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# Strength Analysis and Variation of Elastic Properties in Plantain Fiber/Polyester Composites for Structural Applications

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## Abstract

Plantain fiber-reinforced composite materials have demonstrated significant properties that are applicable in structural design and development. However, two major concerns arise in relation to the obvious material anisotropy and challenges imposed by structural discontinuity encountered as need for use of fasteners arises. The study assesses the extent of variation of elastic properties ( $E_x$ ,  $E_y$ ,  $G_{xy}$ ,  $\nu_{xy}$ ,  $\nu_{yx}$ ,  $m_x$ ,  $m_y$ ) with fiber orientation using MATLAB functions while considering the extent of variation of the tangential stresses around an idealized functional hole edge. The tensile strength of 410.15 and 288.1 MPa was recorded at  $0^\circ$  fiber orientation angle, while 37.3397 and 33.133 MPa were obtained at fiber orientation angle of  $90^\circ$  for Plantain Empty Fruit Bunch Fiber Composite (PEFBFC) and Plantain Pseudo Stem Fiber Composite (PPSFC), respectively. The tangential stress distribution at hole edge indicated maximum stress value of 119.15 and 100.587 MPa at angular position  $\theta = 90^\circ$  for PEFBFC and PPSFC, respectively. Judging from various failure indices considered, failure will be initiated at  $\theta = 70^\circ$  for PEFBFC with stress concentration factor of 2.53 and  $\theta = 65^\circ$  for PPSFC with stress concentration factor of 2.13, which are less than the stress concentration around the peak stress when angular position is  $90^\circ$ . Both PEFBFC and PPSFC showed similar trends in response to the design scenario considered.

**Keywords:** elastic properties, structural application, plantain fiber, composites, matrix

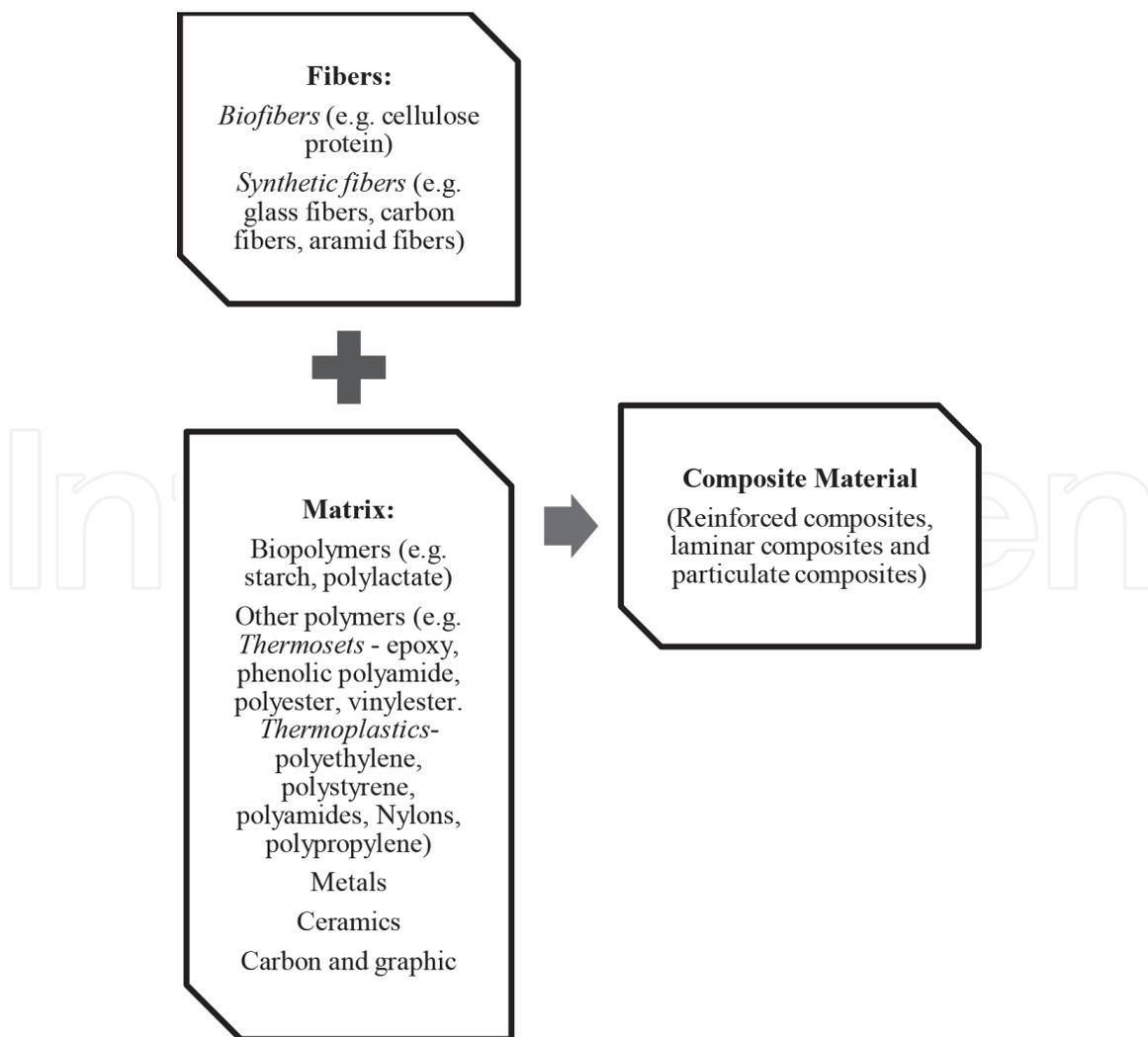
## 1. Introduction

These days several shortcomings have been observed with respect to the utilization of synthetic fiber-reinforced polymers, hence empowering the drive for more utilization of plant fiber composite in structural designs. The primary weaknesses of synthetic fiber-reinforced polymers which includes issue in afterlife disposal and non-biodegradability are completely settled by utilizing plant fibers in polymer reinforcements. Reinforced composites are prime choice for light weight structural designs and automotive body parts assembly.

Extensive literature on recent advancements in reinforced composites and its reliability are reported in classical reports of Dehmous et al. [1], Okafor et al. [2],

Xie and Wang [3], Beaumont et al. [4], Pei et al. [5], Bittrich et al. [6], Prasad et al. [7], Wang et al. [8]. The hygrothermal efficiencies has been reported by Foulc et al. [9], Shettar et al. [10]. In addition, the utilization of reinforced composites predi- cates the reuse of domestic and agricultural residues. For example, vehicles made with fiber-reinforced composites are lighter and run on smaller engines which produce fewer emissions to the environment. Most items produced using natural fiber composites is a win-win for manufacturers. Most composite material ventures can utilize their genius green item data to build deals because customers comprehend the ecological dangers of synthetic assembling.

