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Thermodynamics of Reactions  
Among Al<sub>2</sub>O<sub>3</sub>, CaO, SiO<sub>2</sub> and Fe<sub>2</sub>O<sub>3</sub>  
During Roasting Processes

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1. Introduction

The thermodynamic of the chemical reactions among Al<sub>2</sub>O<sub>3</sub>, CaO, SiO<sub>2</sub> and Fe<sub>2</sub>O<sub>3</sub> in the roasting processes was investigated in this chapter. The chemical reactions are classified into SiO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub> system, Fe<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> system, SiO<sub>2</sub>-Fe<sub>2</sub>O<sub>3</sub> system, CaO-Al<sub>2</sub>O<sub>3</sub> system, SiO<sub>2</sub>-CaO system, SiO<sub>2</sub>-calcium aluminates system, CaO-Fe<sub>2</sub>O<sub>3</sub> system, Al<sub>2</sub>O<sub>3</sub>-calcium ferrites system and Al<sub>2</sub>O<sub>3</sub>-CaO-SiO<sub>2</sub>-Fe<sub>2</sub>O<sub>3</sub> system. When the roasting temperature is over 1100K, 3Al<sub>2</sub>O<sub>3</sub>·2SiO<sub>2</sub> is preferentially formed in SiO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub> system; FeO·Al<sub>2</sub>O<sub>3</sub> can be formed in Fe<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> system; ferric oxide and SiO<sub>2</sub> could not generate iron silicate; 12CaO·7Al<sub>2</sub>O<sub>3</sub> is preferentially formed in CaO-Al<sub>2</sub>O<sub>3</sub> system when one mole Al<sub>2</sub>O<sub>3</sub> reacts with CaO; 2CaO·SiO<sub>2</sub> is preferentially formed in SiO<sub>2</sub>-CaO system; except for CaO·2Al<sub>2</sub>O<sub>3</sub> and CaO·Al<sub>2</sub>O<sub>3</sub>, the other calcium aluminates can transform into calcium silicate by reacting with SiO<sub>2</sub> in SiO<sub>2</sub>-calcium aluminates system; 2CaO·Fe<sub>2</sub>O<sub>3</sub> is preferentially formed in CaO-Fe<sub>2</sub>O<sub>3</sub> system; alumina is unable to form 3CaO·Al<sub>2</sub>O<sub>3</sub> with calcium ferrites(2CaO·Fe<sub>2</sub>O<sub>3</sub> and CaO·Fe<sub>2</sub>O<sub>3</sub>), but able to form 12CaO·7Al<sub>2</sub>O<sub>3</sub> with 2CaO·Fe<sub>2</sub>O<sub>3</sub>; when CaO, Fe<sub>2</sub>O<sub>3</sub>, Al<sub>2</sub>O<sub>3</sub>, SiO<sub>2</sub> coexist, they are more likely to form ternary compound 2CaO·Al<sub>2</sub>O<sub>3</sub>·SiO<sub>2</sub> and 4CaO·Al<sub>2</sub>O<sub>3</sub>·Fe<sub>2</sub>O<sub>3</sub>.

2. Binary compounds

2.1 Fe<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub>-CaCO<sub>3</sub> system

Fe<sub>2</sub>O<sub>3</sub> and Al<sub>2</sub>O<sub>3</sub> can all react with limestone during roasting to generate corresponding aluminates and ferrites. In Fe<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub>-CaO system, the reaction Fe<sub>2</sub>O<sub>3</sub> and Al<sub>2</sub>O<sub>3</sub> with CaCO<sub>3</sub> coexist, and the reactions equations are as followed:

Reactions	A, J/mol	B, J/K.mol	Temperature, K
CaCO <sub>3</sub> +Al <sub>2</sub> O <sub>3</sub> =CaO·Al <sub>2</sub> O <sub>3</sub> +CO <sub>2</sub>	161088.3	-244.1	298~1200
CaCO <sub>3</sub> +Fe <sub>2</sub> O <sub>3</sub> =CaO·Fe <sub>2</sub> O <sub>3</sub> +CO <sub>2</sub>	151677.8	-220.9	298~1200

Table 1. The ΔG<sub>T</sub><sup>θ</sup> of Fe<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub>-CaCO<sub>3</sub> system (ΔG<sub>T</sub><sup>θ</sup> = A + BT, J/mol; P<sub>CO<sub>2</sub></sub> =30Pa, i.e., the partial pressure of CO<sub>2</sub> in the air)

The relationships between Gibbs free energy ( $\Delta G_T^\theta$ ) and temperature (T) are as shown in figure 1.

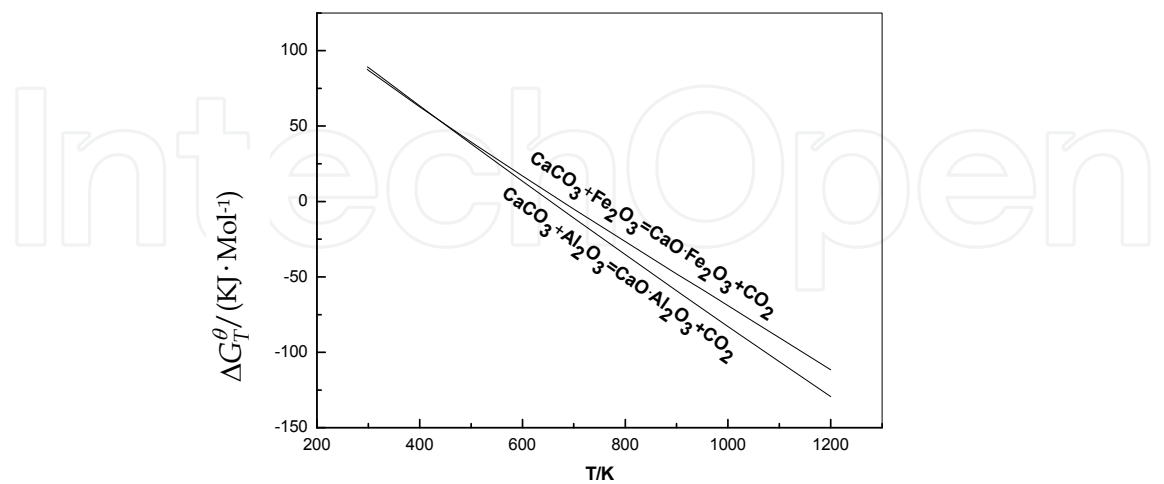


Fig. 1. Relationships between  $\Delta G_T^\theta$  and temperature in  $\text{Fe}_2\text{O}_3\text{-Al}_2\text{O}_3\text{-CaCO}_3$  system

Figure 1 shows that, the Gibbs free energy of reactions on  $\text{Fe}_2\text{O}_3$  and  $\text{Al}_2\text{O}_3$  with  $\text{CaCO}_3$  decreased with the rise of temperature in normal roasting process (due to decomposition of  $\text{CaCO}_3$  over 1200K, so the curve has no drawing above 1200K), and the reactions all can automatically react to generate the corresponding calcium aluminate and calcium ferrite. The  $\Delta G_T^\theta$  of reaction with  $\text{Al}_2\text{O}_3$  is more negative than the  $\Delta G_T^\theta$  of reaction with  $\text{Fe}_2\text{O}_3$  at the same temperature.  $\text{CaCO}_3$  has actually decomposed at 1473~1673K industrial roasting temperature, therefore, only CaO is taken into account on the following analysis.

