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Application of a Strong Tracking Finite-Difference Extended Kalman Filter to Eye Tracking

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1. Introduction

Since eye tracking was first introduced by Mowrer in 1936, it has been gaining in popularity over the past decades as a window into observers' visual and cognitive process. For instance, researchers have utilized eye tracking to study behavior in such domains as driver fatigue detection (Qiang et al., 2004; Horng et al., 2004; Dong et al., 2004), eye typing for helping users with movement disabilities interact with computers (Majaranta & Raiha, 2002), eye tracking analysis of user behavior in WWW search (Laura et al., 2004), using eye tracking techniques to study collaboration on physical tasks for medical research, VR system for measuring inspection methods, and image scanning (Noton & Stark, 1971). Above all applications, two types of human-computer interfaces utilize eye tracking, passive and active interfaces. Passive interfaces monitor the user's eye movements and automatically adapt themselves to the user. For example in driver fatigue detection, the researchers track the driver eyes to fatigue detection, because the human eyes express the most direct reaction when dozing, inattention and yawning. On the other hand, Active interfaces allow users to explicitly control the interface through the use of eye movements. For example, eye typing has users look at keys on a virtual keyboard to type instead of manually depressing keys as on a traditional keyboard (Majaranta & Raiha, 2002; Takehiko et al., 2003). Such active interfaces have been quite effective at helping users with movement disabilities interact with computers. Not surprisingly, eye tracking has attracted the interest of many researchers, and eye trackers have been commercially available for many years (Qiang et al., 2004; Horng et al., 2004; Takehiko et al., 2003; John et al., 2005).

In the past decades, many researchers have paid attention to the eye tracking in human computer interaction. There have been many methods that support non-invasive eye tracking. In (Li et al., 2005), all of these eye tracking algorithms can be classified into two approaches: feature-based and model-based approaches. Feature-based approaches detect and localize image features related to the position of the eye. A commonality among feature-based approaches is that a criteria (e.g., a threshold) is needed to decide when a feature is present or absent. The determination of an appropriate threshold is typically left as a free parameter that is adjusted by the user. The tracked features vary widely across algorithms but most often rely on intensity levels or intensity gradients. For example, in infrared (IR) images created with the dark-pupil technique, an appropriately set intensity threshold can

Source: Kalman Filter, Book edited by: Vedran Kordić,
ISBN 978-953-307-094-0, pp. 390, May 2010, INTECH, Croatia, downloaded from SCIYO.COM

be used to extract the region corresponding to the pupil. The pupil center can be taken as the geometric center of this identified region. The intensity gradient can be used to detect the limbus in visible spectrum images (Zhu & Yang, 2002) or the pupil contour in infrared spectrum images (Tohno et al., 2002). In (Qiang et al., 2004; Zhu et al., 2002; Ebisawa, 1995; Morimoto & Flickner, 2000), several active IR based eye trackers were proposed. The authors thought that eye tracking based on the active remote IR illuminations is a simple and effective approach. But most of them require distinctive bright pupil effect to work well because they all track the eyes by tracking the bright pupils. Qiang et al. has also made significant improvement of eye tracking over existing techniques (Qiang et al., 2004; Zhu et al., 2002). However, their methods need IR eye detector, or bright pupils and steady illumination. Their eye tracking method using Kalman filtering is linear system estimation algorithm. In realistic driving environments, the eye motion is the high nonlinearity of the likelihood model, the stand Kalman filter is no longer optimal.

On the other hand, model-based approaches do not explicitly detect features but rather find the best fitting model that is consistent with the image. For example, integrodifferential operators can be used to find the best-fitting circle (Daugman, 1993) or ellipse (Nishino & Nayar, 2004) for the limbus and pupil contour. Michael Chau and Margrit Betke use correlation with an online template to eye tracking in (Michael & Margrit, 2005). The authors (Hornig et al., 2004) use the dynamic templates for eye tracking. After finding the eye templates, they are used for eye tracking by template matching. And the minimum value within the search area is the most matching position of the eye. The model-based approach can provide a more precise estimate of the pupil center than a feature-based approach given that a feature-defining criteria is not applied to the image data.

Eye tracking has not reached its full potential even though the general-purpose eye tracking technology has been explored for decades. The first obstacle to integrating these techniques into human-computer interfaces is that they have been too expensive for routine use. Currently, a number of eye trackers are available on the market and their prices range from approximately 5,000 to 40,000 US Dollars (Li et al., 2005). The second factor is that it's very difficult to model to eye tracking because of the eye motion being the high nonlinearity. The third factor is the robustness of eye tracking should be improved because of the variety of head and eyes moving fast, external illuminations interference and realistic lighting conditions. The accuracy of eye tracking can't satisfy the realistic requirement of HCI.