Due to scarcely available information regarding some new material response to structural discontinuity, superior properties of those composites are seriously compromised by the utilization of bizarrely enormous factor of safety in design. Accordingly, the quick fate of composite materials as a class of innovative materials may depend more on clear assessment of its performance in various structural design scenario. All inclusive acknowledgment of composites as eco-friendly mate- rials will therefore depend especially on the certainty of the designer and client about the variation of its elastic properties. In a typical fiber-reinforced composites, the polymer matrix serves as a binder and deforming most times for stress distri- bution purposes. There are different options in the choice of matrix/fibers and the general composition of reinforced composites is shown in **Figure 1**. The figure identified the three major categories of polymers to include biopolymers, thermo- plastics and thermosets. Biopolymers are chain like atoms created by organic



**Figure 1.**  
*Composition of reinforced composites.*

biomass. Exceptional nontoxicity and biodegradable properties of biopolymers boosts their applications in composites formulation, hardware and restorative gadgets. Fuse of nano-sized support in the biopolymers to improve the properties contributes to the upgrade functional applications of the matrix.

Though thermosets and thermoplastics sound similar, they have very different properties and applications [11]. Thermosets typically changes from fluid to solid state after curing chemical reaction initiated by addition of a catalyst, cross-linker, and curing agent. In the course of the chemical reaction, the material solidifies as a result of cross-linking and formation of longer molecular networks. Subsequently, any further exposure to high heat will cause the material to degrade unlike thermoplastic parts that melts and softens whenever exposed to elevated temperature, thermoset simply become set in their physical and mechanical properties after an initial treatment and therefore are no longer affected by additional heat exposure.

Again, thermoplastics are dissolvable plastics. At temperature above liquefying point, the thermoplastic condenses. The thermoplastic sets once again into solid state when the temperature is reduced and the handling temperature dips under its melting point. This inherent characteristic of thermoplastics enables its softening when heated above its melting point and re-forming as the temperature decreases below the melting point. Most of the times, the expenses of materials for creating thermoset are lower when contrasted with thermoplastic. Also thermoset is regularly simple for wetting the reinforcements and shaping last composites items. Thermoplastics will in general be harder than thermosets and require no refrigeration as uncured thermosets as often as possible do, and can be more effectively be reused and fixed. Elastomers are typically thermosets (requiring vulcanization).

Obviously literature has indicated several approximate relationships between some reinforced composites elastic constants and the homogenized modules of elasticity [12–14]. Also recent research have reported the possibility of measuring variation elastic constants of materials using ultrasonic methods [15–18]. However, scanty research is available on strength analysis and variation of elastic properties in plantain fiber/polyester composites, a gap that the present study seeks to fill.

## **2. Background to plantain cultivation and utilization as reinforcement in polymer composites**

An expanded enthusiasm for the utilization of agricultural wastes in development of reinforced composites has been on the increase. Natural fibers extracted from bio wastes offer a few points of interest over woody biomass, since they are accessible in huge amounts as leftovers and agricultural wastes [19, 20]. The plantain pseudo stem (PPS) and empty fruit bunch (EFB) strands presented in this chapter are agricultural by-products that are biodegradable and locally available from renewable agricultural sources with potentials to contribute to reduction in environmental pollution when utilized in large scale as polymeric reinforcements.

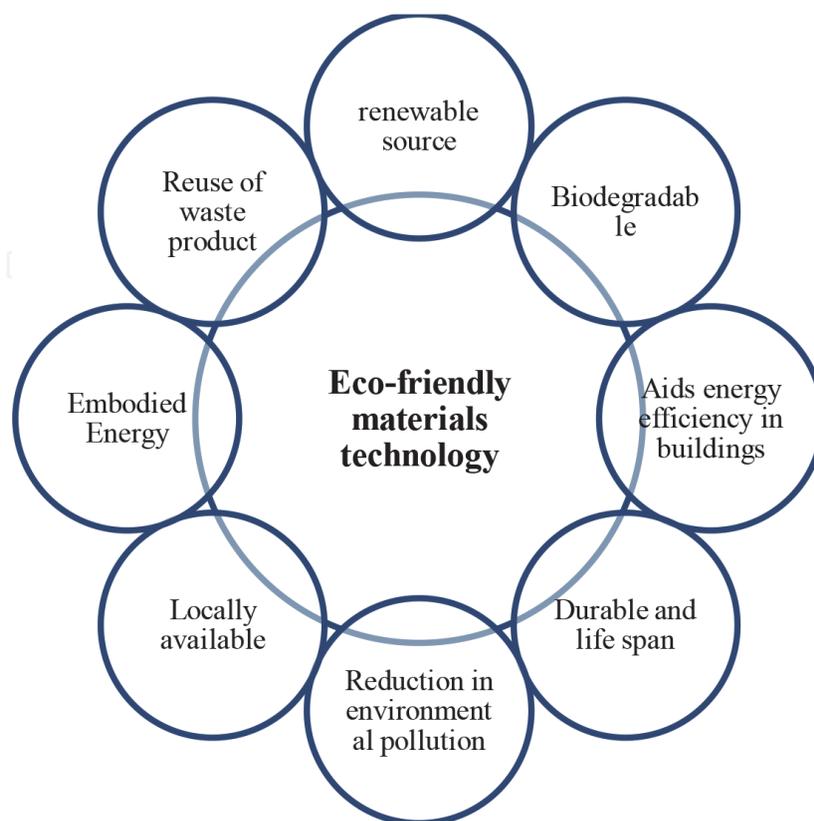
Plantain fruit is one of the staples in Nigeria and it is mainly cultivated in the tropics and ethnic enclaves [21]. It is evaluated that 70 million individuals in West and Central Africa derive most of their nourishment and vitality requirements from plantain fruit plant [22, 23]. Plantain fruit has a fare potential in the light of its huge cultivation and consumption in Nigeria and many other African countries.

Akinyemi et al. [24] reported that plantain plant is the third most important plant grown after cassava and yam in Nigeria; collaborating, Kaine and Okoje [25] showed that plantain production is a very profitable enterprise as every ₦1 naira invested in plantain production yields a return on investment of about ₦12.60 kobo. In a study about economics of plantain production Kainga et al. [26] found that the

associated high return on investment and short maturity period for plantain contributes to its massive cultivation in Nigeria.

Africa cultivates over 50% of worldwide production of plantain and Nigeria is one of the biggest plantain producing nations in the planet. Therefore the interest in plantain plant fiber for polymer reinforcement was as a result of its abundance and accessibility as it is evaluated that over 15.07 million tons of plantain fruit is produced each year in Nigeria with about 2.4 million metric tons produced from southern Nigeria [27, 28]. Plantain fiber also satisfied over 50% conditions for eco-friendly materials as shown in **Figure 2** and can make strong reinforcement in composites. A composite which can be characterized as a physical blend of at least two unique materials, has properties that are commonly superior to those of any of the establishing materials. It is important to utilize blends of materials to tackle issues in light of the fact that any one material alone cannot suffix effectively in eco-friendly materials technology at an acceptable performance [29].

