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The Theory of Giant Splash of Photoresponse in Semiconductors at Low-Level Illumination with Increasing Concentration of Deep Recombination Impurity

Viacheslav A. Kholodnov and Mikhail S. Nikitin

Additional information is available at the end of the chapter

http://dx.doi.org/10.5772/61028

Abstract

Recombination of excess (nonequilibrium) electrons and holes in semiconductors through impurity recombination centers (traps) known as trap-assisted (Shockley-Read-Hall) recombination is in many cases the dominant process. In this chapter, we develop the general theory of trap-assisted recombination and study in detail two key characteristics: (1) dependences of excess charge carriers' lifetime and photoelectric gain on concentration N of recombination centers and (2) effectiveness of band-to-band photoexcitation of charge carriers and photo-emf in semiconductors at low-level illumination considered outside quasi-neutrality approximation.

We have done systematic mathematical and detailed physical analysis of considered characteristics. Giant splash of photoresponse in semiconductors with increasing recombination center concentration N is caused mainly by the growth of charge carriers' lifetime in orders of magnitude. Also, this factor is sufficient to provide an increase, in order of magnitude and more, in efficiency of charge carriers' photoexcitation with increasing N. Results of strict analytical calculations (i.e., outside commonly used local approximation of quasi-neutrality) show, that, photoinduced local space charge affects substantially on giant splash of semiconductor photoelectric response with increasing concentration of recombination centers.

The theory of giant splash of photoresponse in semiconductors at low-level illumination with increasing concentration of recombination centers could develop further through generalization of boundary conditions on semiconductor surfaces and current contact electrodes, accounting for nonuniformity of charge carriers' photoexcitation along the line of current flow and fluctuation processes. The study of nonstationary (frequency domain and transient) characteristics is of particular interest.



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It follows from physical essence of considered effects that similar effects can occur in other mediums with recombination of dissociative or ion-ion type, for example, in multicomponent plasma as well.

Keywords: Impurity recombination center (trap), Trap-assisted (Shockley-Read-Hall) recombination, Excess (nonequilibrium) charge carriers, Band-to-band photogeneration of excess charge carriers, Electron lifetime, Hole lifetime, Photoresponse, Photoelectric gain, Photo-emf, Small deviation from equilibrium state in semiconductor, Photoinduced space charge, Approximation of quasi-neutrality, Giant splash of photoresponse

1. Introduction

Recombination of excess (nonequilibrium) electrons and holes in semiconductors through impurity recombination centers (traps) referred to in this chapter as trap-assisted (Shockley-Read-Hall) recombination is in many cases the dominant process [1-9]. Hall [10] and Shockley and Read [11] have proposed the theory of trap-assisted recombination as early as 1952. Further, the theory of trap-assisted recombination has been developed in many aspects and details [1-5, 12-14]. At the same time, due attention was not paid to study dependences of lifetimes of excess electrons $\tau_n(N)$ and holes $\tau_p(N)$ on concentration of traps N. In some cases, traps are produced intentionally by doping semiconductor (e.g., by bombarding with high-energy ions [15, 16]) to reduce time of transient processes. It seems that lack of attention is caused by traditional understanding that the larger the concentration of traps N, the greater the capture rate of excess charge carriers on impurity level traps and, therefore, the shorter the lifetimes of excess charge carriers.

That reasonable understanding is incompletely adequate to reality. As shown below, lifetimes of excess electrons and holes (see our definition of τ_n and τ_p in Section 2) may grow strongly (in order of magnitude and more) with increase of concentration *N*.

In this chapter, we generalize the theory and give systematic mathematical and detailed physical analysis of dependences $\tau_n(N)$ and $\tau_p(N)$ on concentration of recombination centers.

2. Preliminaries

Let's consider the case of small deviation of free charge carriers' concentrations from equilibrium values. This situation occurs often in semiconductors used for registration of low-level signals, for example, optical signals. It will be shown that both $\tau_n(N)$ and $\tau_p(N)$, under certain conditions, will grow very strongly with increasing N in a particular interval of N values. Completely different physical mechanism causes this increase in lifetimes. It differs from mechanisms available for many years [4], as well as proposed in [17]. We analyze extreme points (corresponding formulas are derived) of dependences $\tau_n(N)$ and $\tau_p(N)$ as functions of semiconductor parameters and temperature. We give detailed physical interpretation of obtained results. In particular, it is shown that physical mechanisms responsible for strong non-monotonic dependences $\tau_n(N)$ and $\tau_n(N)$ differ from each other.

It is reasonable to expect that the growth of lifetimes $\tau_n(N)$ and $\tau_p(N)$ with increasing N will lead to the growth of photoresponse of semiconductor sample (including photoelectric gain G). However, specificity of dependences $\tau_n(N)$ and $\tau_p(N)$ does not determine the type of dependence G(N) in total. As it follows from [18, 19], G increases with increasing charge carriers' lifetime, if ambipolar mobility [2, 13] $\mu_a=0$ or there is no recombination at current contact electrodes (x=0 and x=W; see insert in Figure 1a). In reality, recombination at current contact electrodes is always happening to some extent [5-9]. Therefore, in normal conditions ($\mu_a \neq 0$), increase in lifetimes, after reaching some values, does not lead to an increase in photocurrent I_{ph} [5, 9, 18, 19]. Saturation of I_{ph} becomes apparent in the case of high-rate recombination at the contact electrodes (sweep-out effect [5, 9, 18, 19]) when

$$\Delta n(0) = \Delta p(0) = \Delta n(W) = \Delta p(W) = 0, \tag{1}$$

where $\Delta n(x) = n(x) - n_e$ and $\Delta p(x) = p(x) - p_e$ are deviations of electron n and hole p concentrations from their equilibrium values n_e and p_e , respectively. In trap-assisted recombination, function $\mu(N)$ can vanish at the same (up to small corrections) concentration N, at which dependences $\tau_n(N)$ and $\tau_p(N)$ reach points of maximal extremum $\hat{\tau}_n$ and $\hat{\tau}_p$ (Figure 1b and 1c). Therefore Gand, hence, I_{ph} grow to the extent of increase in $\tau_n(N)$ and $\tau_p(N)$. These are physical grounds of giant splash of photoelectric gain with increasing N (Figure 1a).

It was first reported in [20] that vanishing $\mu(N)$ in points of maximal extremum of dependences $\tau_n(N)$ and $\tau_p(N)$ allows avoiding highly undesirable effect – saturation of *G* in intrinsic photoconductors, when applied bias voltage *V* increases [5, 9, 18, 19, 21, 22]. As is known [19], this disadvantage is the most evident in photoconductors with sweep-out effect on contact electrodes, i.e., when relations (1) are fulfilled. Result presented in Ref. [20] was obtained in approximation of quasi-neutrality [1-9, 13, 18, 19, 21, 22], which was usually used at moderate electric fields, i.e., when we neglect in Poisson equation by term $\Delta \rho \equiv (\varepsilon \times \varepsilon_0) \times div \Delta E$, which determines the density of photoinduced space charge $\Delta \rho$.

In our case, $\Delta E \equiv E(x) - E_0$ is the variation of electric field caused by deviation of concentrations of free charge carriers and their traps from equilibrium values by reason of band-to-band absorption of radiation, E(x) and E_0 are the electric field intensity in the presence and absence of illumination, ε is the relative dielectric permittivity of semiconductor, and ε_0 is the vacuum permittivity. However, even at moderate electric fields ($\approx 1 \div 10$ V/cm), approximation of quasineutrality is not always acceptable [23].

Below, in case of single recombination level, we consider in detail the impact of photoinduced space charge $\Delta \rho$ on value *G* of photoelectric gain *G* in semiconductors with sweep-out effect on contact electrodes at the point of maximal extremum of function *G*(*N*) (Figure 1a). Considering semiconductor as base material for making intrinsic photoconductors with threshold electro-optical performance, we assume that photocarriers are excited by photons of low-intensity optical radiation with wavelength range responding to fundamental absorption band of semiconductor. Figure 2a shows that we cannot use approximation of quasi-neutrality, when voltage *V* across the sample becomes larger than some particular value.

Also, ignoring approximation of quasi-neutrality, we study, at low-level illumination, the effectiveness of band-to-band photoexcitation of charge carriers and photo-emf V_{ph} in semiconductors with dominant trap-assisted recombination. Analytical expressions for photo-emf V_{ph} and mean, with respect to light propagation length, concentrations of photoelectrons $<\Delta n >$ and photoholes $<\Delta p >$ are given. It is shown that target values of V_{ph} , $<\Delta n >$, and $<\Delta p >$ can be improved radically by increasing concentration of recombination centers; moreover, approximation of quasi-neutrality can lead to errors of several orders of magnitude.

Analyzing above-mentioned problems, we do not use conventional (Shockley-Read) expression-based form [1-5, 9, 11-14] of generation-recombination rate. This form does not allow to express explicitly dependences τ_n and τ_p and, even more, I_{ph} and V_{ph} on N. And therefore, because of the need for solving complex transcendental equations, conventional (Shockley-Read) expression-based form leads to serious mathematical difficulties in study (especially analytical) dependences $\tau_{n,p}(N)$ and, even more, $I_{ph}(N)$ and $V_{ph}(N)$.

These difficulties are dramatized by the fact that under certain conditions, $\tau_{n,p'} I_{ph}$ and V_{ph} are dependent very strongly on concentration N in a particular interval of N (Figure 1a, 1b, 7). Perhaps, it was the main reason for longtime absence of complete theoretical analysis of lifetime dependences $\tau_{n,p}(N)$, while detailed analysis of lifetime dependences on concentrations of free charge carriers was made in pioneering paper by Shockley and Read [11] concerning the theory of recombination through impurity level trap. In present chapter, we use the method of calculation assuming that N is expressed in terms of the ratio of the number of filled recombination level states to the number of empty. This allows to avoid transcendental equations, in other words, to avoid the need to solve inverse problem. As a result, the described above approach simplifies greatly the mathematical analysis and physical interpretation of calculations of desired parameters.

3. Model and basic relations

Consider nondegenerated semiconductor doped by shallow fully ionized single type impurity (for definition donors) with concentration N_D . Recombination of excess charge carriers occurs in said semiconductor through the energy level of acceptor impurity atoms with concentration N, which can be in two charge states (assume in neutral and singly negatively charged). Concentration of recombination impurity atoms in neutral state corresponds to concentration of acceptor atoms N_0 , which are simultaneously centers of electron capture and centers of thermal emission of holes. Concentration of atoms $N_{-}=N-N_0$, which are capture centers of holes and, at the same time, centers of thermal emission of electrons. Described above is recombination through single-level trap [10-13] (Figure 5b), which is often dominant [1-5, 9, 14] and called Shockley-Read-Hall recombination.

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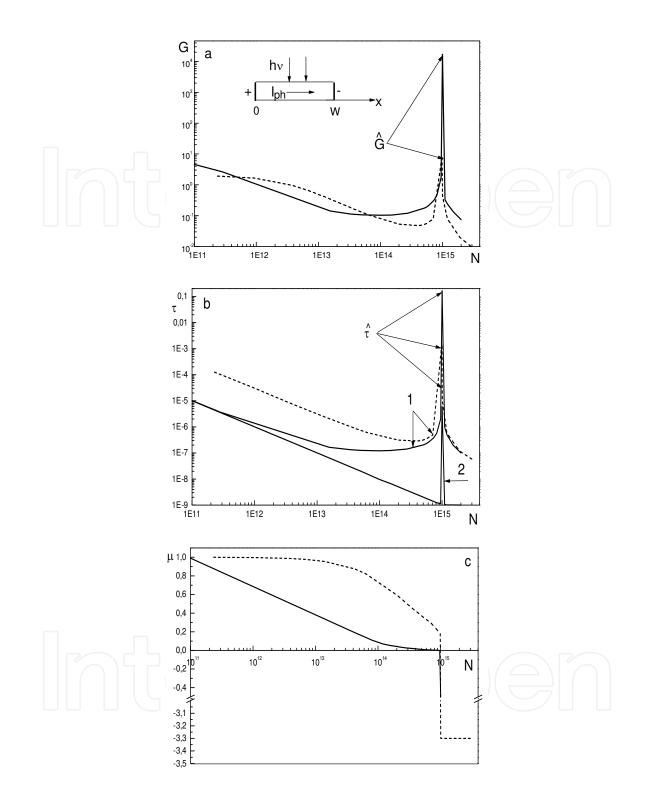


Figure 1. Dependences on concentration of single-level recombination centers N (cm⁻³): (a) G- photoelectric gain; (b) τ - lifetime of electrons (curve 1) and holes (curve 2) (s); (c) μ - ambipolar mobility of charge carriers (in units of hole mobility). Adopted: room temperature, $W=10^{-1}$ cm, $\theta \equiv w_p/w_n=10^2$, $w_n=10^{-8}$ cm³/s, $n_i/n_t=10^4$, $N_D=10^{15}$ cm⁻³, $E_0=10$ V/cm. Solid curves, *GaAs*, and dashed curves, *Si*. Physical parameters of semiconductors are obtained from monograph [3]. Schematic view of photoconductor on insert in Figure 1a

Let either band-to-band excitation (Figure 5b) or injection on the contacts produce excess electrons and holes. Then, in stationary case, equation

$$R_{n} = R_{p} \tag{2}$$

determines the charge state of recombination impurity atoms.

Recombination-generation rates of electrons R_n and holes R_p due to capture of charge carriers by acceptor impurity traps and their thermal emission from recombination level states into permitted conduction or valence bands are equal to

$$R_n = (n \times N_0 - \delta^{-1} \times n_e \times N_-) \times w_n, R_p = (p \times N_- - \delta \times p_e \times N_0) \times w_p.$$
(3)

Here, w_n and w_p are electron and hole capture probabilities, respectively, at appropriate recombination level state, $\delta = N_-^e / N_0^e$ (superscript indicates equilibrium values of concentration of recombination impurity atoms *N* in relevant charge states).