To tackle some of those problems, we propose a strong tracking finite-difference extended Kalman filter algorithm to eye tracking. In this paper, a strong tracking factor is introduced to modify prior covariance matrix to improve the accuracy of the algorithm. And the finite-difference method is presented to calculate partial derivatives of nonlinear functions to eye tracking. At the same time, we overcome the eye tracking modeling in nonlinear system. The last experimental results show that the average correct rate of eye tracking can achieve 99.4% on three video.

The organization of the paper is as follows. Strong Tracking Finite-Difference Extended Kalman Filter algorithm is given in next section. Section 3 gives STFDEKF based Eye Tracking algorithm and experimental results. Final conclusion is in section 4.

2. Strong tracking finite-difference extended Kalman filter

Extended Kalman filter (EKF) is one of the most common and popular filtering approach in nonlinear target tracking and state estimation. It includes state estimation of a nonlinear

dynamic system, parameters estimation for nonlinear system identification and dual estimation where both states and parameters are estimated simultaneously. However, EKF simply linearizes all nonlinear functions to the first order by using the Talyor series expansions. At the same time, EKF may cause more errors for the nonlinear system while estimating system state and its variance. Moreover, the linearization may lead to divergence of filtering process. In a nonlinear mismatched model and limited applications scope, EKF filter will lead the divergence problem of state estimation. For these reasons, two improved EKF algorithms are introduced to tackle some of those problems.

2.1 Suboptimal fading extended Kalman filter

In this section, an adaptive extended Kalman filter - a suboptimal fading extended Kalman filter (SFEKF) is presented. The derivation of the filter is presented (Zhou et al., 1991; Zhou et al., 1990) in detail. SFEKF has the following good properties: 1) lower sensitivity to the statistics of the initial states and the statistics of the system and/or measurement noise, 2) stronger tracking ability to the suddenly changing states and bias no matter whether the filter operates in dynamic or stationary fashion, 3) acceptable computational complexity. Considering a class of nonlinear discrete-time dynamical system,

$$x_{k+1} = f(x_k, u_k, v_k) \quad (1)$$

$$y_k = g(x_k, w_k) \quad (2)$$

where, x_k is the state vector, y_k is the measurement vector, u_k is control input vector, v_k is process noise and w_k is measurement noise. v_k and w_k are statistically independent. The equations of mean and covariance are as follow.

$$\begin{aligned} E[v_k] &= q_k, \quad \text{cov}[v_k, v_j] = Q_k \delta(k-j) \\ E[w_k] &= r_k, \quad \text{cov}[w_k, w_j] = R_k \delta(k-j) \end{aligned} \quad (3)$$

The extended Kalman filter is based on the assumption that sensor noises and, propagation errors are driven by zero-mean, Gaussian-distributed, white, random process. Retaining only the first-order terms in the Taylor series expansion, one obtains

$$\begin{cases} x_{k+1} \approx f(\hat{x}_k, u_k, q_k) + F_x(k)(x_k - \hat{x}_k) + F_v(k)(v_k - q_k), \\ y_k \approx g(\bar{x}_k, r_k) + G_x(k)(x_k - \hat{x}_k) + G_w(k)(w_k - r_k), \end{cases} \quad (4)$$

where $F_x(k)$ and $F_v(k)$ are the partial derivatives of $f(\bullet)$ to x and v , $G_x(k)$ and $G_w(k)$ are the partial derivatives of $g(\bullet)$ to x and w .

So the suboptimal fading extended Kalman filter (SFEKF) is deduced as follows:

The predicted state estimation equations are

$$\bar{x}_{k+1} = f(\hat{x}_k, u_k, v_k) \quad (5)$$

$$\bar{y}_k = g(\bar{x}_k, r_k) \quad (6)$$

The predicted covariance estimation equations are

$$\bar{P}_{k+1} = \lambda(k+1)F_x(k)\hat{P}_k F_x(k)^T + F_v(k)Q_k F_v(k)^T \quad (7)$$

Where $\lambda(k+1) \geq 1$ is the suboptimal fading factor, which is used to fade the bypast datum and adjust predictable state estimation covariance matrix.