Cadena Ch et al. [30] and Adeniyi et al. [31] orchestrated the potentials of natural fibers from plantain pseudo stem for use in fiber-reinforced composites. It is therefore important to assess the extent of variation of elastic properties in plantain fiber-reinforced polyester composites to guard against out of plane failure during structural applications. Unfortunately most studies involving plantain fiber-reinforced composites has dwelt on assessment of tensile, flexural and hardness properties [32], optimization of hardness strengths [33], effect of water and organic extractives removal [34], effects of fiber extraction techniques [35], optimization of flexural strength [36], compressive and impact strength evaluation [37–39], effect of high-frequency microwave radiation [40], effect of chemical treatment on the morphology [41], implications of interfacial energetics on mechanical strength [42]. Although Ihueze, Okafor and Okoye [43] has reported the longitudinal (1) and transverse (2) properties of plantain fiber-reinforced composites in **Figure 1**, there is still need to



**Figure 2.**  
*Properties of eco-friendly building materials.*

establish the essential elastic constants at directions other than the material axis directions 1–2.

The present research efforts will further drive the interests of structural designers in the use of plantain fiber-reinforced composites because the superior strength of materials are rarely utilized to full as a result of incomplete knowledge of elastic properties which are related to various fundamental solid-state characteristics of the composites. In essence, the elastic constants of plantain fiber-reinforced composites is expected to describe the material response to external stressor and provide useful information about bonding characteristics and structural stability. Kenedi et al. [44] assessed the orthotropic elastic properties in a sandwiched composites laminates and proposed models for estimating the orthotropic elastic properties of composite materials. Hwang and Liu [45] reported that elastic modulus and Poisson's ratio vary significantly with different braid angles in carbon fabric/polyurethane composites. Ren et al. [46] reported that elastic modulus and tensile strengths are overly dependent on the angles of fiber orientation. Kumar et al. [47] studied the influence of  $\pm 0^\circ$ ,  $\pm 10^\circ$ ,  $\pm 30^\circ$ ,  $\pm 40^\circ$ ,  $\pm 45^\circ$ ,  $\pm 55^\circ$ ,  $\pm 65^\circ$ ,  $\pm 75^\circ$ , and  $\pm 90^\circ$  angle ply on mechanical properties of glass-polyester composite laminate and found that that glass/polyester with  $0^\circ$  fiber orientation angle yields' high strength. Cordin et al. [48] experimentally examined the effect of  $0^\circ$ ,  $\pm 22.5^\circ$ ,  $\pm 45^\circ$ ,  $\pm 67.5^\circ$  and  $90^\circ$  fiber orientation angles on the mechanical properties of polypropylene-lyocell composites. Ihueze et al. [49] optimally determined the tensile strengths of plantain fiber-reinforced composites considering  $30^\circ$ ,  $45^\circ$  and  $90^\circ$  fiber orientation angles. The application of these previous studies are limited to fiber orientation angles studied, however failure may be initiated from angles other than those considered hence the need to verify the variation of important elastic constants within a wide range of fiber orientation coverage are necessary.

Additionally, researchers have provided various theoretical strategies for determination of elastic constants in reinforced composites using software codes to cover the wide range of fabricating conditions. Jules et al. [50] ascertained the effect of fibers orientation on the predicted elastic properties of long fiber composites using Monte-Carlo simulation to assign the in plane and out of plane orientation values. Venetis and Sideridis [51] developed a model to find the approximate elastic constants in unidirectional fiber-reinforced composite materials in terms of the constituent material properties. Cuartas [52] theoretically determined the elastic properties in CFRP composites which compared favorably with other methods based on tensile tests and ultrasonic characterization. Rahmani et al. [12] found that MATLAB codes are capable of predicting the elastic constants of composites with reasonable confidence.

### **3. Mathematical framework for assessment of extent of variation of elastic properties in plantain fiber-reinforced polyester composites**

One significant property of composite materials is their plainly visible macroscopic anisotropy, which means that the properties estimated in the longitudinal direction are by far not the same as those measured in transverse direction. There are no material planes of symmetry, and normal loads create both normal strains and shear strains. This anisotropic characteristic of reinforced composites results in low mechanical properties in the out-of-plane orientation where the matrix carries the primary load. Consequently the application of reinforced composites is limited in scenarios prone to complex load paths such as lugs and fittings [53].

By implication any endeavor to comprehend the structural application of plantain fiber-reinforced polyester composite must assess the inborn anisotropy.

Composites are a subclass of anisotropic materials that are delegated orthotropic. Orthotropic materials have properties that are unique in three directions with perpendicular axes of symmetry. In this way, orthotropic mechanical properties depend heavily on fiber orientation. An orthotropic ply is thus defined as that having two different material properties in two mutually perpendicular directions at a point and the two mutually perpendicular directions also form the planes of material properties symmetry at the point.

### 3.1 Determination of reduced stiffness matrix and compliance matrix

Considering two possible loading conditions of longitudinal (direction 1) and transverse (direction 2) in the matrix as shown in **Figure 3**, the resulting direct strains from Hooks law are respectively  $e_1 = \frac{-v_{21}\sigma_1}{E_1}$  and  $e_2 = \frac{-v_{12}\sigma_1}{E_1}$  where  $v_{12}$  = major Poisson's ratio and  $v_{21}$  = minor Poisson's ratio.

Hence the application of both direct stresses  $\sigma_1$  and  $\sigma_2$  will yield corresponding strains as follows:

$$e_1 = \frac{\sigma_1}{E_1} - \frac{v_{21}\sigma_2}{E_2} \quad (1)$$

$$e_2 = \frac{\sigma_2}{E_2} - \frac{v_{12}\sigma_1}{E_1} \quad (2)$$

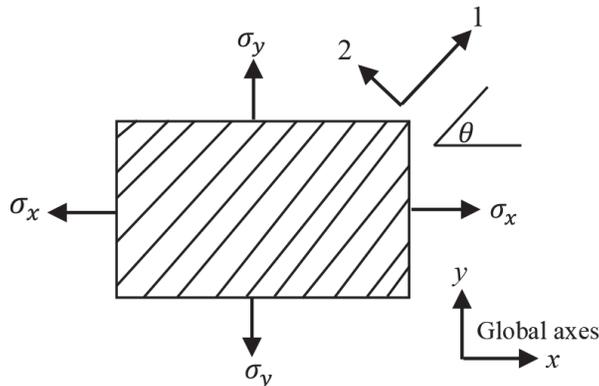
Putting Eqs. (1) and (2) in a matrix form, yields

$$\begin{Bmatrix} e_1 \\ e_2 \end{Bmatrix} = \begin{Bmatrix} \frac{1}{E_1} & \frac{-v_{21}}{E_2} \\ \frac{-v_{12}}{E_1} & \frac{1}{E_2} \end{Bmatrix} \begin{Bmatrix} \sigma_1 \\ \sigma_2 \end{Bmatrix} \quad (3)$$

$$\begin{Bmatrix} \sigma_1 \\ \sigma_2 \end{Bmatrix} = \begin{Bmatrix} \frac{E_1}{1 - v_{12}v_{21}} & \frac{v_{21}E_1}{1 - v_{12}v_{21}} \\ \frac{v_{12}E_2}{1 - v_{12}v_{21}} & \frac{E_2}{1 - v_{12}v_{21}} \end{Bmatrix} \begin{Bmatrix} e_1 \\ e_2 \end{Bmatrix} \quad (4)$$