2.2  $\text{SiO}_2\text{-Al}_2\text{O}_3$  system

$\text{SiO}_2$  mainly comes from the ore and coke ash in the roasting process.  $\text{SiO}_2$  reacts with  $\text{Al}_2\text{O}_3$  to form aluminium silicates. The aluminium silicates mainly include  $\text{Al}_2\text{O}_3 \cdot 2\text{SiO}_2$  ( $\text{AS}_2$ ),  $\text{Al}_2\text{O}_3 \cdot \text{SiO}_2$  ( $\text{AS}$ ,andalusite),  $\text{AS}$ (kyanite),  $\text{AS}$ (fibrolite),  $3\text{Al}_2\text{O}_3 \cdot 2\text{SiO}_2$  ( $\text{A}_3\text{S}_2$ ). Thermodynamic calculation indicates that,  $\text{AS}_2$  can not be formed from the reaction of  $\text{Al}_2\text{O}_3$  and  $\text{SiO}_2$  under the roasting condition. The others equations are shown in table 2.

Reactions	A, J/mol	B, J/K.mol	Temperature, K
$\text{Al}_2\text{O}_3 + \text{SiO}_2 = \text{Al}_2\text{O}_3 \cdot \text{SiO}_2$ ( kyanite )	-8469.3	9.0	298~1696
$\text{Al}_2\text{O}_3 + \text{SiO}_2 = \text{Al}_2\text{O}_3 \cdot \text{SiO}_2$ ( fibrolite )	-4463.8	-0.9	298~1696
$\text{Al}_2\text{O}_3 + \text{SiO}_2 = \text{Al}_2\text{O}_3 \cdot \text{SiO}_2$ ( andalusite )	-6786.1	0.6	298~1696
$\frac{3}{2}\text{Al}_2\text{O}_3 + \text{SiO}_2 = (\frac{1}{2})3\text{Al}_2\text{O}_3 \cdot 2\text{SiO}_2$	12764.7	-16.7	298~1696

Table 2. The  $\Delta G_T^\theta$  of  $\text{Al}_2\text{O}_3\text{-SiO}_2$  system (  $\Delta G_T^\theta = A + BT$  , J/mol)

The relationships of  $\Delta G_T^\theta$  and temperature in  $\text{Al}_2\text{O}_3\text{-SiO}_2$  system is shown in figure 2.

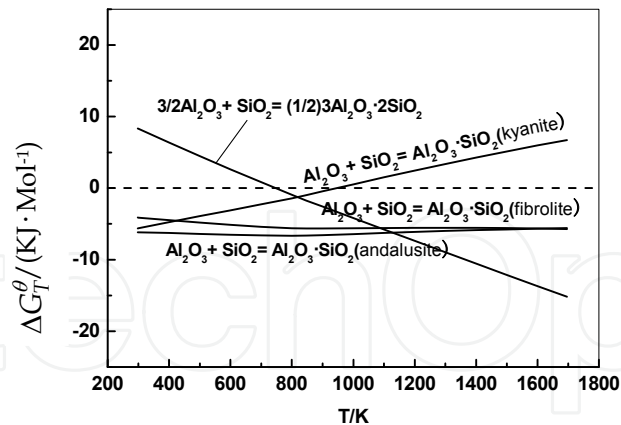


Fig. 2. Relationships of  $\Delta G_T^\theta$  and temperature in Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> system

Figure 2 shows that, the  $\Delta G_T^\theta$  of kyanite is greater than zero at 1000~1700K, so the reaction cannot happen; the  $\Delta G_T^\theta$  of andalusite and fibrolite alter little with temperature changes; the  $\Delta G_T^\theta$  of A<sub>3</sub>S<sub>2</sub> decreases with the rise of temperature. The thermodynamic order of forming aluminium silicates is A<sub>3</sub>S<sub>2</sub>, AS(andalusite), AS(fibrolite) at 1100~1700K.

**2.3 Fe<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> system**

Al<sub>2</sub>O<sub>3</sub> does not directly react with Fe<sub>2</sub>O<sub>3</sub>, but Al<sub>2</sub>O<sub>3</sub> may react with wustite (FeO) produced during roasting process to form FeO·Al<sub>2</sub>O<sub>3</sub>. No pure ferrous oxide (FeO) exists in the actual process. The ratio of oxygen atoms to iron atoms is more than one in wustite, which is generally expressed as Fe<sub>x</sub>O (x=0.83~0.95), whose crystal structure is absence type crystallography. For convenience, FeO is expressed as wustite in this thesis. Al<sub>2</sub>O<sub>3</sub> may react with wustite(FeO) to form FeO·Al<sub>2</sub>O<sub>3</sub> in the roasting process. The relationship of  $\Delta G_T^\theta$  and temperature is shown in figure 2, and the chemical reaction of the equation is as followed:

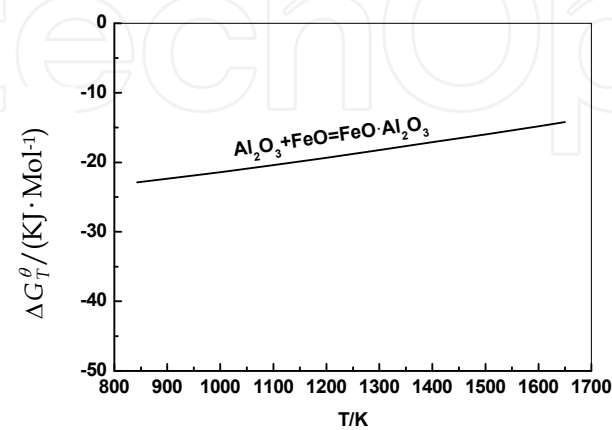
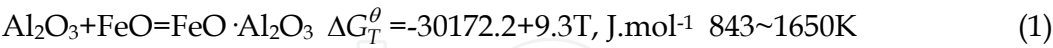


Fig. 3. Relationship of  $\Delta G_T^\theta$  and temperature in Fe<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> system

Figure 3 shows that, the  $\Delta G_T^\theta$  is negative at 843~1650K, reaction can happen and generate  $\text{FeO} \cdot \text{Al}_2\text{O}_3$ ; the  $\Delta G_T^\theta$  rises with the temperature, the higher temperature is, the lower thermodynamic reaction trends.

2.4  $\text{SiO}_2\text{-Fe}_2\text{O}_3$  system

$\text{SiO}_2$  also does not directly react with  $\text{Fe}_2\text{O}_3$ , but  $\text{Al}_2\text{O}_3$  may react with wustite ( $\text{FeO}$ ) to form  $\text{FeO} \cdot \text{SiO}_2$  (FS) and  $2\text{FeO} \cdot \text{SiO}_2(\text{F}_2\text{S})$ . The relationships of  $\Delta G_T^\theta$  and temperature is shown in figure 4, and the chemical reactions of the equations are shown in table 3.

Reactions	A, J/mol	B, J/K.mol	Temperature, K
$\text{FeO} + \text{SiO}_2 = \text{FeO} \cdot \text{SiO}_2$	26524.6	18.8	847~1413
$2\text{FeO} + \text{SiO}_2 = 2\text{FeO} \cdot \text{SiO}_2$	-13457.3	30.3	847~1493

Table 3. The  $\Delta G_T^\theta$  of  $\text{SiO}_2\text{-Al}_2\text{O}_3$  system ( $\Delta G_T^\theta = A + BT$ , J/mol)

Figure 4 shows that, the  $\Delta G_T^\theta$  of  $\text{SiO}_2\text{-Al}_2\text{O}_3$  system are above zero at 847~1500K, so all of the reactions can not happen to form ferrous silicates (FS and  $\text{F}_2\text{S}$ ).