For small deviation of charge carriers' and their capture centers' concentrations $\Delta N_0 = N_0 - N_0^e = -\Delta N_- = N_-^e - N_-$ from equilibrium values, we can linearize relations (2) and (3) with respect to proper deviations. Then taking into account Poisson equation

$$\Delta \rho \equiv \frac{\varepsilon}{4\pi} \times \frac{\partial \Delta E}{\partial x} = q \times \left[\Delta p - \Delta n - \Delta N_{-} \right], \tag{4}$$

we obtain

$$R_n = \frac{\Delta n}{\tau_n} + a_n \times div\Delta E,\tag{5}$$

$$R_{p} = \frac{\Delta p}{\tau_{p}} - a_{p} \times div\Delta E,$$

$$\Delta p = \frac{\tau_{p}}{\tau_{n}} \times \Delta n + (a_{n} + a_{p}) \times \tau_{p} \times \frac{d\Delta E}{dx},$$
(6)
(7)

where

$$\frac{1}{\tau_n} = w_n \times N \times \frac{\delta \times \theta}{1+\delta} \times \frac{N + (1+\delta) \times (1+\delta^{-1}) \times (n_e + p_e)}{\delta \times \theta \times N + (1+\delta) \times (1+\delta^{-1}) \times (n_e + \delta \times \theta \times p_e)},$$
(8)

$$\frac{1}{\tau_p} = w_p \times N \times \frac{\delta}{1+\delta} \times \frac{\delta \times N + (1+\delta)^2 \times (n_e + p_e)}{\delta \times N + (1+\delta^2) \times (n_e + \delta \times \theta \times p_e)},$$
(9)

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$$a_{n} = \frac{\varepsilon}{4\pi \times q} \times w_{n} \times N \times n_{e} \times \frac{\theta \times (1+\delta)}{\delta \times \theta \times N + (1+\delta) \times (1+\delta^{-1}) \times (n_{e} + \delta \times \theta \times p_{e})},$$
(10)

$$a_{p} = \frac{\varepsilon}{4\pi \times q} \times w_{p} \times N \times p_{e} \times \frac{1+\delta}{N+(1+\delta)\times(1+\delta^{-1})(n_{e}+\delta\times\theta\times p_{e})},$$
(11)

 ΔE is change in electric field caused by deviation of charge carriers' and capture centers' concentrations from equilibrium values, and q is absolute electron charge value and $\theta = w_p / w_n$. First terms in (5) and (6) mean recombination rates of excess electrons and holes (and therefore, symbols τ_n and τ_p mean their lifetimes) in quasi-neutrality with respect to electric field ΔE , i.e., at sufficiently small values $div\Delta E$ [1-3, 5, 9-14, 18, 24, 25]. We will use the same terminology for τ_n and τ_p in the case of failure to comply quasi-neutrality (see below); therefore values τ_n and τ_p will not depend on value $div\Delta E$ in the present study.

High-performance photoconductors operate with extremely low-level illumination. Therefore, linear for *g* approximation, usually used in the theory of high-performance photodetectors [5-7, 9, 21, 22, 26], is correct in calculation of photoelectric gain *G*, where *g* is density of charge carriers' photoexcitation rate.

In view of the above provision, we can write expressions for the density of photocurrent components as follows:

$$\Delta I_n = q \times \mu_n \times (E_0 \times \Delta n + n_e \times \Delta E) + q \times D_n \times \frac{\partial \Delta n}{\partial x},$$
(12)

$$\Delta I_{p} = q \times \mu_{p} \times (E_{0} \times \Delta p + p_{e} \times \Delta E) - q \times D_{p} \times \frac{\partial \Delta p}{\partial x}.$$
(13)

where μ_n and μ_p are electron and hole mobility and D_n and D_p are electron and hole diffusion constants. The density of electron ΔI_n and hole ΔI_p components of photocurrent

$$I_{ph} = \Delta I_n + \Delta I_p \tag{14}$$

must satisfy continuity equations:

$$\frac{\partial \Delta I_n}{\partial x} = q \times (R_n - g), \tag{15}$$

$$\frac{\partial \Delta I_p}{\partial x} = q \times (g - R_p), \tag{16}$$

and also

$$\frac{\partial I_{ph}}{\partial x} = 0. \tag{17}$$

Let limit voltage be applied to sample by value

$$V = E_0 \times W \tag{18}$$

that allows to neglect by the dependence of μ_n and μ_p on electric field, where *W* is distance between current contact electrodes (see insert in Figure 1a).

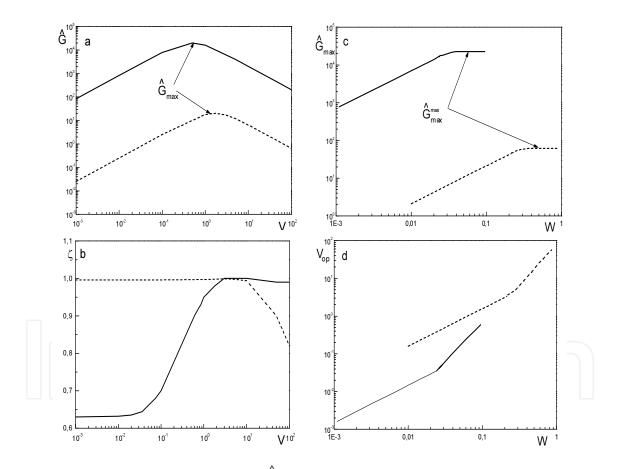


Figure 2. Dependences: (a), photoelectric gain G = G in point of maximal extremum of function $G(N_{\lambda})$ (see Figure 1a) on bias voltage across the sample V (distance between current contacts $W = 10^{-1}$ cm); (b), ratio $\zeta \equiv G_{appr} / G_{exact}$ on V at $W_{\lambda} = 10^{-1}$ cm, where $G_{app\chi}$ and G_{exact} are approximate and exact values G, respectively; (c), value G_{max} on W, where $G_{ma\chi}$ is maximal value G for given W (see Figure 2a); (d), value V_{op} on W, where V_{op} is optimal voltage, at which $G = G_{max}$ (see Figure 2c). Voltage V in V; length W in cm. Physical parameters of semiconductors and temperature are the same as in Figure 1. Solid curves GaAs, dashed curves Si

4. Lifetime of excess charge carriers

Using distribution function of electrons over acceptor level states [12, 27], we can write neutrality equation

$$n_e + N_-^e = p_e + N_D$$
 (19)
for nondegenerated semiconductor at thermodynamic equilibrium as follows:

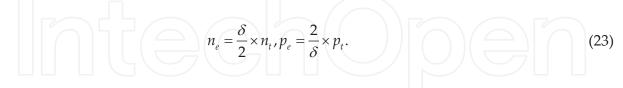
$$N = n_t \times \frac{1+\delta}{2\times\delta^2} \times f(\delta), \tag{20}$$

where

$$\delta = \frac{N_{-}^{e}}{N_{0}^{e}}, f(\delta) = B + A \times \delta - \delta^{2}, \qquad (21)$$

$$A = 2 \times \frac{N_D}{n_t}, B = 4 \times \frac{p_t}{n_t} = \left(\frac{2 \times n_i}{n_t}\right)^2,$$
(22)

 n_t and p_t are equilibrium concentrations of electrons and holes when Fermi level energy coincides with recombination level energy E_t , and n_i is intrinsic charge carriers' concentration. When derived (20), we have adopted that spin degeneracy factor of acceptor state is equal to 1/2 [2, 12, 14, 27]. In considered conditions



From expressions (8), (9), (20), and (23), it follows that

$$\tau_n = \frac{2\delta^2}{f(\delta)} \times \frac{\theta \times f(\delta) + (1+\delta) \times (\theta \times B + \delta)}{[\delta \times A + (2+\delta) \times B + \delta^3] w_v \times n_t},$$
(24)

$$\tau_{p} = \frac{2\delta}{f(\delta)} \times \frac{B + (A + \theta \times B) \times \delta + (\theta \times B + \delta) \times \delta^{2}}{[\delta \times A + (2 + \delta) \times B + \delta^{3}]w_{p} \times n_{t}}.$$
(25)

Expressions (20), (24), and (25) determine dependences $\tau_n(N)$ and $\tau_p(N)$ in parametric form. Figure 1b shows that, as usual, dependences $\tau_n(N)$ and $\tau_p(N)$ fall with increased N, but in some interval of concentration N, dependences can rise up sharply. Further, we give analytical solution of extremum problem for dependences $\tau_n(N)$ and $\tau_p(N)$ at $\theta \ge 1$, because hole is captured on attractive center and electron – on neutral.

4.1. Mathematical analysis of hole lifetime
The analysis of equation
$$\frac{\partial}{\partial \delta} \times \frac{1}{\tau_p} = 0,$$
(26)

which determines extremum points of dependence $\tau_p(N)$, shows that well-defined nonmonotonic behavior of this function occurs at

$$\xi_{1} \equiv \frac{3}{\theta \times B} << 1 << \frac{1}{\xi_{2}} \equiv \frac{A^{2}}{4 \times B}, \xi_{3} \equiv \frac{1}{\sqrt{A}} << 1.$$
(27)

To determine minimum point, let us set out equation (26) into the form

$$\delta^{2} + 2 \times \theta \times B \times \delta - \theta \times A \times B \times [1 + \Lambda_{1p}(\delta)] = 0,$$
(28)

where absolute value of function

$$\Lambda_{1p}(\delta) = \frac{B + (A + \theta \times B) \times \delta}{\theta \times A \times B \times \delta} - \frac{B}{A \times \delta} + \frac{B \times \delta^3 + (\delta^2 + B)[2 \times B + (A + B) \times \delta]}{\theta \times A \times B \times \delta^6} \times [B + (A + \theta \times B) \times \delta + \theta \times B \times \delta^2 + \delta^3] + \frac{B + A \times \delta - \delta^2}{\theta \times A \times \delta^5} \times \{A + (2 \times \theta - 1) \times B + 4 \times \theta \times B \times \delta + [3 + (A + B) \times \theta] \times \delta^2 - 2(\theta - 1) \times \delta^3\}$$
(29)

is much less than unity at

$$\delta = \delta_{1p}^{(0)} \equiv -\theta \times B + \sqrt{\theta \times B \times (A + \theta \times B)}.$$
(30)

It means that the first root of equation (26) δ_{1p} can be found by the method of successive iterations using $\Lambda_{1p}(\delta_{1p})$ as small parameter. Zeroth-order approximation (30) leads to the formula for concentration of recombination centers $N = N_{1p}$, where dependence $\tau_p(N)$ reaches its minimum $\tilde{\tau}_p$ (Figure 1b):

$$N_{1p} = N_D + 2 \times \theta \times p_t - \sqrt{2 \times \theta \times p_t \times (N_D + 2 \times \theta \times p_t)}.$$
(31)

It follows from this formula that ratio N_{1p}/N_D increases from $\frac{1}{2}$ when $N_D < <2 \times \theta \times p_t$ to $(1-\sqrt{2 \times \theta \times p_t}) \cong 1$ when $N_D >>2 \times \theta \times p_t$ with increased N_D (Figure 3a). Further, it will be demonstrated that extremum, like the maximum of dependence $\tau_p(N)$ as well as $\tau_n(N)$, can occur only at values N closer to N_D . Therefore, in expression for upper limit of value N_{1p} , small correction has been remained, which is primal.

To determine maximum point of dependence $\tau_v(N)$, let us set out equation (26) into the form

$$[1 - \Lambda_{2\nu}(\delta)] \times \delta^2 = A + B, \tag{32}$$

where absolute value of function

$$\Lambda_{2p}(\delta) = \frac{1}{\theta \times \delta^4} \times [A + (2 \times \theta - 1) \times B + 3\delta^2 - 2 \times (\theta - 1) \times \delta^3] + \frac{B + \delta^2}{\theta \times B \times \delta^5} \times [2 \times B + (A + B) \times \delta] \times \left[1 + \frac{\delta \times (\delta + 1) \times (\theta \times B + \delta)}{B + A \times \delta - \delta^2}\right]$$
(33)

is much less than unity at

$$\delta = \delta_{2p}^{(0)} = \sqrt{A + B}.$$
(34)

It means that the second root of equation (26) δ_{2p} can be found by the method of successive iterations using $\Lambda_{2p}(\delta_{2p})$ as small parameter. It follows from relations (20) and (34) that concentration of recombination centers $N = N_{2p}$, where dependence $\tau_p(N)$ reaches its maximum $\hat{\tau}_p$ (Figure 1b), is determined in first-order approximation for small parameter $\Lambda_{2p}(\delta_{2p})$ by expression

$$\frac{N_{2p}}{N_D} = 1 - \frac{1}{A+B} - \frac{\sqrt{A+B}}{A} \times \Lambda_{2p} \times \left(\sqrt{A+B}\right) \cong 1.$$
(35)

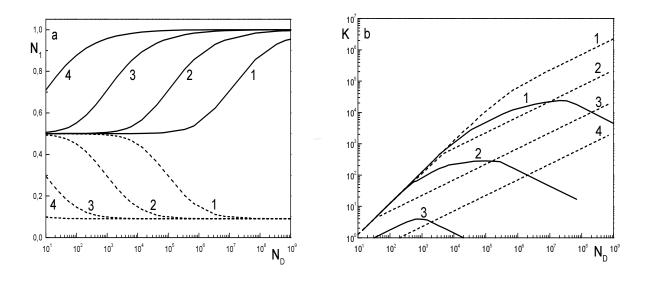


Figure 3. Dependences: point of minimum N_1 of functions $\tau_p(N)$ μ $\tau_n(N)$ (a) and ratio K between maximal to minimal charge carriers' lifetimes (b) on concentration of shallow donors N_D at different locations of recombination level. Solid curves, holes; dashed curves, electrons. Ratio n_t/n_i values: curve 1, 10⁻⁴; curve 2, 10⁻²; curve 3, 1; curve 4, 10². Concentration N_1 is measured in units N_D , concentration N_D in units n_i . Adopted: $\theta = 10^2$

In particular

$$\frac{N_{2p}}{N_{D}} = \begin{cases} 1 - \frac{n_{t}}{2 \times N_{D}} \times \left(1 + \frac{2}{\theta} + \frac{\sqrt{2 \times N_{D} \times n_{t}}}{\theta \times p_{t}}\right), & \text{for} \quad N_{D} \gg 2 \times p_{t} \\ & 1 - \left(\frac{2 \times n_{i}}{N_{D}}\right)^{2}, & \text{for} \quad 2n_{i} \ll N_{D} \ll 2p_{t} \end{cases}$$

$$(36)$$

It follows from (22), (25), (27), (30), and (34) that

$$K_{p}(N_{D}) \equiv \frac{\hat{\tau}_{p}}{\tilde{\tau}_{p}} = \begin{cases} \frac{N_{D}}{8 \times n_{i}}, & \text{for} \quad 8 \times n_{i} << N_{D} << 2 \times p_{t} \\ \sqrt{\frac{N_{D}}{32 \times n_{i}}}, & \text{for} \quad N_{D} << 2\theta \times p_{t} << \theta \times N_{D} \\ \frac{\sqrt{2} \times \theta \times p_{t}}{\sqrt{N_{D} \times n_{t}}}, & \text{for} \quad \sqrt{2 \times N_{D} \times n_{t}} << 2 \times \theta \times p_{t} << N_{D} \\ \approx 1, & \text{for} \quad 2 \times \theta \times p_{t} << \sqrt{2 \times N_{D} \times n_{t}} \end{cases}$$
(37)

Relation (37) shows that function $K_p(N_D)$ is non-monotonic and can vary by several orders of magnitude (Figure 3b). Value

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$$\hat{\tau}_{p} = \left(1 + \frac{\sqrt{2} \times \theta \times p_{t}}{\sqrt{N_{D} \times n_{t} + 2 \times n_{i}^{2}}}\right) \times \left(N_{D} \times w_{p}\right)^{-1}$$
(38)

increases with decreasing recombination level energy E_t (Figure 4a).