Eq. (3) is symmetric about the loading diagonal such that

$$\frac{-v_{21}}{E_2} = \frac{-v_{12}}{E_1} \quad (5)$$



**Figure 3.** Stressed single thin composite lamina. From Ref. [43].

A combined effect of shear and direct stresses gives the reduced stiffness matrix as in Eq. (6) and reduced compliance matrix as in Eq. (7)

$$\begin{Bmatrix} \sigma_1 \\ \sigma_2 \\ \tau_{12} \end{Bmatrix} = \begin{pmatrix} \frac{E_1}{1 - \nu_{12}\nu_{21}} & \frac{\nu_{21}E_1}{1 - \nu_{12}\nu_{21}} & 0 \\ \frac{\nu_{12}E_2}{1 - \nu_{12}\nu_{21}} & \frac{E_2}{1 - \nu_{12}\nu_{21}} & 0 \\ 0 & 0 & G_{12} \end{pmatrix} \begin{Bmatrix} e_1 \\ e_2 \\ e_{12} \end{Bmatrix} \quad (6)$$

$$\begin{Bmatrix} e_1 \\ e_2 \\ e_{12} \end{Bmatrix} = \begin{pmatrix} \frac{1}{E_1} & \frac{-\nu_{21}}{E_2} & 0 \\ \frac{-\nu_{21}}{E_1} & \frac{1}{E_2} & 0 \\ 0 & 0 & \frac{1}{G_{12}} \end{pmatrix} \begin{Bmatrix} \sigma_1 \\ \sigma_2 \\ \tau_{12} \end{Bmatrix} \quad (7)$$

Minor Poisson's ratio is the strain resulting from a stress in the axial direction, Ihueze et al. (2013) calculated the major Poisson's ratio  $\nu_{12}$  for plantain fiber/polyester composites. However, there is need to further assess the minor Poisson's ratio  $\nu_{21}$  using Eq. (5) and **Table 1** as follows

$$\begin{aligned} \nu_{21, \text{PEFBFRP}} &= \frac{E_2\nu_{12}}{E_1} = \frac{7030.962 * 0.38}{14,922} = 0.179 \\ 1 - \nu_{12}\nu_{21} &= 1 - 0.38 * 0.179 = 1 - 0.068 = 0.93 \\ \nu_{21, \text{PPSFC}} &= \frac{E_2\nu_{12}}{E_1} = \frac{6817.175 * 0.29}{13027.5} = 0.152 \\ 1 - \nu_{12}\nu_{21} &= 1 - 0.29 * 0.152 = 1 - 0.044 = 0.956 \end{aligned}$$

The reduced stiffness matrix ( $\mathfrak{N}$ ) for PEFBFC and PPSFC is obtained from Eq. (6).

For PEFBFC

$$\begin{aligned} \frac{E_1}{1 - \nu_{12}\nu_{21}} &= \frac{14922}{1 - 0.38 * 0.179} = 16011.07 \\ \frac{\nu_{21}E_1}{1 - \nu_{12}\nu_{21}} &= 0.179 * 16011.07 = 2865.98 \\ \frac{E_2}{1 - \nu_{12}\nu_{21}} &= \frac{7030.962}{1 - 0.38 * 0.179} = 7544.113 \end{aligned}$$

| Composites | Properties        |                   |                |                |                |              |            |                        |                   |
|------------|-------------------|-------------------|----------------|----------------|----------------|--------------|------------|------------------------|-------------------|
|            | $S_{u1}$<br>(MPa) | $S_{u2}$<br>(MPa) | $S_y$<br>(MPa) | $E_1$<br>(MPa) | $E_2$<br>(MPa) | $E$<br>(MPa) | $\nu_{12}$ | $\tau_{\max}$<br>(MPa) | $G_{12}$<br>(MPa) |
| PEFBFC     | 410.15            | 37.3397           | 33.69          | 14,922         | 7030.962       | 9990.10      | 0.38       | 19.3100                | 3622.99           |
| PPSFC      | 288.10            | 33.1330           | 29.24          | 13027.5        | 6817.175       | 9146.305     | 0.29       | 15.5700                | 3332.835          |

$S_{u1}, S_{u2}$  are tensile strengths in the longitudinal and transverse directions respectively.

**Table 1.** Evaluated mechanical properties of plantain fibers and plantain fibers reinforced polyester composites. From Ref. [43].

$$\mathfrak{N}_{\text{PEFBFC}} = \left\{ \begin{array}{ccc} 16011.07 & 2865.98 & 0 \\ 2865.98 & 7544.113 & 0 \\ 0 & 0 & 3622.99 \end{array} \right\} \text{MPa}$$

For PPSFC

$$\frac{E_1}{1 - \nu_{12}\nu_{21}} = \frac{13027.5}{1 - 0.29 * 0.152} = 13628.23$$

$$\frac{\nu_{21}E_1}{1 - \nu_{12}\nu_{21}} = 0.152 * 13628.23 = 2071.49$$

$$\frac{E_2}{1 - \nu_{12}\nu_{21}} = \frac{6817.175}{1 - 0.29 * 0.152} = 7131.53$$

$$\mathfrak{N}_{\text{PPSFC}} = \left\{ \begin{array}{ccc} 13628.23 & 2071.49 & 0 \\ 2071.49 & 7131.53 & 0 \\ 0 & 0 & 3332.835 \end{array} \right\} \text{MPa}$$

The reduced compliance matrix ( $\beta$ ) is obtained from Eq. (7).

For PEFBFC

$$\frac{1}{E_1} = \frac{1}{14922} = 6.7 \times 10^{-5} 1/\text{MPa}$$

$$\frac{-\nu_{21}}{E_2} = \frac{-0.179}{7030.962} = -2.5 \times 10^{-5} 1/\text{MPa}$$

$$\frac{1}{E_2} = \frac{1}{7030.962} = 1.4 \times 10^{-4} 1/\text{MPa}$$

$$\frac{1}{G_{12}} = \frac{1}{3622.99} = 2.8 \times 10^{-4} 1/\text{MPa}$$

$$\beta_{\text{PEFBFC}} = \left\{ \begin{array}{ccc} 6.7 \times 10^{-5} & -2.5 \times 10^{-5} & 0 \\ -2.5 \times 10^{-5} & 1.4 \times 10^{-4} & 0 \\ 0 & 0 & 2.8 \times 10^{-4} \end{array} \right\} 1/\text{MPa}$$