With this model (Zhou et al., 1993), $\lambda(k+1)$ can be directly determined as follows:

$$\lambda(k+1) = \begin{cases} \lambda_0, \lambda_0 \geq 1; \\ 1, \lambda_0 < 1; \end{cases} \quad (8)$$

Where

$$\lambda_0 = \text{tr}[N(k+1)] / \text{tr}[M(k+1)], \quad (9)$$

$$N(k+1) = V_0(k+1) - G_x(k)F_v(k) \bullet F_v(k)^T - G_w(k)R_k G_w(k)^T, \quad (10)$$

$$M(k+1) = G_x F_x(k) \hat{P}_k F_x(k)^T G_x^T(k). \quad (11)$$

$$V_0(k+1) = \frac{1}{k} \sum_{j=1}^k \gamma_j \gamma_j^T = \begin{cases} G_x(0)\hat{P}_0 G_x(0) + G_w(0)^T, k=0; \\ \frac{\rho V_0(k) + \gamma_j \gamma_j^T}{1+\rho}, k \geq 1 \end{cases} \quad (12)$$

with $0 \leq \rho \leq 1$ is the preselected forgetting, it may be selected according to the real processes. For fast changing processes, a smaller ρ should be selected, and vice versa. As that pointed out in the paper (Zhou et al., 1993), $\lambda(k+1)$ is insensitive to the value of ρ .

2.2 Strong tracking finite-difference extended Kalman filter

Deriving the ideas in papers (Fan et al., 2006; Zhou et al., 1997), the authors proposed a finite-difference method to replace partial derivatives of nonlinear functions. From further improving the self-covariance and between-covariance, we obtain the algorithm based on strong tracking filter-difference enhanced kalman filter.

We adopt cholesky to decompose $Q_k, R_k, \bar{P}_K, \hat{P}_k$,

$$\begin{aligned} Q_k &= S_v S_v^T, R_k = S_w S_w^T, \\ \bar{P}_k &= \bar{S}_x \bar{S}_x^T, P_k = \hat{S}_x \hat{S}_x^T. \end{aligned} \quad (13)$$

central difference of partial derivative in nonlinear function $F_x(k)$:

$$F_x(k) = \{f_{ij}\} = \left\{ \left(f_i(x_{k,j} + \Delta x_{k,j}, u_k, q_k) - f_i(x_{k,j} - \Delta x_{k,j}, u_k, q_k) \right) / 2\Delta x_{k,j} \right\} \quad (14)$$

Where $\Delta \hat{x}_{k,j} = h \hat{s}_{x,j}$, h is the step adjustment coefficient; $\hat{s}_{x,j}$ represents the j column of \hat{S}_x , then

$$F_x(k) \hat{S}_x = S_{x\bar{x}} = \left\{ \left(f(\hat{x}_k + h s_{x,j}, u_k, q_k) - f_i(\hat{x}_k + h s_{x,j}, u_k, q_k) \right) / 2h \right\}. \quad (15)$$

$$F_v(k) S_v = S_{xv} = \left\{ \left(f_i(\hat{x}_k, u_k, q_k + h s_{v,j}) - f_i(\hat{x}_k, u_k, q_k - h s_{v,j}) \right) / 2h \right\}, \quad (16)$$

$$G_x(k) \bar{S}_x = S_{y\bar{x}} = \left\{ \left(g_i(\bar{x}_k + h \bar{s}_{x,j,rk}) - g_i(\bar{x}_k - h \bar{s}_{x,j,rk}) \right) / 2h \right\}, \quad (17)$$

$$G_w(k) S_w = S_{yw} = \left\{ \left(g_i(\bar{x}_k, rk + h s_{w,j}) - g_i(\bar{x}_k, rk - h s_{w,j}) \right) / 2h \right\} \quad (18)$$

The predicted covariance matrix, gain matrix and covariance estimate of suboptimal fading extended Kalman filter (SFEKF) are mended as follows

$$\begin{aligned} \bar{P}_{k+1} &= \lambda(k+1) F_x(k) \hat{P}_k F_x(k)^T + F_v(k) Q_k F_v(k)^T = \\ &\lambda(k+1) F_x(k) \hat{S}_x \hat{S}_x^T F_x(k)^T + F_v(k) \hat{S}_v \hat{S}_v^T F_v(k)^T = \\ &\lambda(k+1) S_{xx} S_{xx}^T + S_{xv} S_{xv}^T; \end{aligned} \quad (19)$$

$$\begin{aligned} K_{k+1} &= \bar{P}_k G_x(k)^T \left[G_x(k) \bar{P}_k G_x(k)^T + G_w(k) R_k G_w(k)^T \right]^{-1} = \\ \bar{S}_x \bar{S}_x^T (S_{y\bar{x}} S_{y\bar{x}}^{-1})^T [S_{y\bar{x}} S_{y\bar{x}}^T + S_{yw} S_{yw}^{-T}]^{-1} &= \bar{S}_x S_{y\bar{x}}^T [S_{y\bar{x}} S_{y\bar{x}}^T + S_{yw} S_{yw}^{-T}]^{-1}; \end{aligned} \quad (20)$$