The dependence of $\hat{\tau}_p$ on temperature *T* is determined by the location of recombination level in forbidden gap of semiconductor (Figure 4b). Value $\hat{\tau}_p$ decreases with lowering temperature if $E_t \ge E_g/2$ and increases if $E_t \le E_g/3$ (value E_t is measured from top of valence band and E_g is the energy gap of semiconductor). If $E_g/3 < E_t < E_g/2$, then dependence $\hat{\tau}_p$ has maximum value at

$$T = \tilde{T} \equiv \frac{E_t}{k} \times \ln^{-1} \left(2 \times \frac{N_v}{N_D} \times \frac{E_g - 2 \times E_t}{3 \times E_t - E_g} \right), \tag{39}$$

where k is Boltzmann constant and N_v is effective density of states in valance band.

4.2. Mathematical analysis of electron lifetime

The analysis of equation

$$\frac{\partial}{\partial\delta} \times \frac{1}{\tau_n} = 0, \tag{40}$$

which determines extremum points of dependence $\tau_n(N)$, shows that well-defined nonmonotonic behavior of this function occurs at

$$2 \times \xi_3 << 1, \xi_4 = 2 \times \frac{\sqrt{B}}{A} << 1.$$
(41)

To determine minimum point let us set out equation (40) into the form

$$(\theta - 1) \times \delta^{2} - 2 \times \theta \times (A + B) \times \delta + \theta \times A \times (A + B) \times [1 + \Lambda_{1n}(\delta)] = 0,$$
(42)

where absolute value of function

$$\Lambda_{1n}(\delta) = \frac{(\theta - 1) \times B}{\theta \times A \times (A + B)} - \frac{2 \times B + A \times \delta}{\theta \times A \times (A + B) \times \delta} \times \left[\left(1 + \frac{2 \times \theta \times B}{\delta} \right) \times \left(1 + \frac{A + B}{\delta^2} + \frac{2 \times B}{\delta^3} \right) + \frac{1}{\delta} \times \left(A + B + \frac{2 \times B}{\delta} \right) \times \left(\theta \times \frac{A + B}{\delta} - \theta + 1 \right) \right] + \frac{B + A \times \delta - \delta^2}{\theta \times A \times (A + B) \times \delta} \left[2 + (\theta - 1) \times \frac{A + B}{\delta} + \frac{6 \times \theta \times B}{\delta} + \frac{2 \times B}{\delta^2} \times \left(2 \times \theta - 2 - \frac{1}{\delta} \right) \right]$$
(43)

is much less than unity at

$$\delta = \delta_{1n}^{(0)} \equiv \frac{\sqrt{\theta \times (A+B)}}{\theta - 1} \times \left(\sqrt{\theta \times (A+B)} - \sqrt{A+\theta \times B}\right). \tag{44}$$

It means that the first root of equation (40) δ_{1n} can be found by the method of successive iterations using $\Lambda_{1n}(\delta_{1n})$ as small parameter. Zeroth-order approximation (44) leads to the formula for concentration of recombination centers $N = N_{1n}$ where dependence $\tau_n(N)$ reaches its minimum $\check{\tau}_n$:

$$N_{1n} = \frac{\sqrt{N_D + 2 \times \theta \times p_t}}{\theta - 1} \times \left(\sqrt{\theta \times (N_D + 2 \times p_t)} - \sqrt{N_D + 2 \times \theta \times p_t}\right).$$
(45)

It follows, from this formula, that ratio N_{1n}/N_D decreases from ½ when $N_D < <2 \times \theta \times p_t$ to $1/(\sqrt{\theta} + 1)$ when $N_D > >2 \times \theta \times p_t$ with increased N_D (Figure 3a).

We can transform equation (40) to form (32) where $\Lambda_{2p}(\delta)$ will be replaced by function:

$$\Lambda_{2n}(\delta) = \frac{2 \times \delta}{A} + \frac{2 \times B}{A} \times \frac{\theta \times (A+B) \times \delta + 2 \times \theta \times B + \delta}{\theta \times (A+B) \times \delta^4} \times \left(2 \times A + B + \frac{2 \times B}{\delta}\right) + (2 \times \theta \times B + \delta) \times \frac{A \times (A+B+\delta^2) + 2 \times B \times \delta}{\theta \times A \times (A+B) \times \delta^3} - 2 \times \frac{B + A \times \delta - \delta^2}{\theta \times A \times (A+B) \times \delta^4} \times (\delta^3 + 3 \times \theta \times B \times \delta^2 - 2 \times B) - (\theta - 1) \times \frac{2 \times B \times [4 \times B + (4 \times A + B) \times \delta + (\delta - 2) \times \delta^2] + 2 \times A \times (A+B) \times \delta^2}{\theta \times A \times (A+B) \times \delta^4} \right].$$
(46)

At value $\delta = \delta_{2n}$, where dependence $\tau_n(N)$ has its maximum $\hat{\tau}_n$, absolute value $|\Lambda_{2n}(\delta)| <<1$. Therefore, in zeroth-order approximation for small parameter $\Lambda_{2n}(\delta_{2n})$, value $\delta_{2n} = \delta_{2p}^{(0)}$ and concentration $N = N_{1n}$, where $\tau_n(N) = \hat{\tau}_n$ equals to N_D (as for holes). And

$$K_{n}(N_{D}) = \frac{\hat{\tau}_{n}}{\bar{\tau}_{n}} = \begin{cases} \frac{N_{D}}{8 \times n_{i}}, & \text{for } 2 \times n_{i} << N_{D} << 2 \times p_{t} \\ \frac{1}{\kappa} \times \sqrt{\frac{N_{D}}{2 \times n_{t}}}, & \text{for } N_{D} >> 2 \times p_{t} \end{cases}$$

$$(47)$$

where $\kappa = 4$ at $\theta = 1$ and $\kappa = 1$ at $\theta >> 1$. It follows from relation (47) that function $K_n(N_D)$, in contrast to $K_p(N_D)$, grows monotonically with increased N_D and this growth can be many orders of magnitude (Figure 4b).

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Value

$$\hat{\tau}_n = \sqrt{\frac{N_D + 2 \times p_i}{2 \times n_i}} \times \left(N_D \times w_n\right)^{-1} \tag{48}$$

increases, as for $\hat{\tau}_{p}$, with the decrease of recombination level energy (Figure 4a) and, in contrast to $\hat{\tau}_{p}$, always falls with temperature rise (Figure 4b).

4.3. Physical interpretation

Let's explain physical mechanisms of the above regularities.

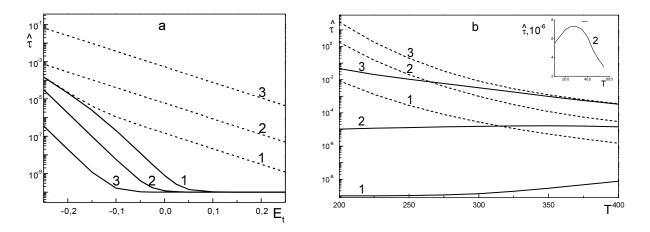


Figure 4. Dependences of maximal lifetime of holes $\hat{\tau}_p(N)$ (solid lines) and electrons $\hat{\tau}_n(N)$ (dashed lines) on recombination level energy E_t (eV) for Ge (1), Si(2), and GaAs (3) at T = 300 K (a) and on temperature T (K) for Si at different values E_t (b): curve 1, 0; curve 2, (-101/152); curve 3, (-3/4). Recombination level energy is reckoned from the middle of forbidden gap. Physical parameters for Ge, Si, and GaAs are obtained from monograph [3]. Adopted: $N_D = 10^{15}$ cm⁻³, $w_n = 10^{-8}$ cm³/s, $\theta = 10^2$

4.3.1. Hole lifetime

Reciprocal hole lifetime

$$\tau_p^{-1} = \tau_{p1}^{-1} + \tau_{p2}^{-1} + \tau_{p3}^{-1} \tag{49}$$

consists of three partial components.

First component

$$\tau_{p1}^{-1} = w_p \times N_-^e = \frac{w_p \times n_t}{2} \times \frac{B + A \times \delta - \delta^2}{\delta}$$
(50)

corresponds to the change of capture rate of holes $\Delta p \times w_p \times N_-^e = \Delta p / \tau_{p1}$ caused only by deviation of hole concentration from its equilibrium value (capture of excess holes Δp at equilibrium trapping centers N_-^e).

Second component

$$\tau_{p2}^{-1} = -w_p \times p_t \times \frac{2}{\delta} \times \frac{(\delta \times \theta - 1) \times (B + A \times \delta - \delta^2)}{A \times \delta + B \times [1 + \delta \times \theta \times (1 + \delta)] + \delta^3}$$
(51)

corresponds to the change of capture rate of holes $p_e \times w_p \times \Delta N_{-} = \Delta p / \tau_{p2}$ caused only by deviation of concentration of hole trapping centers from its equilibrium value (capture of equilibrium holes p_e at nonequilibrium trapping centers ΔN_{-}).

Third component

$$\tau_{p3}^{-1} = \delta \times \tau_{p2}^{-1} \tag{52}$$

corresponds to the change of thermal emission rate of holes from impurity level states into valence band $2 \times p_t \times w_p \times \Delta N_0 = \Delta p / \tau_{p3}$ caused by deviation of concentration of hole generation centers from its equilibrium value (thermal emission of holes from nonequilibrium centers ΔN_0).

Lifetime τ_{p1} can be interpreted as capture time of excess holes by equilibrium traps, lifetime τ_{p2} can be interpreted as relaxation time of excess holes due to capture of equilibrium holes by nonequilibrium traps, and lifetime τ_{p3} can be interpreted as time of thermal emission of holes from nonequilibrium centers.

If conditions (27) are fulfilled and $N < N_D$, then recombination centers are almost completely filled with electrons ($\delta = N_-^e / N_0^e > 1$). For this reason, even if $\theta = w_p / w_n = 1$, capture time of hole τ_{p1} is much shorter than capture time of electron τ_{n1} for the relevant equilibrium trapping centers. In other words, equilibrium traps capture holes much more intensively than electrons. Therefore, the generation of excess free charge carriers initiates the formation of additional nonequilibrium centers of thermal generation of holes and, simultaneously, reducing concentration of trapping centers of electrons ($\Delta N_0 = -\Delta N_->0$). This change of charge state of recombination impurity atoms results in negative values of components $1/\tau_{p2}$ and $1/\tau_{p3}$ in expression (36); moreover $|\tau_{p3}| < |\tau_{p2}|$, because $\delta >>1$ at $N < N_D$. This means that hole lifetime τ_p exceeds capture time of holes τ_{p1} at equilibrium traps due to dominating thermal emission of holes from relevant nonequilibrium centers. As long as $N < N_D$, concentration $N_0^e < N$ of capture centers of electrons still remains low. Therefore, concentration ΔN_0 of nonequilibrium centers of hole thermal emission increases as well. This increase causes faster

decreasing $|\tau_{p3}|$ than decreasing τ_{p1} . As a result, starting with concentration $N = N_{1p}$, the rate of hole thermal emission from nonequilibrium centers and the capture rate of nonequilibrium holes at equilibrium traps become closer to each other. For this reason, τ_p starts to grow (Figure 1b).

When *N* becomes larger than N_D , the concentration N_-^e of equilibrium hole capture centers practically stabilizes, while concentration N_0^e of equilibrium electron capture centers grows with the increase of recombination centers' concentration $(N_-^e \cong N_D, N_0^e \cong N - N_D \text{ at } n_t/2 << N - N_D << N_D^2/2p_t)$. This means that the ratio τ_{p1}/τ_{n1} increases with increasing *N*. For this reason, concentration of nonequilibrium hole thermal emission centers decreases, and concentration of hole traps N_- increases. As a result, $\tau_p(N)$ decreases with increased *N* (Figure 1b). When *N* prevails $N_D^2/2p_t$, the concentration N_-^e of equilibrium hole capture centers grows again with increased *N* due to thermal emission of electrons from valence band to impurity level $(N_-^e \cong \sqrt{2N \times p_t})$. However, concentration of equilibrium capture centers of electrons grows much faster $(N_0^e \cong N)$. Therefore, the decrease of $\tau_p(N)$ continues. As it is seen from (36)-(39), τ_p becomes less than τ_{p1} , when product $\delta \times \theta$ becomes less than unity.

As shown above, minimum point $N = N_{1p}$ of dependence $\tau_p(N)$ shifts toward N_D with growth N_D (Figure 3a). The main reason is that equilibrium electrons are being captured at centers of hole thermal emission and decreased concentration ΔN_0 of these centers. The higher the concentration of equilibrium electrons n_e , the more ΔN_0 decreases. Concentration n_e grows with increased N_D . When N ascends, then n_e descends and N_-^e increases that causes increased ΔN_0 at $N < N_D$. In other words, decreased ΔN_0 with increased N_D is compensated by increased ΔN_0 with increased N. This is the reason why the greater the N_D , the closer the N_{1p} to N_D .

For the same reasons, non-monotonic dependence τ_p on N cancels out, as shown above (Figure 3b), at $N_D > 2 \times (\theta \times p_t)^2 / n_t$ (increased ΔN_0 with increasing N is not able to compensate decreasing ΔN_0 with increasing N_D).

Non-monotonic character of dependence τ_p on N does not occur and at low concentrations N_D (see inequities (27), expressions (22), and Figure 3b), when equilibrium electron population at recombination level is determined mostly by electron-hole transitions between that level and free bands. In this case, values δ cannot provide prevailing growth of hole thermal emission rate from nonequilibrium centers over the growth of capture rate of nonequilibrium holes at equilibrium hole traps with increasing N.

Maximal value of ratio $K_p \equiv \hat{\tau}_p / \tilde{\tau}_p$ is achieved at $N_D \cong 2 \times \theta \times p_t$ and equals to approximately

$$\left(K_{p}\right)_{\max} \cong \sqrt{\frac{\theta \times p_{t}}{n_{t}}}.$$
 (53)

Note that with increasing energy E_t of recombination level, non-monotonicity of dependence $\tau_p(N)$ fades out (Figure 3b) and then cancels out absolutely. This is caused by the increase in concentration n_e of equilibrium electrons and decrease in value δ and fall of the probability of hole thermal emission from recombination level into valence band with increasing energy of recombination level referred to the top of valence band. For the same reason, value $\hat{\tau}_p$ decreases with increasing E_t (Figure 4a).