For PPSFC

$$\frac{1}{E_1} = \frac{1}{13027.5} = 7.7 \times 10^{-5} 1/\text{MPa}$$

$$\frac{-\nu_{21}}{E_2} = \frac{-0.152}{6817.175} = -2.2 \times 10^{-5} 1/\text{MPa}$$

$$\frac{1}{E_2} = \frac{1}{6817.175} = 1.5 \times 10^{-4} 1/\text{MPa}$$

$$\frac{1}{G_{12}} = \frac{1}{3332.835} = 3.0 \times 10^{-4} 1/\text{MPa}$$

$$\beta_{\text{PPSFC}} = \left\{ \begin{array}{ccc} 7.7 \times 10^{-5} & -2.2 \times 10^{-5} & 0 \\ -2.2 \times 10^{-5} & 1.5 \times 10^{-4} & 0 \\ 0 & 0 & 3.0 \times 10^{-4} \end{array} \right\} 1/\text{MPa}$$

| Property                                 | Polyester resin                   |
|--|-----------------------------------|
| Density (g/cm <sup>3</sup> )             | 1.2–1.5 (1400 kg/m <sup>3</sup> ) |
| Young modulus (MPa)                      | 2000–4500                         |
| Tensile strength (MPa)                   | 40–90                             |
| Compressive strength (MPa)               | 90–250                            |
| Tensile elongation at break (%)          | 2                                 |
| Water absorption 24 h at 20°C            | 0.1–0.3                           |
| Flexural modulus (GPa)                   | 11.0                              |
| Poisson's ratio                          | 0.37–0.38                         |
| <b>Plantain pseudo stem fibers</b>       |                                   |
| Young modulus (MPa)                      | 23,555                            |
| UTS (MPa)                                | 536.2                             |
| Strain (%)                               | 2.37                              |
| Density (kg/m <sup>3</sup> )             | 381.966                           |
| <b>Plantain empty fruit bunch fibers</b> |                                   |
| Young modulus (MPa)                      | 27,344                            |
| UTS (MPa)                                | 780.3                             |
| Strain (%)                               | 2.68                              |
| Density (kg/m <sup>3</sup> )             | 354.151                           |

**Table 2.**  
 Mechanical properties of plantain fibers and polyester resin. From Ref. [43].

### 3.2 Transformation of elastic constants

The know of the stress-strain relationship in the plantain/polyester composite is completely comprehended by knowing the associated independent engineering elastic constants ( $E_1$ ,  $E_2$ ,  $G_{12}$  and  $\nu_{12}$ ) as previously determined by Ihueze et al. (2013) as in **Tables 1** and **2**. However, there is need to further establish these elastic properties at different directions of fibers other than directions 1 and 2. Datoo [54] derived various expressions for determination of the elastic properties in the reference axes  $x$ - $y$  for any fiber orientation as expressed in Eqs. (8)–(14) where  $c = \cos\theta$ ,  $s = \sin\theta$ ,  $E_x$ ,  $E_y$ ,  $G_{xy}$ ,  $\nu_{xy}$ ,  $m_x$  and  $m_y$  are the elastic properties at any fiber orientation  $\theta$  relative to a reference direction  $x$ - $y$ .

$$\frac{1}{E_x} = \frac{c^4}{E_1} + \frac{s^4}{E_2} + c^2s^2 \left( \frac{1}{G_{12}} - \frac{2\nu_{12}}{E_1} \right) \quad (8)$$

$$\frac{1}{E_y} = \frac{s^4}{E_1} + \frac{c^4}{E_2} + c^2s^2 \left( \frac{1}{G_{12}} - \frac{2\nu_{12}}{E_1} \right) \quad (9)$$

$$\frac{1}{G_{xy}} = c^2s^2 \left( \frac{4}{E_1} + \frac{4}{E_2} + \frac{8\nu_{12}}{E_1} \right) + (c^2 - s^2) \frac{1}{G_{12}} \quad (10)$$

$$\nu_{xy} = E_x \left[ (c^4 + s^4) \frac{\nu_{12}}{E_1} - c^2s^2 \left( \frac{1}{E_1} + \frac{1}{E_2} - \frac{1}{G_{12}} \right) \right] \quad (11)$$

The minor Poissons ratio with respect to the material reference axes is obtained from Eq. (5) such that

$$\frac{v_{xy}}{E_x} = \frac{v_{yx}}{E_y} \quad (12)$$

$$m_x = E_x \left[ c^3 s \left( \frac{1}{G_{12}} - \frac{2v_{12}}{E_1} - \frac{2}{E_1} \right) - c s^3 \left( \frac{1}{G_{12}} - \frac{2v_{12}}{E_1} - \frac{2}{E_2} \right) \right] \quad (13)$$

$$m_y = E_y \left[ c s^3 \left( \frac{1}{G_{12}} - \frac{2v_{12}}{E_1} - \frac{2}{E_1} \right) - c^3 s \left( \frac{1}{G_{12}} - \frac{2v_{12}}{E_1} - \frac{2}{E_2} \right) \right] \quad (14)$$

### 3.3 Variation of engineering elastic constants with fiber orientation $\theta$

Considering fiber orientation  $\theta^\circ$  ranging from  $0^\circ$  to  $90^\circ$  in increments of  $5^\circ$  the variation of  $E_x$ ,  $E_y$ ,  $G_{xy}$ ,  $v_{xy}$ ,  $m_x$  and  $m_y$  has been assessed Plantain Empty Fruit Bunch Fiber Composite (PEFBFC) and Plantain Pseudo Stem Fiber Composite (PPSFC) using Eqs. (8)–(14) and presented in **Tables 3** and **4**, respectively.

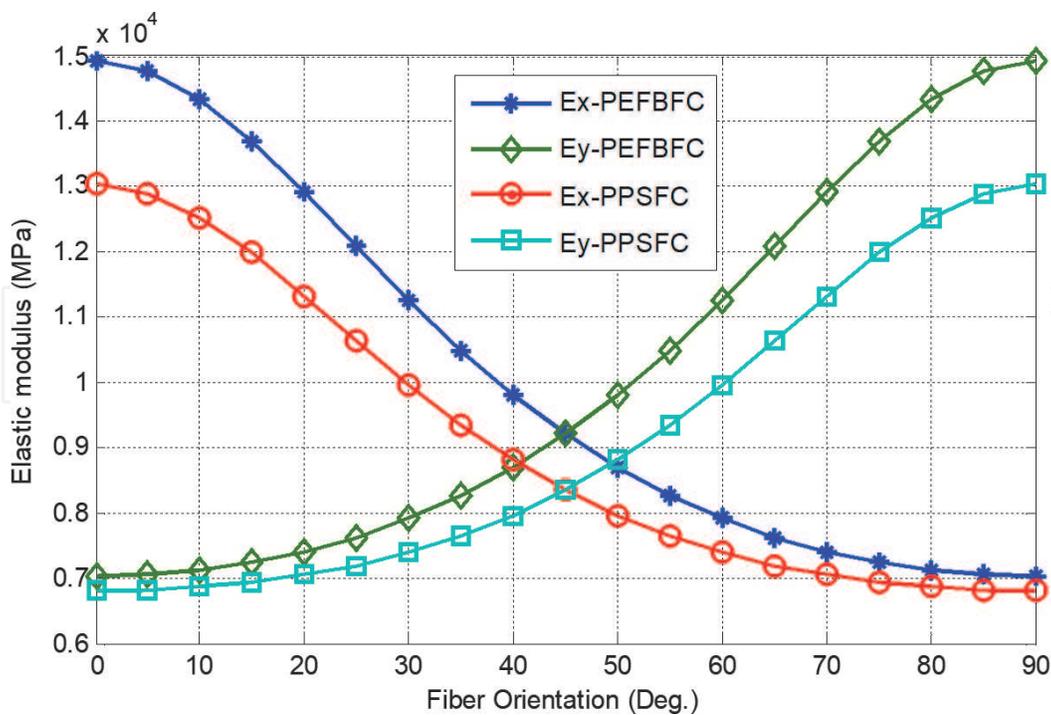
**Figure 4** shows the variation of elastic modulus with fiber orientation, it can be seen that the highest value of 14,922 and 13027.5 MPa in the reference  $x$ -direction ( $E_x$ ) is attained in the fiber orientation angle  $0^\circ$  for PEFBFC and PPSFC respectively. However as fiber orientation angle changes, there is a sharp drop in the value of elastic modulus in the reference  $x$ -direction to a respective lowest value of 7030.96 and 6817.18 MPa as the fiber orientation angle increased to  $90^\circ$ . On the contrary, the lowest value of 7030.96 and 6817.18 MPa were recorded for elastic modulus in the