$$\begin{aligned} \hat{P}_{k+1} &= \\ [I - K_{k+1} G_x(k) \bar{P}_{k+1}] &= \\ \bar{S}_x \bar{S}_x^T - K_{k+1} G_x(k) \bar{S}_x \bar{S}_x^T &= \\ \bar{S}_x \bar{S}_x^T - \bar{S}_x \bar{S}_{y\bar{x}}^T K_{k+1}^T - K_{k+1} \bar{S}_{y\bar{x}}^T \bar{S}_x^T + \bar{S}_x \bar{S}_{y\bar{x}}^T K_{k+1}^T &= \\ \bar{S}_x \bar{S}_x^T - \bar{S}_x \bar{S}_{y\bar{x}}^T - K_{k+1} \bar{S}_{y\bar{x}}^T \bar{S}_x^T + & \\ K_{k+1} \bar{S}_{y\bar{x}}^T \bar{S}_{y\bar{x}}^T K_{k+1}^T + K_{k+1} S_{yw} S_{yw}^T K_{k+1}^T &= \\ [\bar{S}_x - K_{k+1} \bar{S}_{y\bar{x}} K_{k+1} S_{yw}] \times [\bar{S}_x - K_{k+1} \bar{S}_{y\bar{x}} K_{k+1} S_{yw}]^T & \end{aligned} \quad (21)$$

From before-mentioned deduction, we can infer to that all calculations of above include the process noise impact and the error problem of model linearization. The step number which nonlinear function is linearized also changes with last time covariance matrix, process noise and observation noise. The filter becomes very simple because of replacing partial derivatives calculation using finite-difference value. The new strong finite-difference Kalman filter (STFDEKF) has more accuracy and covariance estimation, and improves the

robustness of target tracking. The last experiment results show that the STFDEKF can be used for the high nonlinear stochastic systems such as eye tracking.

3. STFDEKF based eye tracking and results

In this section, we develop the following eye tracking using STFDEKF. Because the eye motion is the high nonlinearity of the likelihood model, it's very difficult to model human eye movement dynamics. In our tracking system, the following nonlinear equations are used to model the eye movement dynamics.

$$x = x_0 + vt + \frac{1}{2}at^2 \tag{22}$$

$$\dot{x}_{k+1} = v_0 + A_k \sin(\omega_k t) \tag{23}$$

$$a_{k+1} = \ddot{x}_{k+1} = A_k \omega_k \cos(\omega_k t) \tag{24}$$

where, the initial value x_0 and v_0 are zero. The acceleration a follows the sine distribution, and a will be considered process noise (v_k), respectively $A_k = 0.08m/s$ and $\omega_k = \pi rad/s$. The proposed eye tracking experiment is developed in platform of OPEN CV. Our system uses a ViewQuest VQ680 video camera to capture human images. The experiment is tested on a Pentium III 1.7G CPU with 128MB RAM. Eye tracking based on the proposed method can reach 10 frames per second. The format of input video is 352×288. Fig.1 represents the eye tracking using STFDEKF algorithm. The Correct Rate of eye tracking is shown in Table.1.