The character of dependence $\hat{\tau}_p$ on temperature (Figure 4b) is determined by the following dependences on temperature:

$$\delta_{2p}(T) = \frac{1}{n_i(T)} \times \sqrt{2 \times N_D \times p_t(T) + 4 \times p_t^2(T)},\tag{54}$$

$$p_t(T) = N_v \times \exp\left(-\frac{E_t}{kT}\right), n_e(T) = \frac{\delta_{2p}(T) \times n_i^2(T)}{2 \times p_t(T)}.$$
(55)

Values $p_t(T)$ and $n_e(T)$ increase always with temperature T rise. Increased p_t means increasing probability of thermal emission of hole from recombination center into valence band. Therefore, the above-mentioned process facilitates increasing $\hat{\tau}_p$ with T rise. At the same time, growth $n_e(T)$ facilitates decreasing $\hat{\tau}_p$ with T rise due to decreasing concentration of nonequilibrium centers ΔN_0 of hole thermal emission.

Value δ_{2p} decreases with T rise at $E_t \leq E_g/3$ due to approaching N_{2p} closer and closer to N_D (see expression (36)). Value δ_{2p} decreases also at $E_t \geq E_g/2$ up to temperature at which nonmonotonic dependences τ_p and τ_n on N cancel out. Falling δ_{2p} decreases ΔN_0 that facilitates decreasing $\hat{\tau}_p$ with T rise. When $E_t \geq E_g/2$, then $p_t(T)$ increases faster and $\delta_{2p}(T)$ falls and $n_e(T)$ grows. As a result, $\hat{\tau}_p$ increases with temperature rise (Figure 4b). If $E_t \leq E_g/3$, then increased p_t with temperature rise cannot compensate decreased $\delta_{2p}(T)$ and growth $n_e(T)$. As a result, $\hat{\tau}_p$ decreases with temperature rise (Figure 4b). If $E_g/3 < E_t < E_g/2$, then at $T < \tilde{T}$, dependence $\hat{\tau}_p(T)$ will be increasing, and at $T > \tilde{T}$ dependence $\hat{\tau}_p(T)$ will be falling for the same reasons that in previous cases (see expression (39) and insert in Figure 4b).

4.3.2. Electron lifetime

By analogy with hole lifetime, reciprocal electron lifetime consists of three partial components:

$$\tau_n^{-1} = \tau_{n1}^{-1} + \tau_{n2}^{-1} + \tau_{n3}^{-1} \tag{56}$$

First component

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$$\tau_{n1}^{-1} = w_n \times N_0^e = \frac{w_n \times n_t}{2} \times \frac{B + A \times \delta - \delta^2}{\delta^2}$$
(57)

corresponds to the change of electron capture rate $\Delta n \times w_p \times N_0^e = \Delta n / \tau_{n1}$ caused by deviation of electron concentration from equilibrium value (capture of excess electrons Δn on equilibrium traps N_0^e).

Second component

$$\tau_{n2}^{-1} = \frac{w_n \times n_t}{2} \times \frac{(\delta \times \theta - 1) \times (B + A \times \delta - \delta^2)}{\theta \times (B + A \times \delta - \delta^2) + (1 + \delta) \times (\theta \times B + \delta)}$$
(58)

corresponds to the change of electron capture rate $n_e \times w_n \times \Delta N_0 = \Delta n / \tau_{n2}$ caused solely by deviation of concentration of electron capture centers from equilibrium value (capture of equilibrium electrons n_e on nonequilibrium capture centers ΔN_0).

Third component

$$\tau_{n3}^{-1} = (\delta \times \tau_{n2})^{-1} \tag{59}$$

corresponds to the change of thermal emission rate of electrons from impurity level into valence band $(1/2) \times n_t \times w_n \times \Delta N_= -\Delta n / \tau_{n3}$ caused by deviation of concentration of electron thermal emission centers from equilibrium value (thermal emission of electrons from none-quilibrium centers ΔN_{-}).

Times τ_{n1} , τ_{n2} and $(-\tau_{n3})$ have physical sense similar to times τ_{p1} , τ_{p2} and $(-\tau_{p3})$, respectively.

Value $\delta >>1$ as long as $N < N_D$, and hence ratio $\tau_{p1}/\tau_{n1} <<1$. Therefore, the occurrence of excess free charge carriers leads to the formation of additional (nonequilibrium) capture centers of electrons and, at the same time, decrease in concentration ($\Delta N_0 = -\Delta N_->0$) of electrons' generation centers. Partial components $1/\tau_{n2}$ and $1/\tau_{n3}$ are positive values at such change of charge state of recombination centers; moreover $\tau_{n2} < \tau_{n3}$, because of $\delta >1$ at $N < N_D$. It means that, due to preferable capture of equilibrium electrons on nonequilibrium traps, lifetime of electrons τ_n is shorter, than capture time of electrons on equilibrium traps. With further increased N, the number of equilibrium capture centers of holes grows, but the number of equilibrium capture centers of electrons increases. For this reason, starting from concentration $N = N_{1n}$, capture rate of equilibrium electrons on nonequilibrium traps becomes higher than capture rate of nonequilibrium electrons on equilibrium traps becomes higher than capture rate of nonequilibrium electrons on equilibrium traps. In other words, partial component $1/\tau_{n2}$ becomes critical component defining reciprocal lifetime of electrons $1/\tau_n$. Component $1/\tau_{n2}$ falls with growth N due to the decrease in concentration n_e of equilibrium electrons, so $\tau_n \approx \tau_{n2}$ and increases with growth N (Figure 1b).

At values *N* greater than N_D , the ratio τ_{p1}/τ_{n1} increases with increasing *N*. This, again, leads to decreasing concentration of nonequilibrium capture centers of electrons with increasing *N*. Value n_e continues to fall as well. As a result, partial component $1/\tau_{n1}$ becomes critical component defining reciprocal electron lifetime $1/\tau_n$, and therefore, $\tau_n(N)$ falls with increasing *N* (Figure 1b).

As shown above, in contrast to dependence $\tau_p(N)$, ratio N_{1n}/N_D decreases (Figure 3a) and ratio $K_n \equiv \hat{\tau}_n/\tilde{\tau}_n$ always increases monotonically with increasing N_D (Figure 3b). Such regularities are caused by increased n_e with increasing N_D . Because of this, capture rate of equilibrium electrons at nonequilibrium traps becomes greater than capture rate of nonequilibrium electrons at equilibrium traps at lower concentrations ΔN_0 , i.e., at lower values of ratio N/N_D . In contrast to the situation with holes, here, decreasing ΔN_0 with increased N_D is compensated by increasing n_e .

Similar to the behavior of hole lifetime, non-monotonic dependence $\tau_n(N)$ fades gradually and then cancels out (Figure 3b) with decreasing N_D or increasing E_t . First regularity is caused by decreased n_e and $\delta = 2n_e/n_t$ with decreasing N_D . Second regularity is caused by decreasing δ and, hence, ΔN_{0r} , with increasing energy E_t of recombination level. In this case, however, due to growth n_e , non-monotonicity of dependence $\tau_n(N)$ cancels out at larger values E_t than in the case of holes.

Due to decreasing δ_{2n} with increasing E_t , value $\hat{\tau}_n$ decreases as well (Figure 4a). The type of dependence $\hat{\tau}_n$ on temperature (Figure 4b) is determined only by dependence $\delta_{2n}(T)$, because in maximum point $\tau_n = \tau_{n1}/2 \sim 1/N_0^e \sim \delta_{2n}$. In zeroth approximation, $\delta_{2n}(T)$ coincides with $\delta_{2p}(T)$, determined by expression (56). Therefore, $\hat{\tau}_n$ decreases always with temperature rise (Figure 4b).

5. Relation between concentrations of photoholes and photoelectrons outside approximation of quasi-neutrality

Note first, from formulas (10), (11), (20), and (23) follow

$$a_{n} = \frac{\varepsilon}{8\pi \times q} \times \frac{(1+\delta) \times f(\delta) \times w_{p} \times n_{t}}{\theta \times f(\delta) + (1+\delta) \times (\theta \times B + \delta)},$$
(60)

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$$a_{p} = \frac{\varepsilon}{2\pi \times q} \times \frac{(1+\delta^{-1}) \times f(\delta) \times w_{p} \times p_{t}}{B + (A+\theta \times B) \times \delta + (\theta \times B+\delta) \times \delta^{2}}.$$
(61)

Differentiating (12) with respect to x, we obtain

$$\frac{\partial \Delta E}{\partial x} = \frac{1}{q \times \mu_n \times n_e} \times \frac{\partial \Delta I_n}{\partial x} - \frac{E_0}{n_e} \times \frac{\partial \Delta n}{\partial x} - \frac{D_n}{\mu_n n_e} \times \frac{\partial^2 \Delta n}{\partial x^2}.$$
(62)

Recall that $\Delta E \equiv E(x) - E_0$ is the change of electric field intensity caused by deviation of concentrations of free charge carriers and their capture centers from equilibrium values by reason of band-to-band absorption of optical radiation: E(x) and E_0 are electric field intensities with and without illumination.

From equation (16) and formula (5), we find

$$\frac{1}{q} \times \frac{\partial \Delta I_n}{\partial x} = \frac{\Delta n}{\tau_n} + a_n \times \frac{\partial \Delta E}{\partial x} - g.$$
(63)

Eliminating $\frac{1}{q} \times \frac{\partial \Delta I_n}{\partial x}$ from equations (62) and (63), we obtain that

$$\frac{\partial \Delta E}{\partial x} = \frac{1}{1 - \tilde{\xi}_n} \times \left[\frac{1}{\mu_n \times n_e} \times \left(\frac{\Delta n}{\tau_n} - g \right) - \frac{E_0}{n_e} \times \frac{\partial \Delta n}{\partial x} - \frac{D_n}{\mu_n \times n_e} \times \frac{\partial^2 \Delta n}{\partial x^2} \right], \tag{64}$$

where
$$\tilde{\xi}_n = \frac{a_n}{\mu_n \times n_e}$$
. (65)

Eliminating $\frac{\partial \Delta E}{\partial x}$ from equations (7) and (64) and taking into account expressions (23) and (65), we find that relation between concentrations of excess holes Δp and electrons Δn is determined by the following formula:

$$\Delta p = \frac{\tau_p}{\tau_n} \times \Delta n + \chi \times \left(\frac{\tau_p}{\tau_n} \times \Delta n - g \times \tau_p - \mu_n \times \tau_p \times E_0 \times \frac{\partial \Delta n}{\partial x} - D_n \times \tau_p \times \frac{\partial^2 \Delta n}{\partial x^2}\right),\tag{66}$$

where

$$\chi = \frac{a_n + a_p}{\mu_n \times n_t \times \frac{\delta}{2} - a_n}.$$
(67)
In quasi-neutrality approximation $a_n = a_p = 0$; therefore, in this case,

$$\Delta p = \frac{\tau_p}{\tau_n} \times \Delta n.$$
(68)

6. Derivation of equation for distribution function of photoexcited charge carriers' concentration outside quasi-neutrality

From expressions (12)–(14), it follows that

$$\Delta E = \frac{I_{ph} - q \times \left(\mu_n \times \Delta n + \mu_p \times \Delta p\right) \times E_0 + q \times D_p \times \frac{\partial \Delta p}{\partial x} - q \times D_n \times \frac{\partial \Delta n}{\partial x}}{q \times \left(\mu_n \times n_e + \mu_p \times p_e\right)}.$$
(69)

Plugging this expression for intensity ΔE of photoinduced electric field in (12) and taking into account (17), we obtain

$$\Delta I_n = \frac{b \times n_e \times I_{ph}}{b \times n_e + p_e} - \frac{n_e \times \Delta p - p_e \times \Delta n}{b \times n_e + p_e} \times q \times \mu_n \times E_0 + \left(n_e \times \frac{\partial \Delta p}{\partial x} + p_e \times \frac{\partial \Delta n}{\partial x}\right) \times \frac{q \times D_n}{b \times n_e + p_e},\tag{70}$$

where $b = \mu_n / \mu_p = D_n / D_p$. Formulas (17) and (70) allow writing

$$\frac{1}{q} \times \frac{\partial \Delta I_n}{\partial x} = -\frac{n_e \times \frac{\partial \Delta p}{\partial x} - p_e \times \frac{\partial \Delta n}{\partial x}}{b \times n_e + p_e} \times \mu_n \times E_0 + \left(n_e \times \frac{\partial^2 \Delta p}{\partial x^2} + p_e \times \frac{\partial^2 \Delta n}{\partial x^2}\right) \times \frac{D_n}{b \times n_e + p_e}.$$
(71)

Plugging relation (66) between Δp and Δn in (71), we find that

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where

$$\frac{1}{q} \times \frac{\partial \Delta I_n}{\partial x} = -\left(\mu_n^a + \frac{\xi}{1 - \tilde{\xi}_n} \times \frac{\tau_p}{\tau_n} \times \mu_p\right) \times E_0 \times \frac{\partial \Delta n}{\partial x} + \left(D_n^a + \frac{\xi}{1 - \tilde{\xi}_n} \times \left(\tau_p \times \mu_p \times \mu_n \times E_0^2 + \frac{\tau_p}{\tau_n} \times D_p\right)\right) \times \frac{\partial^2 \Delta n}{\partial x^2} + \left(\frac{\xi}{1 - \tilde{\xi}_n} \left(-\tau_p \times \frac{\mu_p}{\mu_n} \times D_n^2 \times \frac{\partial^4 \Delta n}{\partial x^4} + \tau_p \times \mu_p \times E_0 \times \frac{\partial g}{\partial x} - \tau_p \times D_p \times \frac{\partial^2 g}{\partial x^2}\right),$$
(72)

$$D_n^a = \frac{n_e \times \tau_p + p_e \times \tau_n}{(p_e + b \times n_e) \times \tau_n} \times D_n = \frac{\delta^2 \times \tau_p + B \times \tau_n}{(B + b \times \delta^2) \times \tau_n} \times D_n,$$
(73)

$$\mu_n^a = \frac{n_e \times \tau_p - p_e \times \tau_n}{(p_e + b \times n_e) \times \tau_n} \times \mu_n = \frac{\delta^2 \times \tau_p - B \times \tau_n}{(B + b \times \delta^2) \times \tau_n} \times \mu_n.$$
(74)