| S/N | $\theta^\circ$ | $E_x$     | $E_y$     | $G_{xy}$ | $v_{xy}$ | $v_{yx}$ | $m_x$ | $m_y$ | $\frac{E_x}{E_2}$ | $\frac{G_{xy}}{E_2}$ |
|-----|----------------|-----------|-----------|----------|----------|----------|-------|-------|-------------------|----------------------|
| 1   | 0              | 14922.000 | 7030.962  | 3622.990 | 0.380    | 0.179    | 0.000 | 0.000 | 2.122             | 0.515                |
| 2   | 5              | 14769.770 | 7053.373  | 3629.270 | 0.378    | 0.180    | 0.116 | 0.037 | 2.101             | 0.516                |
| 3   | 10             | 14337.670 | 7121.323  | 3647.477 | 0.372    | 0.185    | 0.221 | 0.073 | 2.039             | 0.519                |
| 4   | 15             | 13690.480 | 7236.950  | 3675.727 | 0.362    | 0.191    | 0.304 | 0.111 | 1.947             | 0.523                |
| 5   | 20             | 12911.620 | 7403.786  | 3710.985 | 0.350    | 0.201    | 0.362 | 0.150 | 1.836             | 0.528                |
| 6   | 25             | 12081.300 | 7626.692  | 3749.256 | 0.336    | 0.212    | 0.395 | 0.190 | 1.718             | 0.533                |
| 7   | 30             | 11262.730 | 7911.712  | 3785.946 | 0.320    | 0.225    | 0.405 | 0.231 | 1.602             | 0.538                |
| 8   | 35             | 10497.990 | 8265.787  | 3816.391 | 0.304    | 0.239    | 0.398 | 0.271 | 1.493             | 0.543                |
| 9   | 40             | 9810.462  | 8696.213  | 3836.528 | 0.288    | 0.255    | 0.377 | 0.310 | 1.395             | 0.546                |
| 10  | 45             | 9209.655  | 9209.655  | 3843.571 | 0.271    | 0.271    | 0.346 | 0.346 | 1.310             | 0.547                |
| 11  | 50             | 8696.213  | 9810.462  | 3836.528 | 0.255    | 0.288    | 0.310 | 0.377 | 1.237             | 0.546                |
| 12  | 55             | 8265.787  | 10497.990 | 3816.391 | 0.239    | 0.304    | 0.271 | 0.398 | 1.176             | 0.543                |
| 13  | 60             | 7911.712  | 11262.730 | 3785.946 | 0.225    | 0.320    | 0.231 | 0.405 | 1.125             | 0.538                |
| 14  | 65             | 7626.692  | 12081.300 | 3749.256 | 0.212    | 0.336    | 0.190 | 0.395 | 1.085             | 0.533                |
| 15  | 70             | 7403.786  | 12911.620 | 3710.985 | 0.201    | 0.350    | 0.150 | 0.362 | 1.053             | 0.528                |
| 16  | 75             | 7236.950  | 13690.480 | 3675.727 | 0.191    | 0.362    | 0.111 | 0.304 | 1.029             | 0.523                |
| 17  | 80             | 7121.323  | 14337.670 | 3647.477 | 0.185    | 0.372    | 0.073 | 0.221 | 1.013             | 0.519                |
| 18  | 85             | 7053.373  | 14769.770 | 3629.270 | 0.180    | 0.378    | 0.037 | 0.116 | 1.003             | 0.516                |
| 19  | 90             | 7030.962  | 14922.000 | 3622.990 | 0.179    | 0.380    | 0.000 | 0.000 | 1.000             | 0.515                |

**Table 3.** Variation of engineering elastic constants with fiber orientation  $\theta$  in PEFBFC.

| S/N | $\theta^\circ$ | $E_x$     | $E_y$     | $G_{xy}$ | $\nu_{xy}$ | $\nu_{yx}$ | $m_x$ | $m_y$ | $\frac{E_x}{E_2}$ | $\frac{G_{xy}}{E_2}$ |
|-----|----------------|-----------|-----------|----------|------------|------------|-------|-------|-------------------|----------------------|
| 1   | 0              | 13027.500 | 6817.175  | 3332.835 | 0.290      | 0.152      | 0.000 | 0.000 | 1.911             | 0.489                |
| 2   | 5              | 12897.620 | 6830.651  | 3343.613 | 0.290      | 0.154      | 0.114 | 0.023 | 1.892             | 0.490                |
| 3   | 10             | 12530.190 | 6872.014  | 3375.039 | 0.291      | 0.159      | 0.214 | 0.047 | 1.838             | 0.495                |
| 4   | 15             | 11983.280 | 6944.024  | 3424.350 | 0.291      | 0.168      | 0.293 | 0.073 | 1.758             | 0.502                |
| 5   | 20             | 11330.960 | 7051.119  | 3486.843 | 0.290      | 0.180      | 0.344 | 0.103 | 1.662             | 0.511                |
| 6   | 25             | 10643.310 | 7199.198  | 3555.901 | 0.287      | 0.194      | 0.369 | 0.136 | 1.561             | 0.522                |
| 7   | 30             | 9974.406  | 7395.333  | 3623.334 | 0.282      | 0.209      | 0.371 | 0.173 | 1.463             | 0.532                |
| 8   | 35             | 9359.192  | 7647.394  | 3680.229 | 0.275      | 0.224      | 0.356 | 0.212 | 1.373             | 0.540                |
| 9   | 40             | 8816.012  | 7963.509  | 3718.337 | 0.265      | 0.239      | 0.328 | 0.252 | 1.293             | 0.545                |
| 10  | 45             | 8351.207  | 8351.207  | 3731.758 | 0.253      | 0.253      | 0.292 | 0.292 | 1.225             | 0.547                |
| 11  | 50             | 7963.509  | 8816.012  | 3718.337 | 0.239      | 0.265      | 0.252 | 0.328 | 1.168             | 0.545                |
| 12  | 55             | 7647.394  | 9359.192  | 3680.229 | 0.224      | 0.275      | 0.212 | 0.356 | 1.122             | 0.540                |
| 13  | 60             | 7395.333  | 9974.406  | 3623.334 | 0.209      | 0.282      | 0.173 | 0.371 | 1.085             | 0.532                |
| 14  | 65             | 7199.198  | 10643.310 | 3555.901 | 0.194      | 0.287      | 0.136 | 0.369 | 1.056             | 0.522                |
| 15  | 70             | 7051.119  | 11330.960 | 3486.843 | 0.180      | 0.290      | 0.103 | 0.344 | 1.034             | 0.511                |
| 16  | 75             | 6944.024  | 11983.280 | 3424.350 | 0.168      | 0.291      | 0.073 | 0.293 | 1.019             | 0.502                |
| 17  | 80             | 6872.014  | 12530.190 | 3375.039 | 0.159      | 0.291      | 0.047 | 0.214 | 1.008             | 0.495                |
| 18  | 85             | 6830.651  | 12897.620 | 3343.613 | 0.154      | 0.290      | 0.023 | 0.114 | 1.002             | 0.490                |
| 19  | 90             | 6817.175  | 13027.500 | 3332.835 | 0.152      | 0.290      | 0.000 | 0.000 | 1.000             | 0.489                |