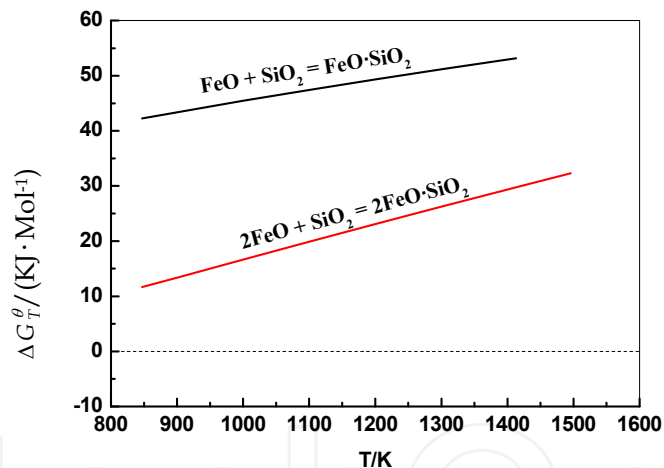


Fig. 4. Relationships of  $\Delta G_T^\theta$  and temperature in  $\text{SiO}_2\text{-Fe}_2\text{O}_3$  system

2.5  $\text{CaO-Al}_2\text{O}_3$  system

$\text{Al}_2\text{O}_3$  can react with  $\text{CaO}$  to form calcium aluminates such as  $3\text{CaO} \cdot \text{Al}_2\text{O}_3(\text{C}_3\text{A})$ ,  $12\text{CaO} \cdot 7\text{Al}_2\text{O}_3(\text{C}_{12}\text{A}_7)$ ,  $\text{CaO} \cdot \text{Al}_2\text{O}_3(\text{CA})$  and  $\text{CaO} \cdot 2\text{Al}_2\text{O}_3(\text{CA}_2)$ . As regard as the calcium aluminates only  $\text{C}_{12}\text{A}_7$  can be totally soluble in soda solution,  $\text{C}_3\text{A}$  and  $\text{CA}$  dissolve with a slow speed, and the other calcium aluminates such as  $\text{CA}_2$  are completely insoluble. Equations that  $\text{Al}_2\text{O}_3$  reacted with  $\text{CaO}$  to form  $\text{C}_3\text{A}$ ,  $\text{C}_{12}\text{A}_7$ ,  $\text{CA}$  and  $\text{CA}_2$  are presented in table 4.

Figure 5 shows that, the  $\Delta G_T^\theta$  of reactions of  $\text{Al}_2\text{O}_3$  with  $\text{CaO}$  decreases with the rise of temperature; all reactions automatically proceed to generate the corresponding calcium aluminates at normal roasting temperature (1473~1673K, same as follows); At the same

roasting temperature, the thermodynamic order that one mole Al<sub>2</sub>O<sub>3</sub> reacts with CaO to generate calcium aluminates such as C<sub>12</sub>A<sub>7</sub>, C<sub>3</sub>A, CA, CA<sub>2</sub>.

Reactions	A, J/mol	B, J/K.mol	Temperature, K
3CaO+ Al <sub>2</sub> O <sub>3</sub> =3CaO ·Al <sub>2</sub> O <sub>3</sub>	-9.9	-28.4	298~1808
$\frac{12}{7}$ CaO+Al <sub>2</sub> O <sub>3</sub> =( $\frac{1}{7}$ )12CaO ·7Al <sub>2</sub> O <sub>3</sub>	318.3	-44.5	298~1800
CaO+ Al <sub>2</sub> O <sub>3</sub> =CaO ·Al <sub>2</sub> O <sub>3</sub>	-15871.5	-18.1	298~1878
$\frac{1}{2}$ CaO+Al <sub>2</sub> O <sub>3</sub> =( $\frac{1}{2}$ )CaO ·2Al <sub>2</sub> O <sub>3</sub>	-6667.2	-13.8	298~2023

Table 4. The  $\Delta G_T^\theta$  of Al<sub>2</sub>O<sub>3</sub>-CaO system ( $\Delta G_T^\theta = A + BT$  , J/mol)

The relationships between  $\Delta G_T^\theta$  and temperature (T) are shown in figure 5.

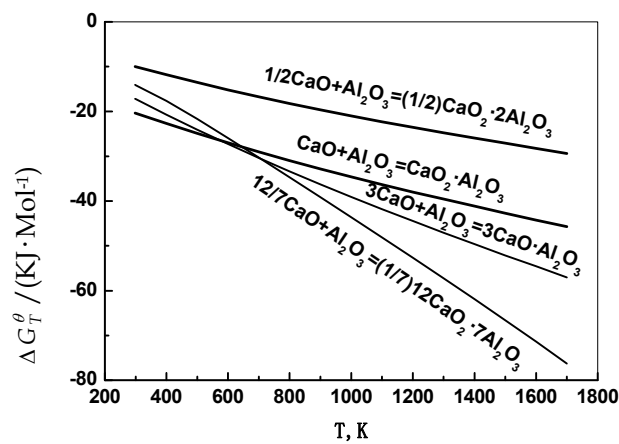


Fig. 5. Relationships between  $\Delta G_T^\theta$  and temperature in Al<sub>2</sub>O<sub>3</sub>-CaO system

Reactions	A, J/mol	B, J/K.mol	Temperature, K
$(\frac{4}{3})3\text{CaO} \cdot \text{Al}_2\text{O}_3 + \text{Al}_2\text{O}_3 = (\frac{1}{3})12\text{CaO} \cdot 7\text{Al}_2\text{O}_3$	13939.7	-65.8	298~1800
$(\frac{1}{2})3\text{CaO} \cdot \text{Al}_2\text{O}_3 + \text{Al}_2\text{O}_3 = (\frac{3}{2})\text{CaO} \cdot \text{Al}_2\text{O}_3$	-18843.8	-13.0	298~1878
$(\frac{1}{5})3\text{CaO} \cdot \text{Al}_2\text{O}_3 + \text{Al}_2\text{O}_3 = (\frac{3}{5})\text{CaO} \cdot 2\text{Al}_2\text{O}_3$	-6011.2	-10.9	298~2023
$(\frac{1}{5})12\text{CaO} \cdot 7\text{Al}_2\text{O}_3 + \text{Al}_2\text{O}_3 = (\frac{12}{5})\text{CaO} \cdot \text{Al}_2\text{O}_3$	-38544.8	18.8	298~1878
$(\frac{1}{17})12\text{CaO} \cdot 7\text{Al}_2\text{O}_3 + \text{Al}_2\text{O}_3 = (\frac{12}{17})\text{CaO} \cdot 2\text{Al}_2\text{O}_3$	-9541.1	-1.2	298~2023
$\text{CaO} \cdot \text{Al}_2\text{O}_3 + \text{Al}_2\text{O}_3 = \text{CaO} \cdot 2\text{Al}_2\text{O}_3$	2543.8	-9.5	298~2023

Table 5. The  $\Delta G_T^\theta$  of Al<sub>2</sub>O<sub>3</sub>-calcium aluminates system ( $\Delta G_T^\theta = A + BT$  , J/mol)

When CaO is insufficient, redundant Al<sub>2</sub>O<sub>3</sub> may promote the newly generated high calcium-to-aluminum ratio (CaO to Al<sub>2</sub>O<sub>3</sub> mole ratio) calcium aluminates to transform into lower calcium-to-aluminum ratio calcium aluminates. The reactions of the equations are presented in table 5:

The relationships between  $\Delta G_T^\theta$  of reactions of Al<sub>2</sub>O<sub>3</sub>-calcium aluminates system and temperature (T) are shown in figure 6.

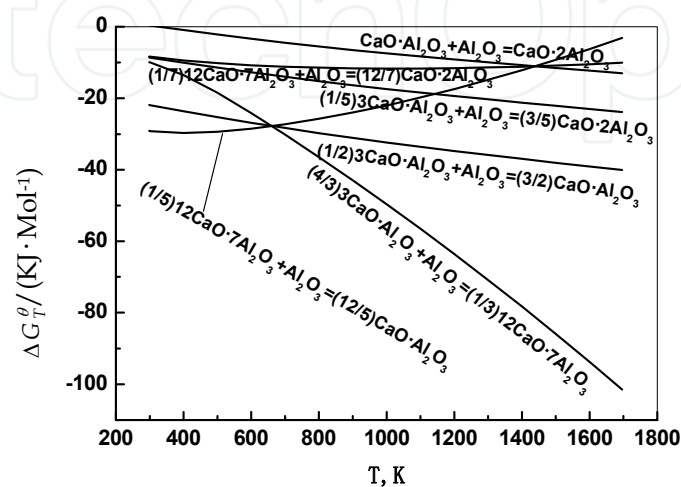


Fig. 6. Relationships between  $\Delta G_T^\theta$  of reactions Al<sub>2</sub>O<sub>3</sub>-calcium aluminates system and temperature

Figure 6 shows that, Gibbs free energy of the reaction of Al<sub>2</sub>O<sub>3</sub>-calcium aluminates system are negative at 400~1700K, and all the reactions automatically proceed to generate the corresponding low calcium-to-aluminum ratio calcium aluminates; Except for the reaction of Al<sub>2</sub>O<sub>3</sub>-C<sub>12</sub>A<sub>7</sub>, the  $\Delta G_T^\theta$  of the rest reactions decreases with the rise of temperature and becomes more negative. Comparing figure 4 with figure 5, it can be found that Al<sub>2</sub>O<sub>3</sub> reacts with CaO easily to generate C<sub>12</sub>A<sub>7</sub>.

