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$$\begin{aligned}
\rho_t &= \frac{\sqrt{r_{mt}}}{\sqrt{r_{mt}} + \sqrt{p_{mt}}} \\
W_t &= \frac{C_d^a P_{t|t-1} C_d^{aT}}{1 - \rho_t} + \frac{R^a}{\rho_t} \\
K_t^e &= \frac{P_{t|t-1} C_d^{aT} W_t^{-1}}{1 - \rho_t} \\
\delta_t &= 1 - (Y_t - C_d^a \hat{X}_{t|t-1}^a)^T W_t^{-1} (Y_t - C_d^a \hat{X}_{t|t-1}^a) \\
\hat{X}_{t|t}^a &= \hat{X}_{t|t-1}^a + K_t^e (Y_t - C_d^a \hat{X}_{t|t-1}^a) \\
P_{t|t} &= \delta_t (\frac{P_{t|t-1}}{1 - \rho_t} - \frac{P_{t|t-1}}{1 - \rho_t} C_d^{aT} W_t^{-1} C_d^a \frac{P_{t|t-1}}{1 - \rho_t}) \\
\hat{X}_{t+1|t}^a &= A_d^a \hat{X}_{t|t}^a + B_d^a U_t \\
\beta_t &= \frac{\sqrt{Tr(Q^a)}}{\sqrt{Tr(Q^a)} + \sqrt{Tr(A_d^a P_{t|t} A_d^{aT})}} \\
P_{t+1|t} &= \frac{A_d^a P_{t|t} A_d^{aT}}{1 - \rho_t} + \frac{Q^a}{\beta_t}
\end{aligned}$$
(3)

#### 4. Modified GPC for unmanned helicopters

To eliminate the negative influence of model errors and control delay in flight, besides the active estimation algorithm like ASMF that does not require a normal distribution assumption, an effective control algorithm has to be designed according to the reference model of Eq. (1) while adopting the on-line estimation of f as compensation.

We describe the normal GPC in Section 4.1, and then, the modified scheme is proposed in Section 4.2 & 4.3 to eliminate the negative influence of model errors in real applications.

#### 4.1 Preliminary work for generalized predictive control

Generally, for a linear system with actuator time delay like,

$$\begin{cases} X_{t+1} = A_d X_t + B_d u_{t-k} + W_t \\ y_t = C_d X_t \end{cases}$$
(4)

where  $X_t \in \mathbb{R}^{n \times 1}$  is the system state vector at sampling time t,  $y_t \in \mathbb{R}^{l \times 1}$  is the output vector,  $u_t \in \mathbb{R}^{m \times 1}$  is the control input vector, k is the actuators' time-delay and  $W_t$  is process noise; traditional Generalized Predictive Control (GPC) [23] can be designed as:

#### **Step I: Make prediction**

Firstly, for the case that predictive step i is less than time-delay k (i.e., the time instant that system behavior cannot be regulated through current and future control action), prediction can be denoted as following equation,

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