**Table 4.**  
 Variation of engineering elastic constants with fiber orientation  $\theta$  in PPSFC.



**Figure 4.**  
 Variation of elastic modulus with fiber orientation in PEFBFC and PPSFC.

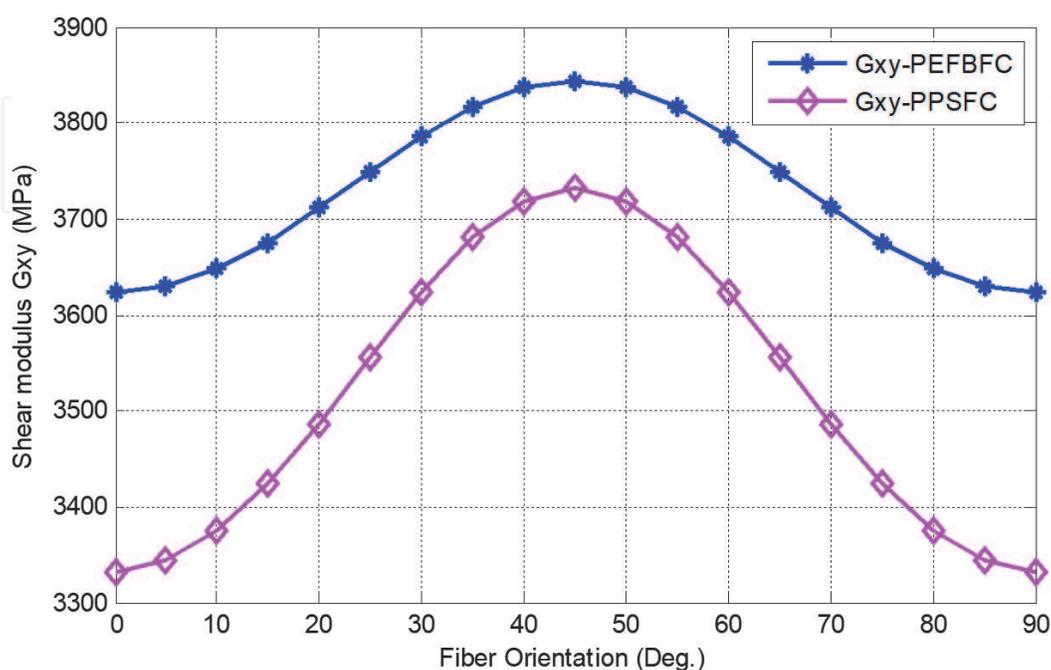
reference  $y$ -direction ( $E_y$ ) as the fiber orientation angle increased from  $0^\circ$  to  $90^\circ$  reaching a peak value of 14,922 and 13027.5 MPa for PEFBFC and PPSFC respectively. The implication is that reinforcements are required to be aligned in the

direction of applied load [55]. Although Jones [56] intuitively suggested that highest value of material properties may not necessarily occur along the principal material directions, rather it is essential that transverse reinforcement is needed in unidirectional fiber composites which are subjected to multi axial loading [57].

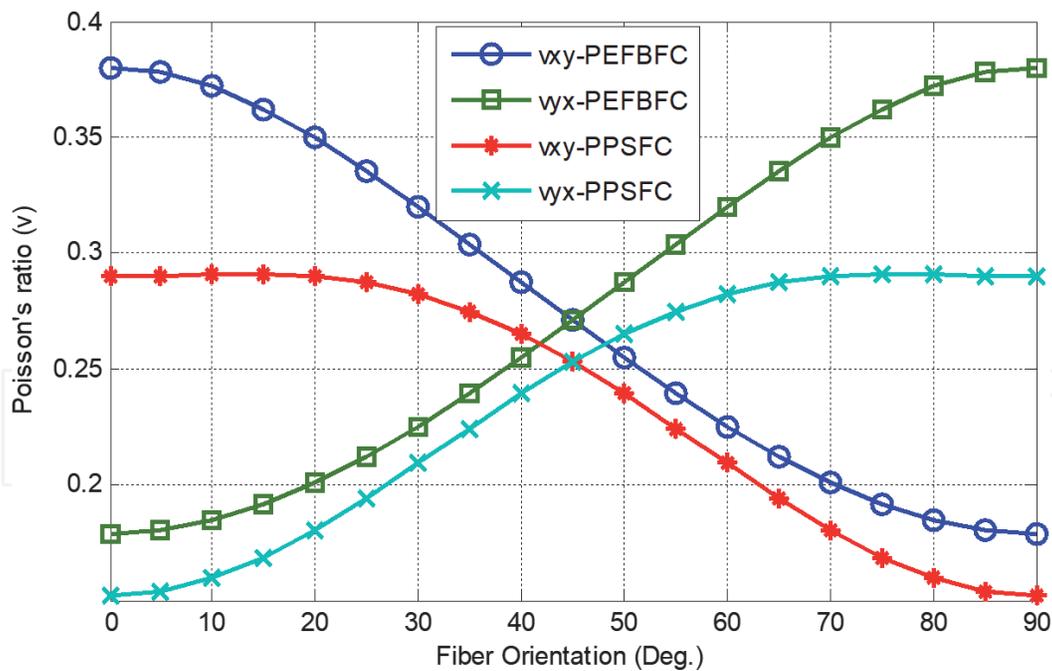
As can be seen in **Figure 5** that shear modulus peaked at 45° fiber orientation and shear modulus was symmetric at about 45° fiber orientation angle for both PEFBFC and PPSFC considered. This implies that the higher in-plane shear resistance is achievable when fiber orientation is 45°. Also the respective minimum value of 3622.99 and 3332.83 MPa at fiber orientation 0° for PEFBFC and PPSFC can be seen to gradually increase to maximum values of 3843.57 and 3731.758 MPa at fiber orientation 45° and then reversed parabolically at 90° where it again reaches to 3622.99 and 3332.84 MPa. Similar trend was obtained by Farooq and Myler [58] who developed efficient procedures for determination of mechanical properties of carbon fiber-reinforced laminated composite panels. This trend in which the value of  $G_{xy}$  peaks at 45° fiber orientation angle and lowers at 0° and 90° fiber orientation angle indicates that off-axis reinforcement is very necessary for robust shear stiffness in unidirectional composites [57].

**Figure 6** shows variation of Poisson's ratio with fiber orientation, the graph depicts a gradual drop of major Poisson's ratio ( $\nu_{xy}$ ) for PEFBFC and PPSFC respectively from 0.38 and 0.29 when fibers are aligned at 0° orientation angle to a lowest value of 0.18 and 0.15 value when fibers were aligned at 90° orientation angle. Additionally, the minor Poissons ratio ( $\nu_{yx}$ ) for PEFBFC and PPSFC increased respectively from 0.18 and 0.15 when fibers are aligned at 0° orientation angle to a highest value of 0.38 and 0.29 value when fibers were aligned at 90° orientation angle.