2.6 SiO<sub>2</sub>- CaO system

SiO<sub>2</sub> can react with CaO to form CaO·SiO<sub>2</sub> (CS), 3CaO·2SiO<sub>2</sub> (C<sub>3</sub>S<sub>2</sub>), 2CaO·SiO<sub>2</sub> (C<sub>2</sub>S) and 3CaO·SiO<sub>2</sub>(C<sub>3</sub>S) in roasting process. The reactions are shown in table 6, and the relationships between  $\Delta G^0$  of the reactions of SiO<sub>2</sub> with CaO and temperature are shown in figure 7.

Reactions	A, J/mol	B, J/K.mol	Temperature, K
CaO+SiO <sub>2</sub> = CaO·SiO <sub>2</sub> (pseud-wollastonite)	-83453.0	-3.4	298~1817
CaO+SiO <sub>2</sub> = CaO·SiO <sub>2</sub> (wollastonite)	-89822.9	-0.3	298~1817
$\frac{3}{2}$ CaO+SiO <sub>2</sub> =( $\frac{1}{2}$ ) 3CaO·2SiO <sub>2</sub>	-108146.6	-3.1	298~1700
3CaO+SiO <sub>2</sub> = 3CaO·SiO <sub>2</sub>	-111011.9	-11.3	298~1800
2CaO+SiO <sub>2</sub> = 2CaO·SiO <sub>2</sub> (β)	-125875.1	-6.7	298~2403
2CaO+SiO <sub>2</sub> = 2CaO·SiO <sub>2</sub> (γ)	-137890.1	3.7	298~1100

Table 6. The  $\Delta G_T^\theta$  of SiO<sub>2</sub>-CaO system( $\Delta G_T^\theta = A + BT$  , J/mol)

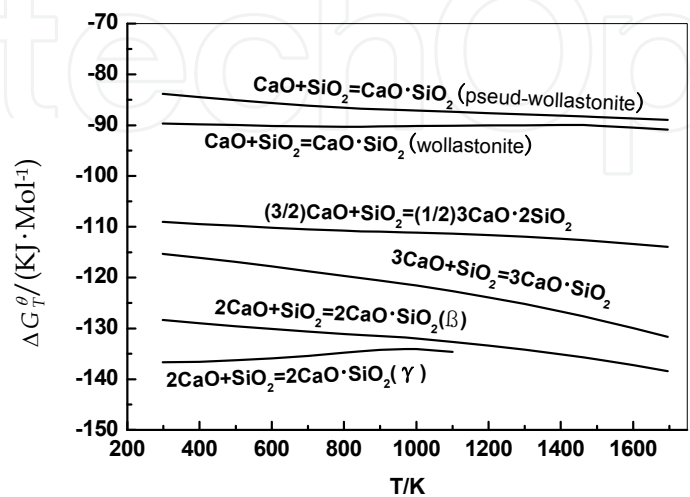


Fig. 7. Relationships between  $\Delta G_T^\theta$  and temperature

Figure 7 shows that, SiO<sub>2</sub> reacts with CaO to form γ-C<sub>2</sub>S when temperature below 1100K, but β-C<sub>2</sub>S comes into being when the temperature above 1100K. At normal roasting temperature, the thermodynamic order of forming calcium silicate is C<sub>2</sub>S, C<sub>3</sub>S, C<sub>3</sub>S<sub>2</sub>, CS.

Figure 5 ~ figure 7 show that, CaO reacts with SiO<sub>2</sub> and Al<sub>2</sub>O<sub>3</sub> firstly to form C<sub>2</sub>S, and then C<sub>12</sub>A<sub>7</sub>. Therefore, it is less likely to form aluminium silicates in roasting process.

## 2.7 SiO<sub>2</sub>- calcium aluminates system

In the CaO-Al<sub>2</sub>O<sub>3</sub> system, if there exists some SiO<sub>2</sub>, the newly formed calcium aluminates are likely to react with SiO<sub>2</sub> to transform to calcium silicates and Al<sub>2</sub>O<sub>3</sub> because SiO<sub>2</sub> is more acidity than that of Al<sub>2</sub>O<sub>3</sub>. The reaction equations are presented in table 7, the relationships between  $\Delta G_T^\theta$  and temperature are shown in figure 8.

Figure 8 shows that, the  $\Delta G_T^\theta$  of all the reactions increases with the temperature increases; the reaction (3CA<sub>2</sub>+SiO<sub>2</sub>=C<sub>3</sub>S+6Al<sub>2</sub>O<sub>3</sub>) can not happen when the roasting temperature is above 900K, i.e., the lowest calcium-to-aluminum ratio calcium aluminates cannot transform to the highest calcium-to-silicon ratio (CaO to SiO<sub>2</sub> molecular ratio) calcium silicate; when the temperature is above 1500K, the  $\Delta G_T^\theta$  of reaction(3CA+ SiO<sub>2</sub>=C<sub>3</sub>S+3Al<sub>2</sub>O<sub>3</sub>) is also more than zero; but the other calcium aluminates all can react with SiO<sub>2</sub> to generate calcium silicates at 800~1700K. The thermodynamic sequence of calcium aluminates reaction with SiO<sub>2</sub> is firstly C<sub>3</sub>A, and then C<sub>12</sub>A<sub>7</sub>, CA, CA<sub>2</sub>.