Formulas (73) and (74) are, none other than, well-known (in quasi-neutrality approximation) expressions for ambipolar diffusion constant D_n^a , and ambipolar mobility μ_n^a of electrons and dimensionless parameter

$$\xi = \frac{a_n + a_p}{\mu_n \times n_e + \mu_p \times p_e} = \frac{2 \times (a_n + a_p) \times \delta}{(\delta^2 \times \mu_n + B \times \mu_p) \times n_t}$$
(75)

is much less than unity (see below). On the other hand, as it follows from equations (63) and (64),

$$\frac{1}{q} \times \frac{\partial \Delta I_n}{\partial x} = \frac{1}{1 - \tilde{\xi}_n} \times \left(\frac{\Delta n}{\tau_n} - g\right) - \frac{\tilde{\xi}_n}{1 - \tilde{\xi}_n} \times \left(\mu_n \times E_0 \times \frac{\partial \Delta n}{\partial x} + D_n \times \frac{\partial^2 \Delta n}{\partial x^2}\right).$$
(76)

Equating (72) and (76), we obtain equation

$$\xi \times D_n \times D_p \times \tau_p \times \frac{\partial^4 \Delta n}{\partial x^4} - \left[\left(1 - \tilde{\xi}_n \right) \times D_n^a + \xi \times \tau_p \times \mu_p \times \mu_n \times E_0^2 + \xi \times \frac{\tau_p}{\tau_n} \times D_p + \tilde{\xi}_n \times D_n \right] \times \frac{\partial^2 \Delta n}{\partial x^2} + \left[\left(1 - \tilde{\xi}_n \right) \times \mu_n^a + \xi \times \frac{\tau_p}{\tau_n} \times \mu_p - \tilde{\xi}_n \times \mu_n \right] \times E_0 \times \frac{\partial \Delta n}{\partial x} + \frac{\Delta n}{\tau_n} = g + \xi \times \tau_p \times \left(\mu_p \times E_0 \times \frac{\partial g}{\partial x} - D_p \times \frac{\partial^2 g}{\partial x^2} \right).$$

$$(77)$$

Because

$$D_{n} - D_{n}^{a} = \frac{b - \tau_{p} / \tau_{n}}{b \times n_{e} + p_{e}} \times n_{e} \times D_{n}, \mu_{n}^{a} + \mu_{n} = \frac{b + \tau_{p} / \tau_{n}}{b \times n_{e} + p_{e}} \times n_{e} \times \mu_{n},$$
(78)

then

$$\left(D_n - D_n^a\right) \times \tilde{\xi}_n + \xi \times \frac{\tau_p}{\tau_n} \times D_p = \xi_n \times D_n + \xi_p \times \frac{\tau_p}{\tau_n} \times D_p,$$

$$\xi \times \frac{\tau_p}{\tau_n} \times \mu_p - \left(\mu_n^a + \mu_n\right) \times \tilde{\xi}_n = \xi_p \times \frac{\tau_p}{\tau_n} \times \mu_p - \xi_n \times \mu_n, \tag{79}$$

where

$$\xi_n = \frac{a_n}{\mu_n n_e + \mu_p p_e} << 1, \xi_p = \xi - \xi_n = \frac{a_p}{\mu_n n_e + \mu_p p_e} << 1.$$
(80)

Therefore, we can rewrite equation (77) as follows:

$$Q \times \frac{\partial^4 \Delta n}{\partial x^4} - D \times \frac{\partial^2 \Delta n}{\partial x^2} + \mu \times E_0 \times \frac{\partial \Delta n}{\partial x} + \frac{\Delta n}{\tau_n} = g + \xi \times \tau_p \times \left(\mu_p \times E_0 \times \frac{\partial g}{\partial x} - D_p \frac{\partial^2 g}{\partial x^2} \right), \tag{81}$$

where

$$D = D_n^a + D_E + D_{\xi}, \mu = \mu_n^a + \mu_{\xi},$$

$$D_E = \xi \times \tau_p \times \mu_p \times \mu_n \times E_0^2,$$
(82)
(83)

$$Q = \xi \times D_n \times D_p \times \tau_p, D_{\xi} = \xi_p \times \frac{\tau_p}{\tau_n} \times D_p + \xi_n \times D_n, \mu_{\xi} = \xi_p \times \frac{\tau_p}{\tau_n} \times \mu_p - \xi_n \times \mu_n.$$
(84)

Equation (81) is the desired equation. It depicts adequately the continuity of electron, hole, and total currents [see (15)-(17)].

7. Solitary Illuminated Sample

In this section, we will consider opportunities for improving photoexcitation of charge carriers and photo-emf V_{vh} by increasing concentration N of recombination centers.

7.1. Preliminaries: Basic relations

We will call the sample as solitary, if it is not in external electric field and external electrical circuit is open.

For simplicity, we will characterize effectiveness of charge carriers' photoexcitation by lightpropagation-length averaged concentrations of photoelectrons $<\Delta n>$ and photoholes $<\Delta p>$ (Figure 5).

Figures 6 and 7 show calculated dependences $\langle \Delta n \rangle (N)$ and $V_{ph}(N)$.

We have not used in study quasi-neutrality approximation [2-9, 13, 18, 21, 22, 28-31] because it can lead to unacceptable errors in calculation of dependences $<\Delta n > (N)$, $<\Delta p > (N)$ (Figures 8 and 9), and $V_{ph}(N)$ (Figures 10 and 11) due to the fundamental contribution of photoexcited space charge into photoelectric effects in semiconductors. In other words, even in solitary sample, photoexcited electron-hole plasma in semiconductor may not always be quasi-neutral.

Let's consider a homogeneous semiconductor sample (Figure 5) with no voltage applied, i.e., in absence of illumination and intensity of electric field $E_0=0$. The density of photogeneration rate of charge carriers, in view of multiple internal reflections, is determined by the following expression:

$$g(x) = \gamma \times \left[a_{-} \times \exp(-\gamma x) + a_{+} \times \exp(\gamma x) \right],$$
(85)

in which

$$a_{-} = \frac{(1-R) \times F_{0}}{1-R^{2} \times \exp(-2\gamma \tilde{W})}, a_{+} = a_{-} \times R \times \exp(-2\gamma \tilde{W}),$$
(86)

where *R* and γ are coefficients of light reflection and absorption, F_0 is density of incident photon flux, and \widetilde{W} is sample thickness along incident light direction (Figure 5a). As is clear from (66) and (81), in discussed conditions, relation between concentrations of excess holes Δp and electrons Δn is as follows:

$$\Delta p = \frac{\tau_p}{\tau_n} \times \Delta n + \chi \times \left(\frac{\tau_p}{\tau_n} \times \Delta n - g \times \tau_p - D_n \times \tau_p \times \frac{\partial^2 \Delta n}{\partial x^2}\right),\tag{87}$$

and function $\Delta n(x)$ obeys the equation

$$Q \times \frac{\partial^4 \Delta n}{\partial x^4} - D \times \frac{\partial^2 \Delta n}{\partial x^2} + \frac{\Delta n}{\tau_n} = g(x) - \xi \times \tau_p \times D_p \times \frac{\partial^2 g}{\partial x^2},$$
(88)

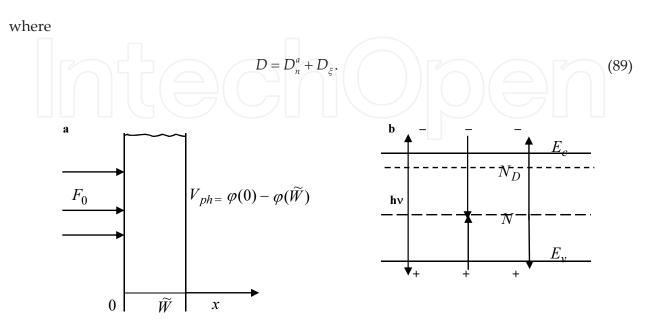


Figure 5. Layout of sample illumination (**a**) and generation-recombination processes in semiconductor (**b**). F_{0} , density of incident photon flux; V_{ph} , photo-emf; $\phi(x)$, electric potential; \widetilde{W} , thickness of sample along light propagation; E_c and E_v , energy of conduction band bottom and valence band top

Denote: τ_n and τ_p are electron (24) and hole (25) lifetimes; $D_{n,p}$ are their diffusion constants and values D_n^a , D_{ξ} and Q and dimensionless parameters χ and $\xi <<1$ are determined by expressions (73), (84), (67), and (75), respectively.

Exact solution of equation (88) is

$$\Delta n(x) = \sum_{i=1}^{4} C_i \times \exp(k_i \times x) + T_n \times g(x), \tag{90}$$

where

$$k_{1,2} = \sqrt{\frac{L^2 - \sqrt{L^4 \mp 4 \times \xi \times L_n^2 \times L_p^2}}{2 \times \xi \times L_n^2 \times L_p^2}}, k_3 = -k_1, k_4 = -k_2,$$
(91)

$$T_{n} = \frac{\left(\frac{1}{\xi \times L_{p}^{2}}\right) - \gamma^{2}}{D_{n} \times (\gamma^{2} - k_{1}^{2}) \times (\gamma^{2} - k_{2}^{2})},$$
(92)

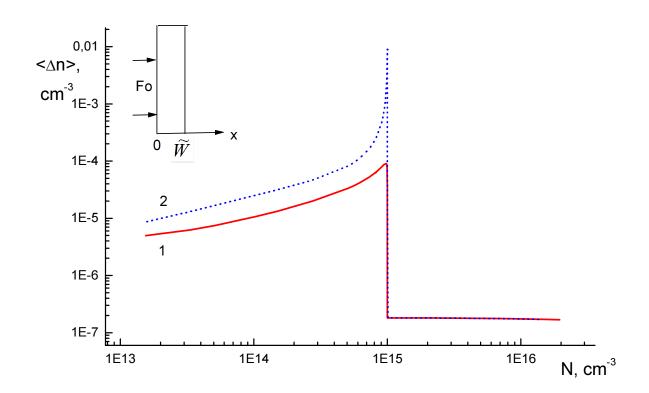


Figure 6. Dependences of mean concentration of photoelectrons $<\Delta n >$ in *GaAs* for levels with energy (eV): $E_t = E_{t1} = -0.42$ (curve 1) and $E_t = E_{t2} = -0.24$ (curve 2) on concentration of recombination impurity N; layout of sample illumination and axis x are shown on insert. Adopted: light absorption coefficient $\gamma = 10^4$ cm⁻¹, diffusion constants of electrons $D_n = 221$ cm³/s and holes $D_p = 10.4$ cm³/s [2-9]; $\widetilde{W} = 10^{-3}$ cm; $F_0 = 1$ cm⁻²×s⁻¹; T = 300 K; concentration of shallow donors $N_D = 10^{15}$ cm⁻³; $\theta = w_p / w_n = 10^2$, $w_n = 10^{-8}$ cm³/s [1-9], where w_p and w_n are capture probabilities of hole and electron

$$L^{2} = L_{a}^{2} + \xi_{n} \times L_{n}^{2} + \xi_{p} \times L_{p}^{2},$$
(93)

$$L_a^2 = \frac{p_e \times L_n^2 + b \times n_e \times L_p^2}{p + b \times n_e} = \frac{B \times \tau_n + \delta^2 \times \tau_p}{B + b \times \delta^2} \times D_n \equiv D_n^a \times \tau_n = D_p^a \times \tau_p, \tag{94}$$

 $L_n = \sqrt{D_n \times \tau_n}$ and $L_p = \sqrt{D_p \times \tau_p}$ are electron and hole diffusion lengths, D_p^a is quasi-neutral ambipolar hole diffusion constant, and L_a is quasi-neutral ambipolar diffusion length of charge carriers.

In quasi-neutrality approximation, parameters ξ , ξ_n and ξ_p are equal to zero; therefore, in this approximation, the distribution of excess electrons' concentration is determined by equation

$$D_n^a \times \frac{\partial^2 \Delta n}{\partial x^2} - \frac{\Delta n}{\tau_n} = -g(x).$$
⁽⁹⁵⁾

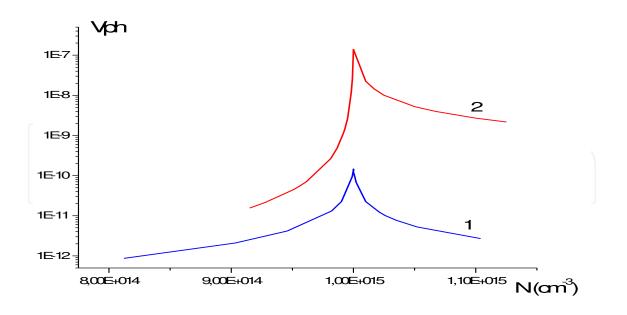


Figure 7. Dependence of photo-emf V_{ph} (arbitrary units) in *GaAs* for levels with energy E_{t1} (curve 1) and E_{t2} (curve 2) on concentration of recombination impurity *N*. Parameters are the same as in Figure 6

7.2. Effectiveness of charge carriers' photoexcitation

We define the mean value $\langle y \rangle$ of variable y(x) as

$$\langle y \rangle = \frac{1}{\tilde{W}} \int_{0}^{\tilde{W}} y(x) dx.$$
(96)

Let's analyze the worst case, when recombination of excess charge carriers on illuminated (x=0) and unilluminated ($x=\widetilde{W}$) surfaces of the sample (Figure 5a) is so intensive that

$$\Delta n(0) = \Delta p(0) = \Delta n(\tilde{W}) = \Delta p(\tilde{W}) = 0.$$
From (87), (90), and (97), it follows that
$$(97)$$

$$\Delta n(x) = \Delta n_1(x) + \Delta n_2(x) + T_n \times g(x),$$
⁽⁹⁸⁾

$$\Delta n_1(x) = \frac{k_1^2 \times (L_n^2 \times k_2^2 - 1)}{D_n \times (k_2^2 - k_1^2) \times (\gamma^2 - K_1^2)} \times \frac{g(0) \times sh[k_1 \times (\tilde{W} - x)] + g(\tilde{W}) \times sh(k_1 \times x)}{sh(k_1 \times \tilde{W})},$$
(99)

$$\Delta n_2(x) = -\frac{k_2^2 \times (L_n^2 \times k_1^2 - 1)}{D_n \times (k_2^2 - k_1^2) \times (\gamma^2 - k_2^2)} \times \frac{g(0) \times sh[k_2 \times (\tilde{W} - x)] + g(\tilde{W}) \times sh(k_2 \times x)}{sh(k_2 \times \tilde{W})},$$
(100)

