t^*(1/q)']_r = 7.293 \times 10^{-6} \text{ D/Mscf}$
$(1/q)_r = 5.76 \times 10^{-5} \text{ D/Mscf}$	$t_{rpi} = 0.06 \text{ hr}$

Eqs. (65), (66), and (70) are used to obtain permeability, skin factor, and drainage.

$$k = \frac{711.5817T}{h \Delta m(P)[t \times (1/q)']_r} = \frac{711.5817(670)}{(80)(30976300)(7.293 \times 10^{-6})} = 26.37 \text{ md}$$

$$s' = 0.5 \left\{ \frac{(5.76 \times 10^{-5})}{(7.293 \times 10^{-6})} - \ln\left(\frac{(25)(0.0472)}{(0.25)(0.0122)(0.00187)(0.3)^2}\right) + 7.43 \right\} = 0.68$$

$$r_e = 22.727 \times 10^{-3}(0.3) \left(\frac{(25)}{(0.25)(0.0122)(0.00187)(0.3)^2}\right)^{0.4627} (0.6)^{0.4627} = 19.5 \text{ ft}$$

Notice that the results closely match the permeability and external reservoir radius as presented by Ref. [9].

Finally, it is worth to mention that nowadays, conventional shale-gas reservoirs have become very attractive in the oil industry. Then, their characterization via well test analysis is very important. Shale-gas reservoir is normally tested under constant well-flowing pressure conditions—transient rate analysis—then, the recent studies performed in Refs. [17] and [22] should be read. If such wells are tested under constant rate conditions—pressure transient analysis—then the reader should refer to the works by Bernal et al. [3] and Escobar et al. [18].

## Nomenclature

А	Well drainage area, ft <sup>2</sup> and Ac
В	Volumetric factor, rb/MSCF
С	Wellbore storage coefficient, bbl/psi
C <sub>t</sub>	Total compressibility, 1/psi
D	Turbulent flow factor, Mscf/D
h	Formation thickness, ft
$h_p$	Perforated interval, ft
$I_{0}, I_{1}$	Bessel function
k	Permeability, md
$K_{0}, K_{1}$	Bessel function
т	Semilog slope
$m^*$	Cartesian slope
m(P)	Pseudopropressure function, psi <sup>2</sup> /cp
$M_{decline}$	Slope of plot of log( <i>q</i> ) versus time
п	Flow exponent
Р	Pressure, psi

$P_D$	Dimensionless pressure
$P_{wf}$	Well-flowing pressure, psi
q	Gas flow rate, MSCF
1/q	Reciprocal of the flow rate, D/Mscf
r	Radius, ft
r <sub>e</sub>	External reservoir radius, ft
$r_w$	Radio del pozo, ft
r <sub>weff</sub>	Effective wellbore radius, $r_w e^{-s}$ , ft
s'	Apparent or pseudoskin factor
Sa	Total skin factor
t	Time, hr
$t_D * P_D'$	Dimensionless pressure derivative
$t_{Dpss}$	Exponential decline period
$t^{*}(1/q)'$	Reciprocal rate derivative, D/Mscf
$t_D^*(1/q_D)'$	Dimensionless reciprocal rate derivative
$t_p$	Horner or producing time
$t_{pss}$	Exponential decline period, hr
$t_{spss}$	Time to initiate pseudosteady state, hr
u	Argument for a Bessel function
Ζ	Gas supercompressibility factor

## Greek

- $\alpha$  Turbulence factor or inertial factor
- $\triangle$  Change, drop
- $\phi$  Porosity, fraction
- $\gamma$  Euler's constant 1.781 or e<sup>0.5772</sup>
- $\gamma_{g}$ Gas gravity
- $\lambda$  Mobility, md/cp
- $\mu$  Viscosity, cp

## Suffices

- 1 *hr* One hour
- *cr* Condition at critical point
- DA Dimensionless referred to drainage area
- Da Dimensionless referred to pseudotime
- D Dimensionless
- De Dimensionless referred to external
- e External
- *eff* Effective
- g Gas

i	Initial or intercept
pss	Pseudosteady state
r	Radial flow
ref	Reference
rpi	Intercept radial-pseudosteady
t	Total
$t_a(P)$	Pseudotime, psi-hr/cp
w	Well
Autł	nor details

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