Reactions	A, J/mol	B, J/K.mol	Temperature, K
$(3)\text{CaO} \cdot 2\text{Al}_2\text{O}_3 + \text{SiO}_2 = 3\text{CaO} \cdot \text{SiO}_2 + 6\text{Al}_2\text{O}_3$	-69807.8	70.8	298~1800
$(3)\text{CaO} \cdot \text{Al}_2\text{O}_3 + \text{SiO}_2 = 3\text{CaO} \cdot \text{SiO}_2 + 3\text{Al}_2\text{O}_3$	-62678.8	42.6	298~1800
$(\frac{1}{4})12\text{CaO} \cdot 7\text{Al}_2\text{O}_3 + \text{SiO}_2 = 3\text{CaO} \cdot \text{SiO}_2 + \frac{7}{4}\text{Al}_2\text{O}_3$	-111820.6	66.7	298~1800
$(2)\text{CaO} \cdot 2\text{Al}_2\text{O}_3 + \text{SiO}_2 = 2\text{CaO} \cdot \text{SiO}_2 + 4\text{Al}_2\text{O}_3$	-98418.8	48.1	298~1710
$(\frac{3}{2})\text{CaO} \cdot 2\text{Al}_2\text{O}_3 + \text{SiO}_2 = (\frac{1}{2})3\text{CaO} \cdot 2\text{SiO}_2 + 3\text{Al}_2\text{O}_3$	-87585.9	38.0	298~1700
$\text{CaO} \cdot 2\text{Al}_2\text{O}_3 + \text{SiO}_2 = \text{CaO} \cdot \text{SiO}_2 + 2\text{Al}_2\text{O}_3$	-76146.6	27.1	298~1817
$\text{CaO} \cdot \text{Al}_2\text{O}_3 + \text{SiO}_2 = \text{CaO} \cdot \text{SiO}_2 + \text{Al}_2\text{O}_3$	-73770.2	17.7	298~1817
$(\frac{3}{2})\text{CaO} \cdot \text{Al}_2\text{O}_3 + \text{SiO}_2 = (\frac{1}{2})3\text{CaO} \cdot 2\text{SiO}_2 + \frac{3}{2}\text{Al}_2\text{O}_3$	-84021.4	23.8	298~1700
$(2)\text{CaO} \cdot \text{Al}_2\text{O}_3 + \text{SiO}_2 = 2\text{CaO} \cdot \text{SiO}_2 + 2\text{Al}_2\text{O}_3$	-93666.1	29.2	298~1710
$(\frac{1}{12})12\text{CaO} \cdot 7\text{Al}_2\text{O}_3 + \text{SiO}_2 = \text{CaO} \cdot \text{SiO}_2 + \frac{7}{12}\text{Al}_2\text{O}_3$	-90150.8	25.7	298~1800
$(\frac{1}{8})12\text{CaO} \cdot 7\text{Al}_2\text{O}_3 + \text{SiO}_2 = (\frac{1}{2})3\text{CaO} \cdot 2\text{SiO}_2 + \frac{7}{8}\text{Al}_2\text{O}_3$	-108592.3	35.9	298~1700
$(\frac{1}{6})12\text{CaO} \cdot 7\text{Al}_2\text{O}_3 + \text{SiO}_2 = 2\text{CaO} \cdot \text{SiO}_2 + \frac{7}{6}\text{Al}_2\text{O}_3$	-126427.4	45.3	298~1710
$(\frac{1}{3})3\text{CaO} \cdot \text{Al}_2\text{O}_3 + \text{SiO}_2 = \text{CaO} \cdot \text{SiO}_2 + \frac{1}{3}\text{Al}_2\text{O}_3$	-86654.2	9.4	298~1808
$3\text{CaO} \cdot \text{Al}_2\text{O}_3 + \text{SiO}_2 = 3\text{CaO} \cdot \text{SiO}_2 + \text{Al}_2\text{O}_3$	-100774.6	16.9	298~1808
$(\frac{1}{2})3\text{CaO} \cdot \text{Al}_2\text{O}_3 + \text{SiO}_2 = (\frac{1}{2})3\text{CaO} \cdot 2\text{SiO}_2 + \frac{1}{2}\text{Al}_2\text{O}_3$	-103069.3	11.0	298~1700
$(\frac{2}{3})3\text{CaO} \cdot \text{Al}_2\text{O}_3 + \text{SiO}_2 = 2\text{CaO} \cdot \text{SiO}_2 + \frac{2}{3}\text{Al}_2\text{O}_3$	-119063.3	12.1	298~1710

Table 7. The  $\Delta G_T^\theta$  of the reactions  $\text{SiO}_2$  with calcium aluminates(  $\Delta G_T^\theta = A + BT$  , J/mol)

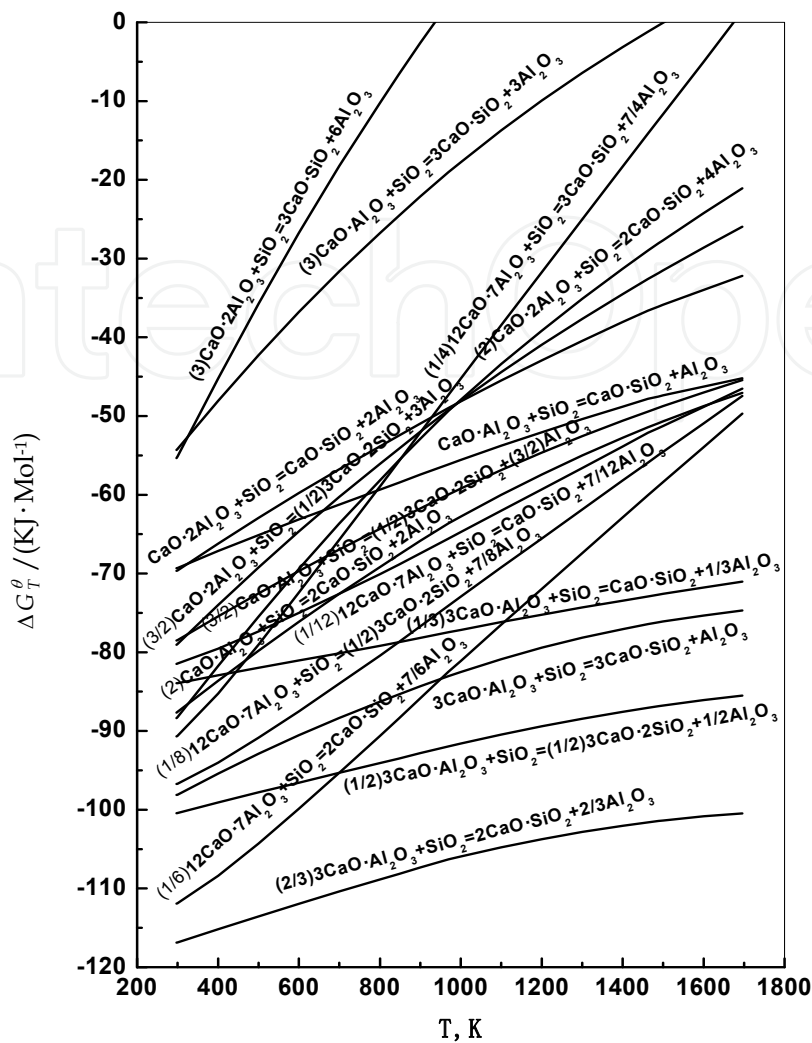


Fig. 8. Relationships between  $\Delta G_T^0$  and temperature in SiO<sub>2</sub>-calcium aluminates system

2.8 CaO- Fe<sub>2</sub>O<sub>3</sub> system

Fe<sub>2</sub>O<sub>3</sub> can react with CaO to form CaO·Fe<sub>2</sub>O<sub>3</sub>(CF) and 2CaO·Fe<sub>2</sub>O<sub>3</sub>(C<sub>2</sub>F). When Fe<sub>2</sub>O<sub>3</sub> is used up, the newly formed C<sub>2</sub>F can react with Fe<sub>2</sub>O<sub>3</sub> to form CF. The reaction equations are shown in table 8, and the relationships between  $\Delta G^0$  and temperature are shown in figure 9.

Figure 9 shows that, Fe<sub>2</sub>O<sub>3</sub> reacts with CaO much easily to form C<sub>2</sub>F; CF is not from the reaction of C<sub>2</sub>F and Fe<sub>2</sub>O<sub>3</sub>, but from the directly reaction of Fe<sub>2</sub>O<sub>3</sub> with CaO. When Fe<sub>2</sub>O<sub>3</sub> is excess, C<sub>2</sub>F can react with Fe<sub>2</sub>O<sub>3</sub> to form CF.