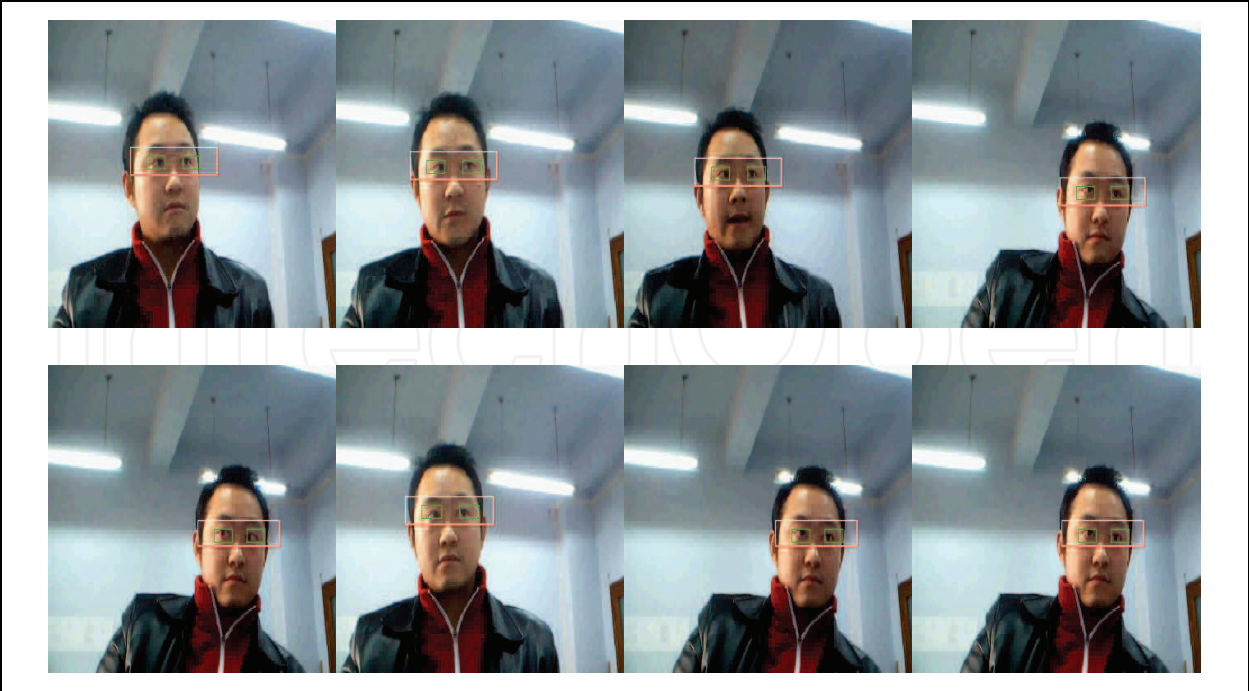


Fig. 1. Eye tracking using STFDEKF algorithm

	Video 1 (without glasses)	Video2 (glasses)	Video3(long hair)
Total Frames	1999	2941	2889
Tracking Failure	9	16	18
Correct Rate	99.45%	99.35%	99.4%
Average Correct Rate	99.4%		

Table 1. Result of eye tracking using STFDEKF algorithm

Correct Rate of eye tracking is defined as in equation (25).

$$Correct\ Rate = \frac{Total\ Frames - Tracking\ Failure}{Total\ Frames}$$

(25)

The following experimental results evaluate the performance of our proposed method and other eye tracking methods.

Algorithm	Correct rate	remark
Templates Match	99.1%	Refer to (Horng et al., 2004)
Kalman and mean shift algorithm	99.1%	Refer to (Zhu et al., 2002)
EKF tracking algorithm	99%	
STFDEK algorithm in this paper	99.4%	Refer to Table.1

Table 2. Comparison of eye tracking algorithms

In order to qualitatively gauge performance and discuss resulting issues, we consider using the traditional measures of performance: the RMSE (Root Mean Square Error) and MSE (Mean Square Error). The simulation results of RMSE and MSE are depicted in Table 3.

Algorithm	RMSE	MSE
Kalman Filter algorithm	0.13155	0.164661
EKF tracking algorithm	0.1222	0.0904
STFDEK algorithm in this paper	0.0989	0.0780

Table 3. RMSE and MSE of eye tracking filtering algorithms

The results of above experiments indicate that the proposed method has better performance. So we can use STFDEK algorithm for eyes tracking.

4. Conclusion

This paper proposes a new eye tracking method using strong finite-difference Kalman filter. Firstly, strong tracking factor is introduced to modify priori covariance matrix to improve the accuracy of the eye tracking algorithm. Secondly, the finite-difference method is proposed to replace partial derivatives of nonlinear functions to eye tracking. From above deduction, the new strong finite-difference Kalman filter becomes very simple because of replacing partial derivatives calculation using finite-difference value. The last experiment results show that STFDEKF has more accuracy and covariance estimation, improves the robustness of target tracking, and can be used for the high nonlinear stochastic systems such as eye tracking.

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Kalman Filter

Edited by Vedran Kordic

ISBN 978-953-307-094-0

Hard cover, 390 pages

Publisher InTech

Published online 01, May, 2010

Published in print edition May, 2010

The Kalman filter has been successfully employed in diverse areas of study over the last 50 years and the chapters in this book review its recent applications. The editors hope the selected works will be useful to readers, contributing to future developments and improvements of this filtering technique. The aim of this book is to provide an overview of recent developments in Kalman filter theory and their applications in engineering and science. The book is divided into 20 chapters corresponding to recent advances in the field.

How to reference

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Zutao Zhang and Jiashu Zhang (2010). Application of a Strong Tracking Finite-Difference Extended Kalman Filter to Eye Tracking, Kalman Filter, Vedran Kordic (Ed.), ISBN: 978-953-307-094-0, InTech, Available from: <http://www.intechopen.com/books/kalman-filter/application-of-a-strong-tracking-finite-difference-extended-kalman-filter-to-eye-tracking>

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