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$$\Delta p(x) = \frac{\tau_p}{\tau_n} \times \Delta n(x) - \frac{\tau_p}{\tau_n} \times \chi \times \frac{(L_n^2 \times k_1^2 - 1) \times (L_n^2 \times k_2^2 - 1)}{D_n} \times \left\{ \frac{A_1 + A_2}{k_2^2 - k_1^2} + \frac{\gamma^2 \times g(x)}{(\gamma^2 - k_1^2) \times (\gamma^2 - k_2^2)} \right\}$$
where
$$A_1 = \frac{k_1^2}{\gamma^2 - k_1^2} \times \frac{g(o) \times sh[k_1 \times (\tilde{W} - x)] + g(\tilde{W}) \times sh(k_1 \times x)}{sh(k_1 \times \tilde{W})},$$
(101)

$$A_{2} = -\frac{k_{2}^{2}}{\gamma^{2} - k_{2}^{2}} \times \frac{g(o) \times sh[k_{2} \times (\tilde{W} - x)] + g(\tilde{W}) \times sh(k_{2} \times x)}{sh(k_{2} \times \tilde{W})}.$$
(103)

Thus, according to definition (96), we find

$$<\Delta n >= \eta_n \times \langle g \rangle, \langle \Delta p \rangle = \eta_p \times \langle g \rangle, \tag{104}$$

where

$$\eta_{n} = T_{n} + \frac{\gamma \times cth(\gamma \times \tilde{W}/2)}{(k_{2}^{2} - k_{1}^{2}) \times D_{n}} \times \sum_{i=1}^{2} (-1)^{i-1} \times \frac{k_{i} \times \alpha_{3-i}}{\gamma^{2} - k_{i}^{2}} \times th\left(\frac{k_{i} \times \tilde{W}}{2}\right),$$
(105)

$$\alpha_{1,2} = k_{1,2}^{2} \times L_{n}^{2} - 1,$$
(106)
$$< g >= \frac{(1 - R) \times F_{0}}{W} \times \frac{1 - \exp(-\gamma \times \tilde{W})}{1 - R \times \exp(-\gamma \times \tilde{W})},$$
(107)

$$\eta_p = \frac{4\pi}{\varepsilon} \times (a_n + a_p) \times \tau_p \times \eta_\rho + \frac{\tau_p}{\tau_n} \times \eta_n, \qquad (108)$$

$$\eta_{\rho} = -\frac{\varepsilon}{4\pi} \times \frac{\gamma \times \alpha_1 \times \alpha_2}{(\mu_n \times n_e - a_n) \times L_n^2} \times \left\{ \Lambda^3 - \frac{\operatorname{cth}(\gamma \times \tilde{W}/2)}{k_2^2 - k_1^2} \times \sum_{i=1}^2 (-1)^i \times \frac{k_i}{\gamma^2 - k_i^2} \times \operatorname{th}\left(\frac{k_i \times \tilde{W}}{2}\right) \right\} \equiv \frac{\langle \Delta \rho \rangle}{\langle g \rangle}, \quad (109)$$

$$\Lambda^{3} = \frac{\gamma}{(\gamma^{2} - k_{1}^{2})(\gamma^{2} - k_{2}^{2})},$$
(110)

and $\Delta \rho$ is photoexcited space charge density.

Outside quasi-neutrality approximation, expressions (20)–(25), (60), (61), (75), (80), (91)–(94), and (104)–(110) determine, in parametric form (value $\delta = N_{-}^{e}/N_{0}^{e}$ is used as parameter), dependences $\langle \Delta n \rangle \langle N \rangle$ and $\langle \Delta p \rangle \langle N \rangle$. We will call found dependences (see Figures 6, 8, and 9) as exact, because, in linear approximation with respect to F_{0} , dependences are exact in contrast to quasi-neutrality approximation case.

Denote desired dependences in quasi-neutrality approximation as $<\Delta \tilde{p}(N)>$ and $<\Delta \tilde{p}(N)>$. In quasi-neutrality approximation,

$$\Delta n(x) = \Delta \tilde{n} \equiv \frac{\tau_n}{1 - \gamma^2 \times L_a^2} \times \left\{ g(x) - \frac{g(0) \times sh[(\tilde{W} - x) / L_a] + g(\tilde{W}) \times sh(x / L_a)}{sh(\tilde{W} / L_a)} \right\},\tag{111}$$

$$<\Delta p>=<\Delta \tilde{p}>\equiv<\Delta \tilde{n}>\times \frac{\tau_p}{\tau_n},$$
(112)

$$<\Delta n> = <\Delta \tilde{n} > \equiv \frac{(1-R) \times F_0 \times \tau_n}{(1-\gamma^2 \times L_a^2) \times \tilde{W}} \times \frac{1-\exp(-\gamma \tilde{W}) - \gamma \times L_a \times \left[1+\exp(-\gamma \tilde{W})\right] \times th(\tilde{W}/2L_a)}{1-R \times \exp(-\gamma \tilde{W})}.$$
 (113)

Figure 6 shows that the effectiveness of charge carriers' photoexcitation may grow significantly with increasing *N*. Up to small corrections, dependences $<\Delta n > (N)$ and $<\Delta p > (N)$ reach maximums $<\Delta n >_{max}$ and $<\Delta p >_{max}$ at the same concentration $N = N = N_D$ as for lifetimes (Figure 1b) and after that fall very strongly. Figures 8 and 9 illustrate the influence of photoexcited space charge in point N = N on the validity of results. It is clear from Figures 8 and 9 that with thinning \widetilde{W} of sample, using quasi-neutrality approximation leads to error up to several orders of magnitude. Let's clarify Figures 6, 8, and 9.

Lengths L and $L_1 = 1/k_1$, up to small corrections, equal to L_a ; moreover

$$L_n > L_1 > L_2 \equiv \frac{1}{k_2}.$$
 (114)

At $\widetilde{W} < < L_{a'}$ we have

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$$<\Delta \tilde{n} >= \frac{\psi(\tilde{W}, \gamma)}{D_n^a}, <\Delta \tilde{p} >= \frac{\psi(\tilde{W}, \gamma)}{D_p^a},$$
(115)

where function $\psi(\widetilde{W}, \gamma)$ is independent on τ_n and τ_p . On the other hand, if inequality $\widetilde{W} << L_2$ is sufficiently strong, and when $L_p >> \widetilde{W}$ as well, from expressions (104), (105), and (108)–(110), it follows that

$$<\Delta n>=\frac{\psi(\tilde{W},\gamma)}{D_n}, <\Delta p>=\frac{\psi(\tilde{W},\gamma)}{D_p}.$$
(116)

This means that diffusion of photoelectrons and photoholes is independent from each other. Therefore, L_2 has physical meaning as shielding length of photoinduced space charge.

Length $L_2 << L_a$, \widetilde{W} in the vicinity of the point $N = \hat{N}$, i.e. quasi-neutrality is valid. At values $\hat{N} < \hat{N}$, length $L_a < \widetilde{W}$ due to small value D_n^a . When N passing through the point \hat{N} toward larger values N, then D_n^a increases very strongly (by several orders of magnitude), and after that it is remaining substantially constant. As a result, length $L_a > \widetilde{W}$ at values N higher \hat{N} . This explains the asymmetry of dependence $<\Delta n > (N)$ about point $N = \hat{N}$, and "plateau," when N > N as well (Figure 6).

At point N = N and about it, length L_2 is so long that even at $\widetilde{W} \sim 0.1$ cm, solution in quasineutrality approximation is unacceptable; moreover, with decreasing \widetilde{W}

and

$$\frac{\langle \Delta n \rangle_{\max}}{\langle \Delta \tilde{n} \rangle_{\max}} \rightarrow \frac{D_n^a}{D_n} \ll 1, \qquad (117)$$

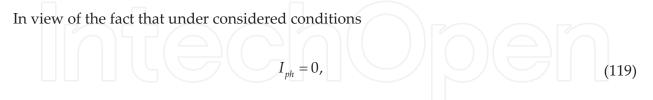
$$\frac{\langle \Delta p \rangle_{\max}}{\langle \Delta n \rangle_{\max}} \rightarrow \frac{D_n}{D_p} \cong 20, \qquad (118)$$

despite the fact that $\tau_p << \tau_n$ (Figure 1b).

When $\gamma^{-1} << \widetilde{W}$ and inequity $\widetilde{W} << L_n$ are sufficiently strong, then the total quantity of photoelectrons is proportional to \widetilde{W} due to reducing loss on unilluminated surface. Therefore, there is a "plateau" on dependence $<\Delta n >_{max}$ on \widetilde{W} . For the same reason, at $\gamma^{-1} << \widetilde{W} << L_{a'}$ dependence $<\Delta n >_{max}$ on \widetilde{W} has a "plateau" as well. However, in the last case, "plateau" height is much higher, and its width is much wider than true "plateau" (Figure 8, curve 1).

Moreover, shielding length of photoinduced space charge $L_2 \approx L_a$ when impurity level energy equals to E_{t2} . Therefore, solution obtained in quasi-neutrality approximation, even when $\widetilde{W} \rightarrow \infty$, differs from exact solution at least by several times (Figures 8 and 9, curve 2).

7.3. Effectiveness of photo-emf excitation



from expressions (12)–(14) and (87), we obtain that photo-emf

$$V_{ph} = \int_{0}^{\tilde{W}} \Delta E(x) dx = \phi(0) - \phi(\tilde{W}), \qquad (120)$$

i.e. potential $\phi(x)$ of illuminated surface with respect to unilluminated (Figure 5a) expressed by formula

$$V_{ph} = \frac{D_n \times \Delta_n - D_p \times \Delta_p}{\mu_n \times n_e + \mu_p \times n_e} = \frac{(L_n^2 - L_p^2) \times \Delta_n + \chi \times L_p^2 \times (\tau_n \times \Delta_g + L_n^2 \times \Delta_n'' - \Delta_n)}{(\mu_n \times n_e + \mu_p \times n_e) \times \tau_n},$$
(121)

where

$$\Delta_n = \Delta n(0) - \Delta n(\tilde{W}), \Delta_p = \Delta p(0) - \Delta p(\tilde{W}), \qquad (122)$$

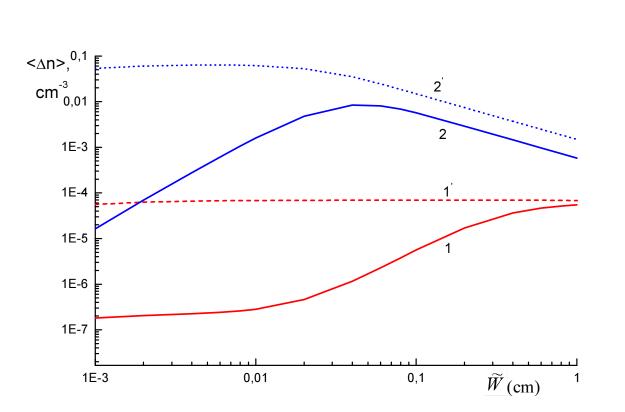
$$\Delta_{g} = g(0) - g(\tilde{W}), \Delta_{n}'' = \frac{\partial^{2} \Delta n}{\partial x^{2}} \bigg|_{x=0} - \frac{\partial^{2} \Delta n}{\partial x^{2}} \bigg|_{x=\tilde{W}}.$$
(123)

It is clear from expression (121) that at infinite surface recombination rate, i.e., when conditions (97) are fulfilled, illumination produces no photo-emf. In this regard, assume that photoexcited charge carriers are not captured on surfaces and there is no charge on surfaces. In these conditions, photoexcited electric field intensity

$$\Delta E(0) = \Delta E(\tilde{W}) = 0 \tag{124}$$

And densities of electron ΔI_n and hole ΔI_p photocurrents

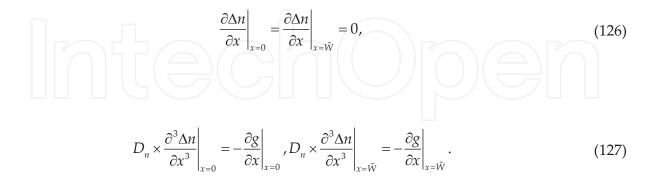
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$$\Delta I_n(0) = \Delta I_v(0) = \Delta I_n(W) = \Delta I_v(W) = 0.$$
(125)

Figure 8. Dependences of $\langle \Delta n \rangle_{max}$ in the point of maximum functions $\langle \Delta n \rangle(N)$ and $\langle \Delta p \rangle(N)$ on thickness \widetilde{W} for *GaAs*. Curves 1 and 2, recombination level energy E_t equals to E_{t1} and E_{t2} , respectively; solid lines - exact solutions; dashed lines - solutions in approximation of quasi-neutrality. Adopted parameters and other symbols are the same as in Figure 6

Therefore, we may write boundary conditions, in view of relation (87), as



From (85), (86), (90), (126), and (127), it follows that

$$C_{1,2} = (-1)^{2,1} \times b_{1,2} \times \frac{g'_0 \times \exp(-k_{1,2} \times \tilde{W}) - g'_{\tilde{W}}}{2 \times sh(k_{1,2} \times \tilde{W})},$$
(128)

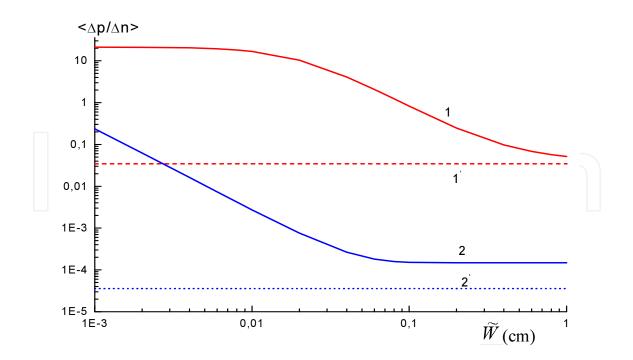


Figure 9. Dependences of ratio $\langle \Delta p \rangle_{max} / \langle \Delta n \rangle_{max}$ in the point of maximum functions $\langle \Delta n \rangle(N)$ and $\langle \Delta p \rangle(N)$ on thickness \widetilde{W} for *GaAs*. Curves 1 and 2, recombination level energy E_t equals to E_{t1} and $E_{t2'}$ respectively; solid lines - exact solutions; dashed lines - solutions in approximation of quasi-neutrality. Adopted parameters and other symbols are the same as in Figure 6

$$C_{3,4} = C_{1,2} \times \frac{g'_0 \times \exp(k_{1,2} \times \tilde{W}) - g'_{\tilde{W}}}{g'_0 \times \exp(-k_{1,2} \times \tilde{W}) - g'_{\tilde{W}}},$$
(129)

where

$$b_{1,2} = \frac{k_{1,2} \times (k_{2,1}^{2} \times L_{n}^{2} - 1)}{D_{n} \times (k_{2}^{2} - k_{1}^{2}) \times (k_{1,2}^{2} - \gamma^{2})'}$$

$$g_{0}' = \frac{\partial g}{\partial x}\Big|_{x=0} = -\gamma^{2} \times a_{-} \times [1 - R \times \exp(-2\gamma \tilde{W})],$$
(130)
(131)

$$g'_{\tilde{W}} = \frac{\partial g}{\partial x}\Big|_{x=\tilde{W}} = \frac{(1-R) \times \exp(-\gamma \tilde{W})}{1-R \times \exp(-2\gamma \tilde{W})} \times g'_{0}.$$
(132)