Reactions	A, J/mol	B, J/K.mol	Temperature, K
CaO+Fe <sub>2</sub> O <sub>3</sub> =CaO·Fe <sub>2</sub> O <sub>3</sub>	-19179.9	-11.1	298~1489
2CaO+Fe <sub>2</sub> O <sub>3</sub> =2CaO·Fe <sub>2</sub> O <sub>3</sub>	-40866.7	-9.3	298~1723
2CaO·Fe <sub>2</sub> O <sub>3</sub> +Fe <sub>2</sub> O <sub>3</sub> =(2)CaO·Fe <sub>2</sub> O <sub>3</sub>	2340.8	-12.6	298~1489

Table 8. The  $\Delta G_T^0$  of Fe<sub>2</sub>O<sub>3</sub>-CaO system( $\Delta G_T^0 = A + BT$ , J/mol)

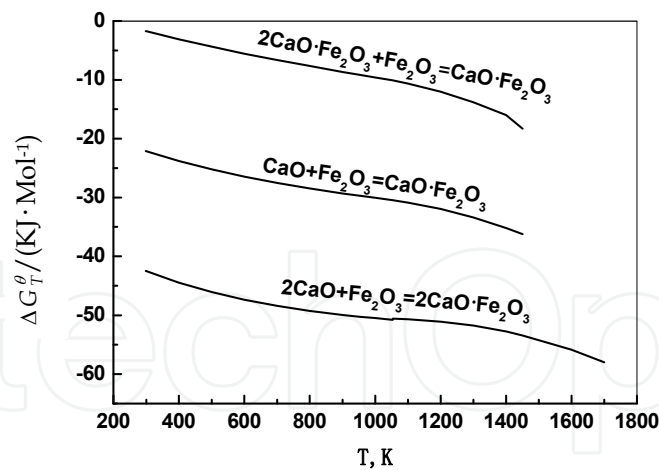


Fig. 9. Relationships between  $\Delta G_T^\theta$  and temperature in  $\text{Fe}_2\text{O}_3$ -CaO system

2.9  $\text{Al}_2\text{O}_3$ - calcium ferrites system

Figure 1 shows that, the  $\Delta G_T^\theta$  of the reaction of  $\text{Al}_2\text{O}_3$  with  $\text{CaCO}_3$  is more negative than that of  $\text{Fe}_2\text{O}_3$  with  $\text{CaCO}_3$ , therefore, the reaction of  $\text{Fe}_2\text{O}_3$  with  $\text{CaCO}_3$  occurs after the reaction of  $\text{Al}_2\text{O}_3$  with  $\text{CaCO}_3$  under the conditions of excess  $\text{CaCO}_3$ . The new generated calcium ferrites are likely to transform into calcium aluminates when  $\text{CaCO}_3$  is insufficient, the reactions are as followed:

Reactions	A, J/mol	B, J/K.mol	Temperature, K
$(3)\text{CaO}\cdot\text{Fe}_2\text{O}_3 + \text{Al}_2\text{O}_3 = 3\text{CaO}\cdot\text{Al}_2\text{O}_3 + 3\text{Fe}_2\text{O}_3$	47922.7	4.5	298~1489
$(\frac{3}{2})2\text{CaO}\cdot\text{Fe}_2\text{O}_3 + \text{Al}_2\text{O}_3 = 3\text{CaO}\cdot\text{Al}_2\text{O}_3 + \frac{3}{2}\text{Fe}_2\text{O}_3$	49.6	$-1.2\times10^{-2}$	298~1723
$(\frac{12}{7})\text{CaO}\cdot\text{Fe}_2\text{O}_3 + \text{Al}_2\text{O}_3 = (\frac{1}{7})12\text{CaO}\cdot7\text{Al}_2\text{O}_3 + \frac{12}{7}\text{Fe}_2\text{O}_3$	32685.1	-24.5	298~1489
$(\frac{6}{7})2\text{CaO}\cdot\text{Fe}_2\text{O}_3 + \text{Al}_2\text{O}_3 = (\frac{1}{7})12\text{CaO}\cdot7\text{Al}_2\text{O}_3 + \frac{6}{7}\text{Fe}_2\text{O}_3$	34514.4	-35.0	298~1723
$\text{CaO}\cdot\text{Fe}_2\text{O}_3 + \text{Al}_2\text{O}_3 = \text{CaO}\cdot\text{Al}_2\text{O}_3 + \text{Fe}_2\text{O}_3$	3626.6	-7.5	298~1489
$(\frac{1}{2})\text{CaO}\cdot\text{Fe}_2\text{O}_3 + \text{Al}_2\text{O}_3 = (\frac{1}{2})\text{CaO}\cdot2\text{Al}_2\text{O}_3 + \frac{1}{2}\text{Fe}_2\text{O}_3$	3215.1	-8.8	298~1489
$(\frac{1}{4})2\text{CaO}\cdot\text{Fe}_2\text{O}_3 + \text{Al}_2\text{O}_3 = (\frac{1}{2})\text{CaO}\cdot2\text{Al}_2\text{O}_3 + \frac{1}{4}\text{Fe}_2\text{O}_3$	3168.6	-11.0	298~1723
$(\frac{1}{2})2\text{CaO}\cdot\text{Fe}_2\text{O}_3 + \text{Al}_2\text{O}_3 = \text{CaO}\cdot\text{Al}_2\text{O}_3 + \frac{1}{2}\text{Fe}_2\text{O}_3$	4009.5	-12.8	298~1723

Table 9. The  $\Delta G_T^\theta$  of the reaction  $\text{Al}_2\text{O}_3$  with calcium ferrites( $\Delta G_T^\theta = A + BT$ , J/mol)

The relationships between  $\Delta G_T^\theta$  and temperature (T) are shown in figure 10. Figure 10 shows that,  $\text{Al}_2\text{O}_3$  cannot replace the  $\text{Fe}_2\text{O}_3$  in calcium ferrites to generate  $\text{C}_3\text{A}$ , and also cannot replace the  $\text{Fe}_2\text{O}_3$  in  $\text{CaO}\cdot\text{Fe}_2\text{O}_3(\text{CF})$  to generate  $\text{C}_{12}\text{A}_7$ , but it can replace the  $\text{Fe}_2\text{O}_3$  in  $2\text{CaO}\cdot\text{Fe}_2\text{O}_3(\text{C}_2\text{F})$  to generate  $\text{C}_{12}\text{A}_7$  when the temperature is above 1000K, the higher temperature is, the more negative Gibbs free energy is;  $\text{Al}_2\text{O}_3$  can react with CF and  $\text{C}_2\text{F}$  to

form CA or CA<sub>2</sub>, the higher temperature, more negative  $\Delta G_T^\theta$ . Because Fe<sub>2</sub>O<sub>3</sub> reacts with CaO more easily to generate C<sub>2</sub>F (Fig.9), therefore, C<sub>12</sub>A<sub>7</sub> is the reaction product at normal roasting temperature(1073~1673K) under the conditions that CaO is sufficient in batching and the ternary compounds are not considered.

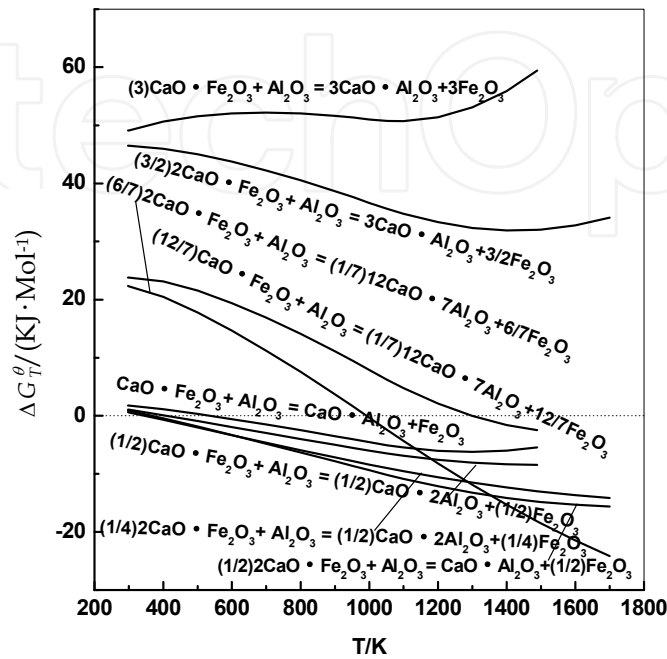


Fig. 10. Relationship between  $\Delta G_T^\theta$  and temperature in Al<sub>2</sub>O<sub>3</sub>- calcium ferrites system

3. Ternary compounds in Al<sub>2</sub>O<sub>3</sub>-CaO-SiO<sub>2</sub>-Fe<sub>2</sub>O<sub>3</sub> system

The ternary compounds formed by CaO, Al<sub>2</sub>O<sub>3</sub> and SiO<sub>2</sub> in roasting process are mainly 2CaO·Al<sub>2</sub>O<sub>3</sub>·SiO<sub>2</sub>(C<sub>2</sub>AS), CaO·Al<sub>2</sub>O<sub>3</sub>·2SiO<sub>2</sub>(CAS<sub>2</sub>), CaO·Al<sub>2</sub>O<sub>3</sub>·SiO<sub>2</sub>(CAS) and 3CaO·Al<sub>2</sub>O<sub>3</sub>·3SiO<sub>2</sub>(C<sub>3</sub>AS<sub>3</sub>). In addition, ternary compound 4CaO·Al<sub>2</sub>O<sub>3</sub>·Fe<sub>2</sub>O<sub>3</sub>(C<sub>4</sub>AF) is formed from CaO, Al<sub>2</sub>O<sub>3</sub> and Fe<sub>2</sub>O<sub>3</sub>. The equations are shown in table 10:

Reactions	A, J/mol	B, J/K.mol	Temperature, K
CaO·SiO <sub>2</sub> +CaO·Al <sub>2</sub> O <sub>3</sub> =2CaO·Al <sub>2</sub> O <sub>3</sub> ·SiO <sub>2</sub>	-30809.41	0.60	298~1600
$\frac{1}{2}$ Al <sub>2</sub> O <sub>3</sub> + $\frac{1}{2}$ CaO + SiO <sub>2</sub> = ( $\frac{1}{2}$ )CaO·Al <sub>2</sub> O <sub>3</sub> ·2SiO <sub>2</sub>	-47997.55	-7.34	298~1826
Al <sub>2</sub> O <sub>3</sub> + 2CaO + SiO <sub>2</sub> =2CaO·Al <sub>2</sub> O <sub>3</sub> ·SiO <sub>2</sub>	-50305.83	-9.33	298~1600
Al <sub>2</sub> O <sub>3</sub> + CaO + SiO <sub>2</sub> =CaO·Al <sub>2</sub> O <sub>3</sub> ·SiO <sub>2</sub>	-72975.54	-9.49	298~1700
$\frac{1}{3}$ Al <sub>2</sub> O <sub>3</sub> + CaO + SiO <sub>2</sub> = ( $\frac{1}{3}$ )3CaO·Al <sub>2</sub> O <sub>3</sub> ·3SiO <sub>2</sub>	-112354.51	20.86	298~1700
4CaO +Al <sub>2</sub> O <sub>3</sub> + Fe <sub>2</sub> O <sub>3</sub> =4CaO·Al <sub>2</sub> O <sub>3</sub> ·Fe <sub>2</sub> O <sub>3</sub>	-66826.92	-62.5	298~2000
Al <sub>2</sub> O <sub>3</sub> + 2CaO + SiO <sub>2</sub> =2CaO·Al <sub>2</sub> O <sub>3</sub> ·SiO <sub>2</sub> (cacoclasite)	-136733.59	-17.59	298~1863

Table 10. The  $\Delta G_T^\theta$  of forming ternary compounds ( $\Delta G_T^\theta = A + BT$ , J/mol)

The relationships between  $\Delta G_T^\theta$  and temperature (T) are shown in figure 11. Figure 11 shows that, except for  $C_3AS_3$ (Hessonite), all the  $\Delta G_T^\theta$  of the reactions get more negative with the temperature increasing; the thermodynamic order of generating ternary compounds at sintering temperature of 1473K is:  $C_2AS$ (cacoclasite),  $C_4AF$ ,  $CAS$ ,  $C_3AS_3$ ,  $C_2AS$ ,  $CAS_2$ .

$C_2AS$  may also be formed by the reaction of CA and CS, the curve is presented in figure 11.

Figure 11 shows that, the  $\Delta G_T^\theta$  of reaction  $(Al_2O_3+CaO+SiO_2)$  is lower than that of reaction of CA and CS to generate  $C_2AS$ . So  $C_2AS$  does not form from the binary compounds CA and CS, but from the direct combination among  $Al_2O_3$ , CaO,  $SiO_2$ . Qiusheng Zhou thinks that,  $C_4AF$  is not formed by mutual reaction of calcium ferrites and sodium aluminates, but from the direct reaction of CaO,  $Al_2O_3$  and  $Fe_2O_3$ . Thermodynamic analysis of figure 1~figure11 shows that, reactions of  $Al_2O_3$ ,  $Fe_2O_3$ ,  $SiO_2$  and CaO are much easier to form  $C_2AS$  and  $C_4AF$ , as shown in figure 12.

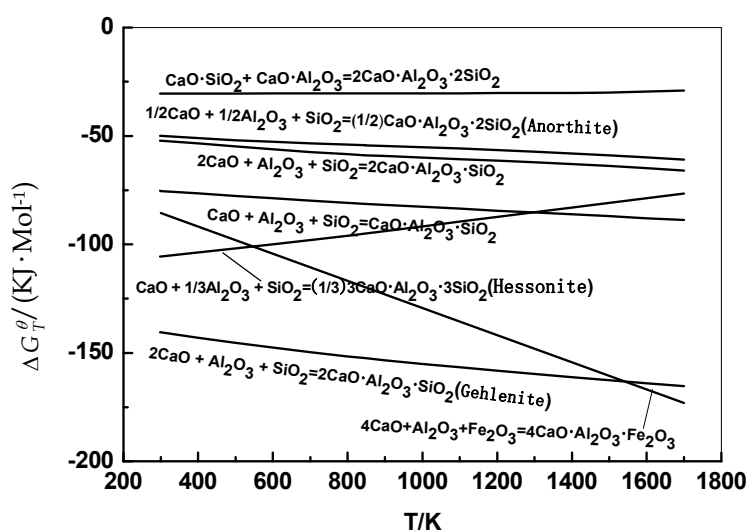


Fig. 11. Relationships between  $\Delta G_T^\theta$  of ternary compounds and temperature

Figure 12 shows that, in thermodynamics,  $C_2AS$  and  $C_4AF$  are firstly formed when  $Al_2O_3$ ,  $Fe_2O_3$ ,  $SiO_2$  and CaO coexist, and then calcium silicates, calcium aluminates and calcium ferrites are generated.

#### 4. Summary

1) When  $Al_2O_3$  and  $Fe_2O_3$  simultaneously react with CaO, calcium silicates are firstly formed, and then calcium ferrites. In thermodynamics, when one mole  $Al_2O_3$  reacts with CaO, the sequence of generating calcium aluminates are  $12CaO \cdot 7Al_2O_3$ ,  $3CaO \cdot Al_2O_3$ ,  $CaO \cdot Al_2O_3$ ,  $CaO \cdot 2Al_2O_3$ . When CaO is insufficient, redundant  $Al_2O_3$  may promote the newly generated high calcium-to-aluminum ratio calcium aluminates to transform to lower calcium-to-aluminum ratio calcium aluminates.  $Fe_2O_3$  reacts with CaO easily to form  $2CaO \cdot Fe_2O_3$ , and  $CaO \cdot Fe_2O_3$  is not from the reaction of  $2CaO \cdot Fe_2O_3$  and  $Fe_2O_3$  but from the directly combination of  $Fe_2O_3$  with CaO.  $Al_2O_3$  cannot replace the  $Fe_2O_3$  in calcium ferrites to generate  $3CaO \cdot Al_2O_3$ , and also cannot replace the  $Fe_2O_3$  in  $CaO \cdot Fe_2O_3$  to generate  $12CaO \cdot 7Al_2O_3$ , but can replace the  $Fe_2O_3$  in  $2CaO \cdot Fe_2O_3$  to generate  $12CaO \cdot 7Al_2O_3$  when the temperature is above 1000K;  $Al_2O_3$  can react with calcium ferrites to form  $CaO \cdot Al_2O_3$  or  $CaO \cdot 2Al_2O_3$ .