Find consistently

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$$\Delta n(0) = T_n \times g_0 + \sum_{i=1}^2 (-1)^{i+1} b_i \times [g'_0 \times cth(k_i \times \tilde{W}) - g'_{\tilde{W}} \times \cos ech(k_i \times \tilde{W})],$$
(133)

$$\Delta n(\tilde{W}) = T_n \times g_{\tilde{W}} + \sum_{i=1}^2 (-1)^{i+1} b_i \times [g'_0 \times \cos ech(k_i \times \tilde{W}) - g'_{\tilde{W}} \times cth(k_i \times \tilde{W})],$$
(134)

where

$$g_0 \equiv g(0) = \gamma \times a_- \times [1 + R \times \exp(-2\gamma \tilde{W})], g_{\tilde{W}} \equiv g(\tilde{W}) = \frac{(1 + R) \times \exp(-\gamma \tilde{W})}{1 + R \times \exp(-2\gamma \tilde{W})} \times g_0.$$
(135)

$$\Delta_n = T_n \times \Delta_g + \sum_{i=1}^2 (-1)^{i+1} \times b_i \times th\left(\frac{k_i \times \tilde{W}}{2}\right) \times \Sigma'_g,$$
(136)

$$\Delta_n'' = \gamma^2 \times T_n \times \Delta_g + \sum_{i=1}^2 (-1)^{i+1} \times k_i^2 \times b_i \times th\left(\frac{k_i \times \tilde{W}}{2}\right) \times \Sigma_g', \tag{137}$$

where

$$\Delta_g = g(0) - g(\tilde{W}) = \gamma \times F_0 \times (1 - R) \times \frac{1 - \exp(-\gamma \tilde{W})}{1 + R \times \exp(-\gamma \tilde{W})},$$
(138)

$$\Sigma'_{g} = g'_{0} + g'_{\tilde{W}} = -\gamma^{2} \times F_{0} \times (1 - R) \times \frac{1 + \exp(-\gamma \tilde{W})}{1 + R \times \exp(-\gamma \tilde{W})}.$$
(139)
If we utilize relation

$$Z \equiv L_n^2 - L_p^2 - \chi \times L_p^2 \times (k_1^2 \times L_n^2 - 1) \times (k_2^2 \times L_n^2 - 1) = 0,$$
(140)

then expressions (121) and (136)–(139) allow us to obtain

$$V_{ph} = \frac{(1-R) \times \gamma \times F_0 \times (L_n^2 - L_p^2)}{\mu_n \times n_e + \mu_p \times p_e} \times M,$$
(141)

where

$$M = \frac{k_1^2 \times k_2^2 \times f_{-}(\gamma \tilde{W})}{(k_1^2 - \gamma^2) \times (k_2^2 - \gamma^2)} + \frac{\gamma \times k_1 \times k_2}{k_2^2 - k_1^2} \times \left[\frac{k_1 \times th(k_2 \times \tilde{W}/2)}{k_2^2 - \gamma^2} - \frac{k_2 \times th(k_1 \times \tilde{W}/2)}{k_1^2 - \gamma^2}\right] \times f_{+}(\gamma \tilde{W}), \quad (142)$$

$$f_{-,+}(\gamma \tilde{W}) = \frac{1 \mp \exp(-\gamma \tilde{W})}{1 + R \times \exp(-\gamma \tilde{W})}.$$
(143)

In quasi-neutrality approximation, we get

$$V_{ph} = \tilde{V} \equiv \frac{(1-R) \times \gamma \times F_0 \times (L_n^2 - L_p^2)}{\mu_n \times n_e + \mu_p \times p_e} \times \tilde{M},$$
(144)

where

$$\tilde{M} = \frac{\gamma \times L_a \times f_+(\gamma \tilde{W}) \times th(\tilde{W} / 2L_a) - f_-(\gamma \tilde{W})}{(\gamma \times L_a)^2 - 1}.$$
(145)

We refer to the dependences (141) of photo-emf V_{ph} on N and \widetilde{W} as exact. The reason is that, in contrast to the case of quasi-neutrality approximation, said dependences are exact in linear approximation with respect to flux density F_0 .

Figures 7, 10, and 11 show these dependences and solution in quasi-neutrality approximation as well. It is clear in Figures 10 and 11 that, in quasi-neutrality approximation, maximal value $V_{ph}(N)$ far exceeds the "true" value; moreover, exceedance may be several orders of magnitude.

We can explain results by the fact that very long shielding length (114) of photoexcited space charge L_2 in the point of maximum $N = N \equiv N_D$ and nearby will cause diffusion of photoelectrons independently on photoholes (see Section 6.2) at $\widetilde{W} \sim 0.1$ cm. In other words, electron diffusion constant D_n determines the distribution of photoelectron concentration $\Delta n(x)$. Aside from that, at $N \cong N$, due to charge coupled to impurities, inequity $D_n >> D_n^a$ is fulfilled. It means that true effectiveness of photoelectrons' spreading is much higher, than that given by quasineutrality approximation. Therefore, ratio $(V_{ph})_{max}/(\widetilde{V}_{ph})_{max} <<1$, when $\widetilde{W} >> L_2$ (Figure 11).

Evidently, with thinning \widetilde{W} , spreading area of photoexcited charge carriers becomes wider, i.e., values $\Delta_n = \Delta n(0) - \Delta n(\widetilde{W})$ $\mu \Delta_p = \Delta p(0) - \Delta p(\widetilde{W})$ decrease. Therefore, values $(V_{ph})_{max}$ and $(\widetilde{V}_{ph})_{max}$ fall with thinning \widetilde{W} (Figure 10).

Note that for impurity level energy equal to E_{t2} , the solution obtained in quasi-neutrality approximation, even when $\widetilde{W} \rightarrow \infty$, differs from the exact solution more than two times (Figure 10). This is due to the fact that in considered case the shielding length of photoexcited space charge $L_2=1/k_2\approx L_{a'}$ where L_a is ambipolar diffusion length of charge carriers.

8. Photoelectric gain

We will consider uniform spatial distribution of density of charge carriers' photoexcitation rate *g* and ignore surface recombination of photoexcited charge carriers.

We will facilitate mathematical description of photoelectric gain (see Figures 1a and 2)

$$G(N,V) \equiv \frac{I_{ph}}{q \times W \times g}$$
(146)

through utilizing small dimensionless parameter (75) $\xi <<1$, which will characterize the degree of deviation of semiconductor from local neutrality under illumination. Here *N* is concentration of recombination centers; I_{ph} is photocurrent density (14); *q* is absolute value of electron charge; *V* is bias voltage applied across the sample; *W* is distance between current electrodes (see insert in Figure 1a).

Using linearized expressions for electron (12) and hole (13) components of photocurrent I_{ph} and expressions (60) and (61), we may rewrite equations (5)–(7) as follows:

where

$$R_{n} = \frac{\Delta n}{\tau_{n}} - \xi_{n} \times \frac{\partial j}{\partial x}, R_{p} = \frac{\Delta p}{\tau_{p}} + \xi_{p} \times \frac{\partial j}{\partial x}, \Delta p = \frac{\tau_{p}}{\tau_{n}} \times \Delta n - \xi \times \tau_{p} \times \frac{\partial j}{\partial x}, \qquad (147)$$

$$j = (\mu_{n} \times \Delta n + \mu_{p} \times \Delta p) \times E_{0} + D_{n} \times \frac{\partial \Delta n}{\partial x} - D_{p} \times \frac{\partial \Delta p}{\partial x}, \qquad (148)$$

 $E_0 = V / W$, and dimensionless small parameters $\xi_n <<1$ and $\xi_p <<1$ as defined in (80). Relations (147) show that, by dimensionless small parameter ξ , we may really characterize the degree of deviation of semiconductor from local neutrality under illumination. If there is no external load (inset in Figure 1a), then illumination does not change voltage *V* across the sample.

Therefore, expressions (4), (5), (8), and (9) with boundary conditions (1) allow us to write

$$I_{ph} = \left\{ \left(b + \frac{\tau_p}{\tau_n} \right) \times \left\langle \Delta n \right\rangle + \xi \times \frac{L_p^2}{W} \times \left(\frac{\partial \Delta p}{\partial x} - b \times \frac{\partial \Delta n}{\partial x} \right) \Big|_{x=0}^{x=W} \right\} \times q \times \mu_p \times E_0, \tag{149}$$

where $\langle n \rangle$ is arithmetic mean with respect to *x* concentration of excess electrons (insert in Figure 1a)

$$\left\langle \Delta n \right\rangle = \frac{1}{W} \times \int_{0}^{W} \Delta n(x) dx, \tag{150}$$
$$b = \mu_n / \mu_p.$$

Actual distribution $\Delta n(x)$ at g(x)=const is defined by equation

$$Q \times \frac{\partial^4 \Delta n}{\partial x^4} - (D_n^a + D_E + D_{\xi}) \times \frac{\partial^2 \Delta n}{\partial x^2} + (\mu_n^a + \mu_{\xi}) \times E_0 \times \frac{\partial \Delta n}{\partial x} + \frac{\Delta n}{\tau_n} = g.$$
(151)

Values of parameters Q, D_{ξ} , μ_{ξ} , and D_E are dictated by photoexcitation of space charge $\Delta \rho$ (4). Analysis shows that inequality $\xi <<1$, which is typically fulfilled with large margin, allowing to omit in equation (151) terms with parameters Q, D_{ξ} and μ_{ξ} . However, term with parameter D_E must be retained, because, even at moderate electric fields, D_E may exceed D_n^a due to squarelaw dependence D_E on E_0 . For the same reason, we can omit in equation (149) terms including small parameter ξ . Thus, we arrive at relations

$$(D_n^a + D_E) \times \frac{\partial^2 \Delta n}{\partial x^2} - \mu_n^a \times E_0 \times \frac{\partial \Delta n}{\partial x} - \frac{\Delta n}{\tau_n} + g = 0,$$
(152)
$$I_{ph} = q \times \left(\mu_n + \frac{\tau_p}{\tau_n} \times \mu_p\right) \times \left\langle \Delta n \right\rangle \times E_0.$$
(153)

Equation (152), with boundary condition (1), and relation (153) allow us to obtain the formula for photoelectric gain:

$$G = \left(\mu_n \times \tau_n + \mu_p \times \tau_p\right) \times \frac{E_0}{W} \times \left\{1 - 4 \times \frac{L_{ef}}{W} \times \sqrt{\left(\frac{d_a}{2L_{ef}}\right)^2 + 1} \times \frac{sh\left(\frac{W}{2L_1}\right) \times sh\left(\frac{W}{2L_2}\right)}{sh\left(\frac{W}{2L_1} + \frac{W}{2L_2}\right)}\right\},\tag{154}$$

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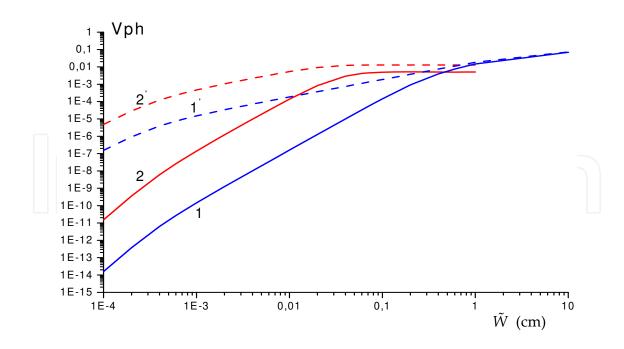


Figure 10. Dependences of maximal value $V_{ph}(N)$ in *GaAs* on thickness \widetilde{W} . Curves 1 and 2, recombination level energy E_t equals to E_{t1} and E_{t2} , respectively; solid curves, exact solutions; dashed curves, solutions in approximation of quasi-neutrality. Adopted parameters and other symbols are the same as in Figure 6

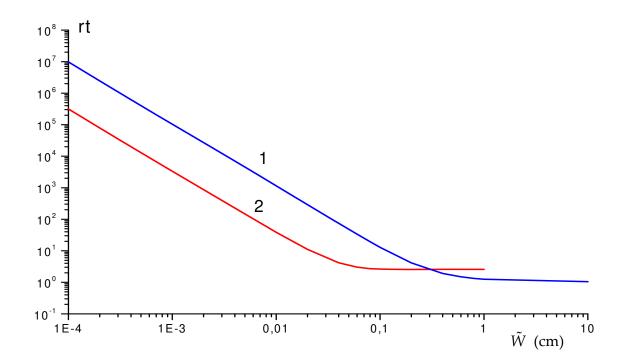


Figure 11. Dependence of ratio $rt = \widetilde{V}_{ph} / V_{ph}$ in the point of maximal value $V_{ph}(N)$ in *GaAs* on thickness \widetilde{W} . Curves 1 and 2 – recombination level energy E_t equals to E_{t1} and E_{t2} . V_{ph} , exact solutions; \widetilde{V}_{ph} , solutions in approximation of quasi-neutrality. Adopted parameters and other symbols are the same as in Figure 6

where quasi-neutral ambipolar drift length of charge carriers

$$d_a = \mu_n^a \times \tau_n \times E_0, \tag{155}$$

effective diffusion length of charge carriers

$$L_{ef} = \sqrt{(D_n^a + D_E) \times \tau_n},$$
(156)
and effective reciprocal diffusion-drift lengths L_1 and L_2 are defined by expressions
$$\frac{1}{L_{1,2}} = \pm \frac{d_a}{2L_{ef}^2} + \sqrt{\left(\frac{d_a}{2L_{ef}^2}\right)^2 + \frac{1}{L_{ef}^2}}.$$
(157)

Relations (18), (20)–(22), (24), (25), (73)–(75), (83), and (153)–(157) determine, in parametric form dependence G(N, V) (see Figures 1a and 2a). Ratio $\delta = N_{-}^{e} / N_{0}^{e}$ is used as parameter in said relations.

It can be shown that equation $\mu_n^a(N)=0$, where μ_n^a is given by expression (74), has a solution when inequalities (27) and (41) are fulfilled. In zeroth-order with respect to small parameters (27) and (41), the root of this equation coincides with maximal extrema of functions $\tau_n(N)$ and $\tau_v(N)$ and equals to N_D (Figure 1b and 1c).

Let's explain dependence μ_n^a on *N* shown in Figure 1c.