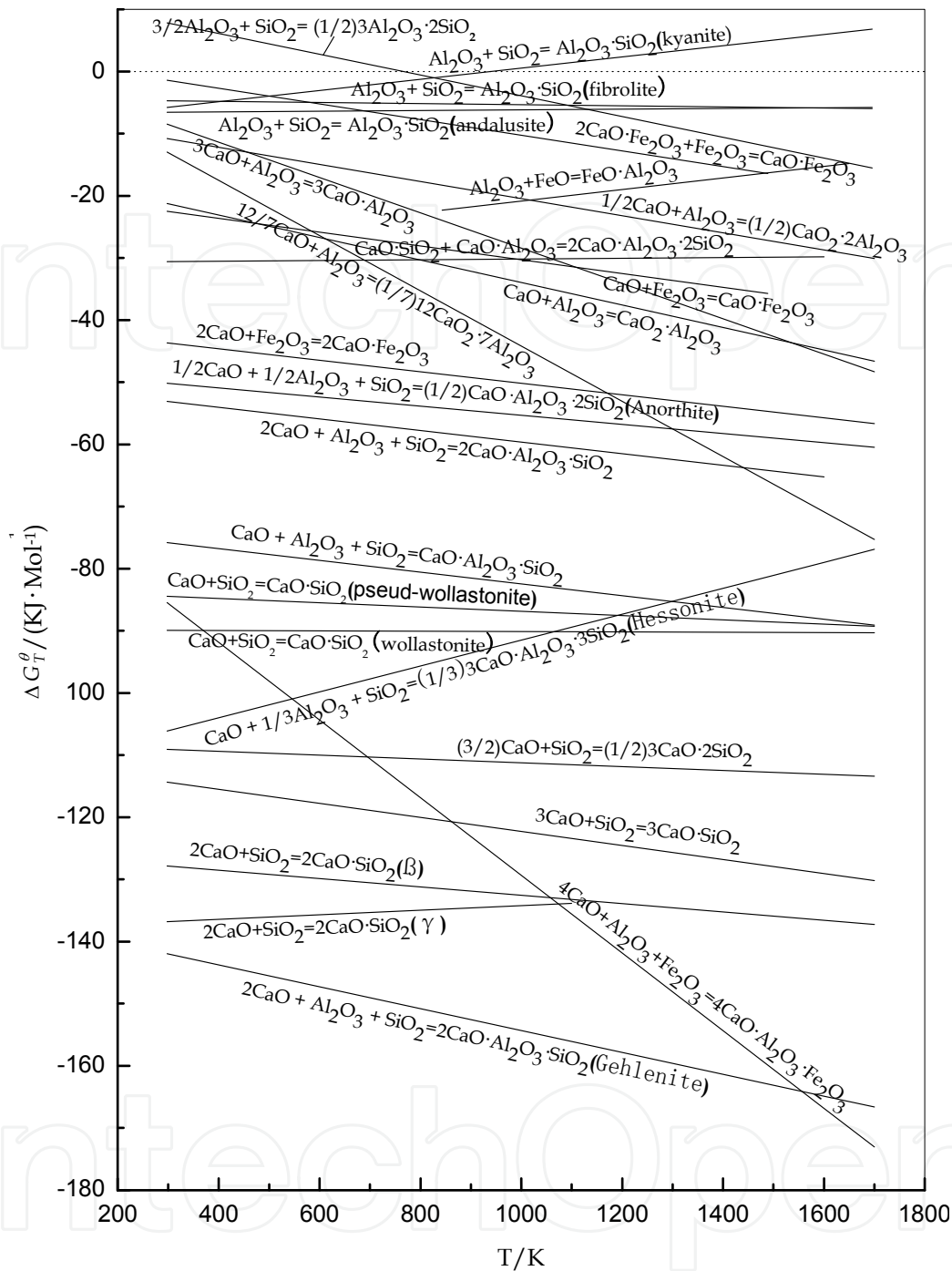


Fig. 12. Relationships between  $\Delta G_T^0$  and temperature in Al<sub>2</sub>O<sub>3</sub>-CaO-SiO<sub>2</sub>-Fe<sub>2</sub>O<sub>3</sub> system

- 2) One mole SiO<sub>2</sub> reacts with Al<sub>2</sub>O<sub>3</sub> much easily to generate 3Al<sub>2</sub>O<sub>3</sub>·2SiO<sub>2</sub>, Fe<sub>2</sub>O<sub>3</sub> can not react with SiO<sub>2</sub> in the roasting process in the air. Al<sub>2</sub>O<sub>3</sub> can not directly react with Fe<sub>2</sub>O<sub>3</sub>, but can react with wustite (FeO) to form FeO·Al<sub>2</sub>O<sub>3</sub>.
- 3) In thermodynamics, the sequence of one mole SiO<sub>2</sub> reacts with CaO to form calcium silicates is 2CaO·SiO<sub>2</sub>, 3CaO·SiO<sub>2</sub>, 3CaO·2SiO<sub>2</sub> and CaO·SiO<sub>2</sub>. Calcium aluminates can react with SiO<sub>2</sub> to transform to calcium silicates and Al<sub>2</sub>O<sub>3</sub>. CaO·2Al<sub>2</sub>O<sub>3</sub> can not transform to 3CaO·SiO<sub>2</sub> when the roasting temperature is above 900K; when the temperature is above



1500K,  $3\text{CaO} \cdot \text{Al}_2\text{O}_3$  can not transform to  $3\text{CaO} \cdot \text{SiO}_2$ ; but the other calcium aluminates all can all react with  $\text{SiO}_2$  to generate calcium silicates at 800~1700K.

4) Reactions among  $\text{Al}_2\text{O}_3$ ,  $\text{Fe}_2\text{O}_3$ ,  $\text{SiO}_2$  and  $\text{CaO}$  easily form  $2\text{CaO} \cdot \text{Al}_2\text{O}_3 \cdot \text{SiO}_2$  and  $4\text{CaO} \cdot \text{Al}_2\text{O}_3 \cdot \text{Fe}_2\text{O}_3$ .  $2\text{CaO} \cdot \text{Al}_2\text{O}_3 \cdot \text{SiO}_2$  does not form from the reaction of  $\text{CaO} \cdot \text{Al}_2\text{O}_3$  and  $\text{CaO} \cdot \text{SiO}_2$ , but from the direct reaction among  $\text{Al}_2\text{O}_3$ ,  $\text{CaO}$ ,  $\text{SiO}_2$ . And  $4\text{CaO} \cdot \text{Al}_2\text{O}_3 \cdot \text{Fe}_2\text{O}_3$  is also not formed via mutual reaction of calcium ferrites and sodium aluminates, but from the direct reaction of  $\text{CaO}$ ,  $\text{Al}_2\text{O}_3$  and  $\text{Fe}_2\text{O}_3$ . In thermodynamics, when  $\text{Al}_2\text{O}_3$ ,  $\text{Fe}_2\text{O}_3$ ,  $\text{SiO}_2$  and  $\text{CaO}$  coexist,  $2\text{CaO} \cdot \text{Al}_2\text{O}_3 \cdot \text{SiO}_2$  and  $4\text{CaO} \cdot \text{Al}_2\text{O}_3 \cdot \text{Fe}_2\text{O}_3$  are firstly formed, and then calcium silicates, calcium aluminates and calcium ferrites.

## 5. Symbols used

Thermodynamic temperature: T, K

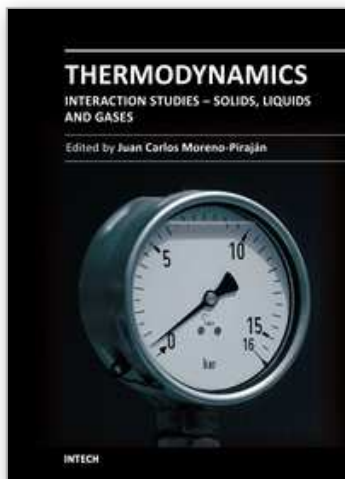
Thermal unit: J

Amount of substance: mole

Standard Gibbs free energy:  $\Delta G_T^\theta$ , J

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## **Thermodynamics - Interaction Studies - Solids, Liquids and Gases**

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