Product

$$\mu_n^a \times \tau_n = \mu_p^a \times \tau_p \tag{158}$$

determines drift length and direction in electric field of concentrational perturbation – quasineutral cloud of positive and negative charges [2, 31], including bound at deep impurity (here μ_n^a and μ_p^a are electron and hole ambipolar mobility). Last mentioned bounding explains dependence μ_n^a on ratio $\tau_p(N)/\tau_n(N)$ in trap-assisted recombination. It would appear reasonable that charge carriers, which prevail in quantity, can easily shield photoexcited space charge, i.e., they are adjusted to drift of charge carriers of another type. That is why, in the case of band-to-band recombination ($\tau_n = \tau_p$), quasi-neutral cloud of positive and negative charges drifts in electric field with the same velocity and in the same direction as minority charge carriers, whereas in intrinsic material, cloud is out of control by electric field at all [2, 31] (μ_n^a $= \mu_p^a \cong \mu_p > 0$ at $n_e > p_e$, $\mu_n^a = \mu_p^a \cong -\mu_n < 0$ at $n_e < p_e$ and $\mu_n^a = \mu_p^a = 0$ at $n_e = p_e$). Similar situation, but not exactly identical, happens in the case of trap-assisted recombination. In this case, due to the fact that $\tau_p < \tau_n$ (Figure 1c), vanishing μ_n^a occurs in n-type material (for specified parameters in Figure 1, at $n_e \cong 10 \times p_e$ in silicon and $n_e \cong 10^4 \times p_e$ in gallium arsenide). Positive sign of perturbation charge bound at deep impurities (ΔN_{-} <0) causes such behavior. Ratio p_e/n_e begins to increase significantly, and very sharply, only when $N \cong N_D$. At the same time, ratio τ_p / τ_n may not have so many orders of smallness as ratio p_e / n_e may have. Therefore, μ_n^a vanishes when $N \cong N_D$, if deep level, according to conditions (27) and (41), lies in lower half of bandgap. If that level lies in upper half of bandgap, then, again, due to the fact that τ_p/τ_n may not have so many orders of smallness as ratio p_e/n_e may have, function $\mu_n^a(N)$ is always positive for actual values N, wherein lifetimes τ_p and τ_n decrease always with increasing N (see Section 3). We denote solution based on relations (152) and (153) as approximate. Parameter $\xi(N)$, still remaining small, reaches its global maximum near point $N = N = N_D$, where function G(N) reaches maximal extremum G (Figure 1a). Deviation of approximate value $G = G_{appr}$ from exact value $G = G_{exact}$ (calculated with due regard for all terms in relation (149) and equation (151)} is shown in Figure 2b. Exact solution at N = N is not so difficult to find, because at this point $\mu_n^a = 0$. It is clear from Figure 2b that agreement \hat{G}_{appr} with \hat{G}_{exact} is quite good.

From expression (154), it follows that

$$\hat{G} = \left\{ 1 - 2 \times \frac{\hat{L}_{ef}}{W} \times th\left(\frac{W}{2\hat{L}_{ef}}\right) \right\} \times \left(\mu_n \times \hat{\tau}_n + \mu_p \times \hat{\tau}_p\right) \times \frac{E_0}{W},$$
(159)

where

$$\hat{L}_{ef} = \sqrt{\hat{L}_{a}^{2} + \hat{L}_{E}^{2}}$$
(160)

is effective ambipolar length (156) at N = N (i.e., at $\delta \cong \sqrt{A+B}$) and $\hat{\tau}_n$ and $\hat{\tau}_p$ are relevant electron (48) and hole (38) lifetimes. We can write that

$$\hat{\tau}_n = \frac{\sqrt{A+B}}{2 \times w_n \times N_D}, \hat{\tau}_p = \frac{2 \times A + \theta \times B \times \sqrt{A+B}}{2 \times w_p \times N_D \times (A+B)},$$
(161)

$$\hat{L}_{a}^{2} = \frac{(A / \theta) + B \times \sqrt{A + B}}{(A + B) \times D_{n} + B \times D_{p}} \times \frac{D_{n} \times D_{p}}{w_{n} \times N_{D}},$$
(162)

$$\hat{L}_{E}^{2} = \frac{\varepsilon}{8 \times \pi \times q} \times \frac{2 \times A + (B+1) \times \theta \times \sqrt{A+B}}{w_{p} \times N_{D} \times n_{t} \times \sqrt{A+B}} \times \frac{\mu_{n} \times \mu_{p} \times E_{0}^{2}}{(A+B) \times \mu_{n} + B \times \mu_{p}}.$$
(163)

Value \hat{L}_{a} is conventional ambipolar diffusion length at maximal extremum of function G(N) (Figure 1a) calculated in quasi-neutrality approximation, i.e., when parameter ξ is set to zero. From expression (159), it follows that function \hat{G} depends non-monotonically on applied bias voltage V (Figure 2a). This is caused by increased \hat{L}_{ef} with increasing $E_0 = V / W$ that provides progressive loss of photoexcited charge carriers resulting from increasing diffusive inflow of photocarriers to current contacts' electrodes with follow-up recombination.

Increase in effective ambipolar diffusion constant $D_{ef} = D_n^a + D_E$ (coefficient before second derivative in equation (152)) causes elongation \hat{L}_{ef} with increasing E_0 . In turn, photoinduced space charge $\Delta \rho$ (4) causes monotonic increased D_{ef} with increasing E_0 . The analysis of expressions (159)–(163) shows that function $\hat{G}(V)$ reaches its maximum value (Figure 2c)

$$\hat{G}_{\max}(W) \cong \begin{cases} \frac{25}{72} \times \frac{W}{\hat{L}_{a}} \times \hat{G}_{\max}^{\max}, & when \quad W < 2 \times \hat{L}_{a} \\ \hat{G}_{\max}^{\max}, & when \quad W > 2 \times \hat{L}_{a} \end{cases}$$
(164)

when bias voltage is applied across sample $V = V_{ovt}(W)$, where optimal bias voltage (Figure 2d)

$$V_{opt}(W) \cong \begin{cases} \tilde{E}_0 \times W, & \text{when } W < 2 \times \hat{L}_a \\ \frac{\tilde{E}_0 \times W^2}{2 \times \hat{L}_a}, & \text{when } W > 2 \times \hat{L}_a \end{cases}$$
(165)

Threshold value $G = \hat{G}_{\max}^{\max}$ (for given physical parameters of semiconductor) and electric field intensity $E_0 = \tilde{E}_{0'}$ at which $\hat{L}_{ef} = \sqrt{2} \times \hat{L}_{a'}$ are defined by the following expressions:

$$\hat{G}_{\max}^{\max} = (\mu_n \times \hat{\tau}_n + \mu_p \times \hat{\tau}_p) \times \frac{3 \times \tilde{E}_0}{25 \times \hat{L}_a},$$

$$\tilde{E} = \sqrt{\frac{8\pi \times kT \times n_i}{\varepsilon}} \times \left(1 + \frac{A}{B}\right)^{1/4}.$$
(167)

8. Summary

Capture rate of excess charge carriers increases with increasing concentration N of deep impurity levels, i.e., recombination centers (traps). However, as shown in this chapter on the

example of single-level acceptor, this increase does not lead to unavoidable decrease in lifetime of excess electrons τ_n and holes τ_p , when nonequilibrium filling of recombination level states is very low. The matter is that lifetimes are determined not only by capture of excess charge carriers at equilibrium traps but also by bound-to-free transitions of electrons and holes from nonequilibrium capture centers due to thermal emission and by capture of equilibrium charge carriers at nonequilibrium traps as well. Therefore, lifetimes of excess charge carriers can be either more or less than the time of their capture at equilibrium traps and can be strongly nonmonotonic functions of recombination center concentration (Figure 1b). In the case of acceptor recombination level, it can happen if recombination level is located in lower half of forbidden gap. In the case of donor recombination level, it must be located in upper half of forbidden gap. It is essential that the ratio of lifetimes in maximum and minimum of functions $\tau_n(N)$ and $\tau_n(N)$ can be several orders of magnitude (Figures 1b and 3b).

It seems, authors of article [25] have reported first about the availability of minimum and portion of weak growth (up to 24 %) on experimental dependence of excess charge carriers' lifetime on recombination center concentration, which increased because of bombarding sample by high-energy electrons. Many years later, increase in lifetime, presumably, caused by increasing *N*, but already gained in several times, was observed experimentally [32].

The main reason for giant splash of photoresponse in semiconductors with increasing recombination center concentration N (Figures 1a, 6, and 7) is the growth of charge carriers' lifetime in orders of magnitude.

This reason is also sufficient to provide increase, in order of magnitude and more, in efficiency of charge carriers' photoexcitation with increasing N (Figure 6).

At and about point $N = \stackrel{\wedge}{N} \cong N_D$, where charge carriers' lifetime is maximal, equilibrium concentration of charge carriers becomes small, where N_D is shallow dopant concentration. Therefore, increase in Dember photo-emf V_{ph} in several orders of magnitude (Figure 7) is caused by both strongly non-monotonic dependences $\tau_n(N)$ and $\tau_p(N)$ (Figure 1b) and highly non-monotonic dependence of sample dark resistance on concentration N [1-3, 8, 30, 31].

However, increase in orders of magnitude in charge carriers' lifetime with increasing *N* (Figure 1b) is not a good reason for the development of giant splash in photoelectric gain *G* with increasing *N* (Figure 1a). As follows from [18, 19], *G* increases with increasing charge carriers' lifetime, if ambipolar mobility μ_a (see (74), (158), [2]) is equal to zero, or if there is no recombination on current contact electrodes (x = 0 and x = W; see inset in Figure 1a).

In reality, recombination on contact electrodes occurs always to more or less extent [5, 9]. Therefore, under normal conditions ($\mu_a \neq 0$), increase in lifetimes, beginning from some lifetime values, does not increase in photocurrent density I_{ph} [5, 18, 19].

Saturation in I_{ph} is most clear in the case of high-rate recombination at contact electrodes (sweep-out effect on contacts [5, 18, 19]), when there are no photocarriers at contacts, i.e., conditions (1) are fulfilled. At trap-assisted recombination, function $\mu(N)$, under the same conditions (27) and (41), when there are non-monotonic dependences $\tau_n(N)$ and $\tau_p(N)$,

vanishes at the same, up to small, correction value $N \cong \hat{N}$, at which functions $\tau_n(N)$ and $\tau_p(N)$ reach their maximal extrema $\hat{\tau}_n$ and $\hat{\tau}_p$ (Figure 2b and 2c). Therefore, I_{ph} and, consequently, *G* increase to the extent of increasing $\hat{\tau}_n$ and $\hat{\tau}_p$. These are physical grounds of giant splash in photoelectric gain *G* with increasing *N* (Figure 2a). Above mentioned results of strict analytical calculations (i.e., outside commonly used local approximation of quasi-neutrality) show that photoelectric response with increasing concentration of recombination centers.

Strict solutions of problems concerning the quantity of photoexcited electrons N_{ph} and holes P_{ph} and Dember photo-emf V_{ph} may be fundamentally different from solutions obtained in approximation of quasi-neutrality \widetilde{N}_{ph} , \widetilde{P}_{ph} , and \widetilde{V}_{ph} , respectively.

It may be that $P_{ph} / N_{ph} >> 1$ even if hole lifetime τ_p is much less than electron lifetime τ_n (Figure 2b). At the same time, in approximation of quasi-neutrality, $\tilde{P}_{ph} / \tilde{N}_{ph} = \tau_p / \tau_n << 1$ (Figure 2b). At point N = N, at which functions $N_{ph}(N)$, $P_{ph}(N)$, and $V_{ph}(N)$ reach maximum values, and for thin samples (with thickness along light propagation $\tilde{W} < 0.1$ cm), in surroundings of point N = N, solutions obtained in quasi-neutrality approximation may differ from solution outside quasi-neutrality in several orders of magnitude (Figures 8–11). Moreover, even $\tilde{W} \to \infty$, neglecting by photoinduced space charge is not always possible, i.e., it is not always possible to solve problem in quasi-neutrality approximation. The reason is that when recombination level is deep enough, then shielding length of photoexcited space charge may be of the order of ambipolar diffusion length of charge carriers.

At sweep-out effect on contact electrodes, splash of G(N) with increasing N depends nonmonotonically on applied voltage V across the sample (Figure 2a). That non-monotonic behavior is not related to heating of charge carriers or lattice and charge carriers injecting contacts. The reason is the increase in effective ambipolar diffusion constant D (coefficient before second derivative in equation (81) determining the distribution of photocarriers) with increasing V, leading to huge loss of photocarriers due to faster diffusion to contacts and subsequent recombination. In turn, increase in $D \sim V^2$ is caused by photoinduced local space charge. What is important is that, at optimum voltage V_{op} (Figure 2d), value G can have several orders of magnitude (Figure 2c) at high concentrations of recombination centers.

As shown in [33], when recombination impurity *N* has three charged states (two-level recombination center), then, again, strong increase in $\tau_n(N)$ and $\tau_p(N)$ with increasing *N* may occur; moreover dependences $\tau_n(N)$ and $\tau_p(N)$ may have two charged states and two minimums and maximums. Opposite to single-level recombination center, in the case of two-level recombination center, maximum *G*(*N*), as shown in [34], can be reached at lower concentrations *N* and have greater peak value. Photoelectric gain *G*, to the left of maximum value *G*(*N*), is larger in the case of two-level recombination center, than in single level. The reason is the low ambipolar mobility of charge carriers in the case of two-level recombination center.

As shown in [35], significant growth of charge carriers' lifetimes with increase in concentration of recombination impurity in certain range could be stimulated by uncontrolled (background) doping by deep impurities. Even two maximums can occur.

Above-mentioned regularities occur at arbitrarily low-level photoexcitation and they become the more evident, the wider the semiconductor bandgap.

The theory of giant splash of photoresponse in semiconductors at low-level illumination with increasing concentration of recombination centers could develop further through the generalization of boundary conditions on semiconductor surfaces and current contact electrodes, accounting for nonuniformity of charge carriers' photoexcitation along the line of current flow and fluctuation processes. The study of nonstationary (frequency domain and transient) characteristics is of particular interest.

From physical essence of considered effects, it follows that similar effects can occur in other mediums with recombination of dissociative or ion-ion type, for example, in multicomponent plasma [36]. More details about topic are given in [37-46].

Acknowledgements

Authors are grateful to Prof. Sergey A. Nikitov for valuable support of publication.

Author details

Viacheslav A. Kholodnov^{1,2} and Mikhail S. Nikitin^{3*}

*Address all correspondence to: nikiboxm@yandex.ru

1 V.A. Kotelnikov Institute of Radio Engineering and Electronics Russian Academy of Sciences, Moscow, Russia

2 Moscow Institute of Physics and Technology (MIPT), Dolgoprudny town, Moscow Region, Russia

3 JSC Shvabe-Photodevice, Moscow, Russia

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