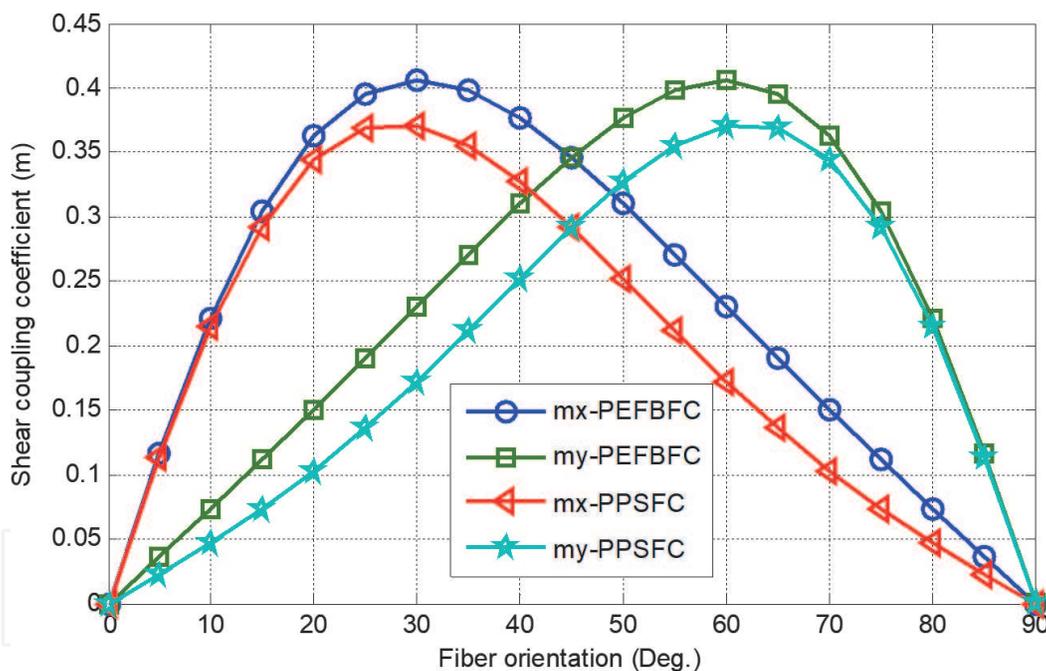
**Figure 7** depicts the variation of shear coupling coefficient with fiber orientation, equal magnitude of shear coupling effect was obtained at 45° fiber orientation angle for both PEFBFC and PPSFC considered. Gibson [57] reported that shear coupling coefficient is a measure of the amount of shear strain developed in the  $xy$  plane per unit normal strain along the direction of the applied normal stress  $\sigma_x$ . **Figure 7** clearly indicate that the maximum value of the shear coupling coefficient in the reference  $x$ -direction for PEFBFC and PPSFC was attained at 30° fiber orientation angle while the coefficient in the reference  $y$ -direction for PEFBFC and



**Figure 5.**  
Variation of shear modulus with fiber orientation in PEFBFC and PPSFC.



**Figure 6.**  
 Variation of Poisson's ratio with fiber orientation in PEFBFC and PPSFC.



**Figure 7.**  
 Variation of shear coupling coefficient with fiber orientation in PEFBFC and PPSFC.

PPSFC was attained at 60° fiber orientation angle. This is an indication that as the shear-coupling ratio increases, the amount of shear coupling increases.

#### 4. Tsai-Hill failure criteria assessment of longitudinal tensile strength

Failure theory is essential in determining whether the composite has failed. Literature review has shown that results of failure prediction depend on failure criterion applied and one major failure criteria used in the industries is Tsai-Hill and

failure criteria. Additionally, since composites ultimate tensile strength and strain depend on the fiber orientation, a failure criterion must be used in which the applied stress system is also in material axis [54]. Tsai-Hill theory considers an interaction of the stresses in the fiber direction. It postulates that failure can only occur in reinforced composites when the failure index exceeds 1, hence Eq. (19) must be satisfied to avoid failure.

By considering an arbitrary positive angle  $\theta$  with reference to the  $x$ -axis in **Figure 3**, Ihueze et al. [43] transformed the stresses within the global axes ( $x$ - $y$ ) into material axes 1-2 as given in Eq. (15)

$$\begin{Bmatrix} \sigma_1 \\ \sigma_2 \\ \tau_{12} \end{Bmatrix} = \begin{bmatrix} c^2 & s^2 & 2sc \\ s^2 & c^2 & -2sc \\ -sc & sc & (c^2 - s^2) \end{bmatrix} \begin{Bmatrix} \sigma_x \\ \sigma_y \\ \tau_{xy} \end{Bmatrix} \quad (15)$$

where  $c = \cos\theta$  and  $s = \sin\theta$ . Taking longitudinal direction stresses as  $\sigma_y = \tau_{xy} = 0$  and thus

$$\sigma_1 = \sigma_x \cos^2\theta \quad (16)$$

$$\sigma_2 = \sigma_x \sin^2\theta \quad (17)$$

$$\tau_{12} = -\sigma_x \cos\theta \sin\theta \quad (18)$$

Considering Tsai-Hill failure criterion and setting the failure index as 1 for the composite failure to occur:

$$\left(\frac{\sigma_1}{S_{u1}}\right)^2 + \left(\frac{\sigma_2}{S_{u2}}\right)^2 + \left(\frac{\tau_{12}}{\tau_{max}}\right)^2 - \left(\frac{\sigma_1}{S_{u1}}\right)\left(\frac{\sigma_2}{S_{u1}}\right) = 1 \quad (19)$$

Substituting the appropriate value in Eq. (19) we have for PEFBFC

$$\left(\frac{\sigma_x \cos^2\theta}{410.15}\right)^2 + \left(\frac{\sigma_x \sin^2\theta}{37.3397}\right)^2 + \left(\frac{-\sigma_x \cos\theta \sin\theta}{19.3100}\right)^2 - \left(\frac{\sigma_x \cos^2\theta}{410.15}\right)\left(\frac{\sigma_x \sin^2\theta}{410.15}\right) = 1$$

$$\sigma_{x, \text{PEFBFC}} = \sqrt{\frac{1}{\left(\frac{\cos^4\theta}{410.15^2} + \frac{\sin^4\theta}{37.3397^2} + \frac{\cos^2\theta \sin^2\theta}{19.3100^2} - \frac{\cos^2\theta \sin^2\theta}{410.15^2}\right)}}$$

And for PPSFC

$$\left(\frac{\sigma_x \cos^2\theta}{288.10}\right)^2 + \left(\frac{\sigma_x \sin^2\theta}{33.1330}\right)^2 + \left(\frac{-\sigma_x \cos\theta \sin\theta}{15.5700}\right)^2 - \left(\frac{\sigma_x \cos^2\theta}{288.10}\right)\left(\frac{\sigma_x \sin^2\theta}{288.10}\right) = 1$$

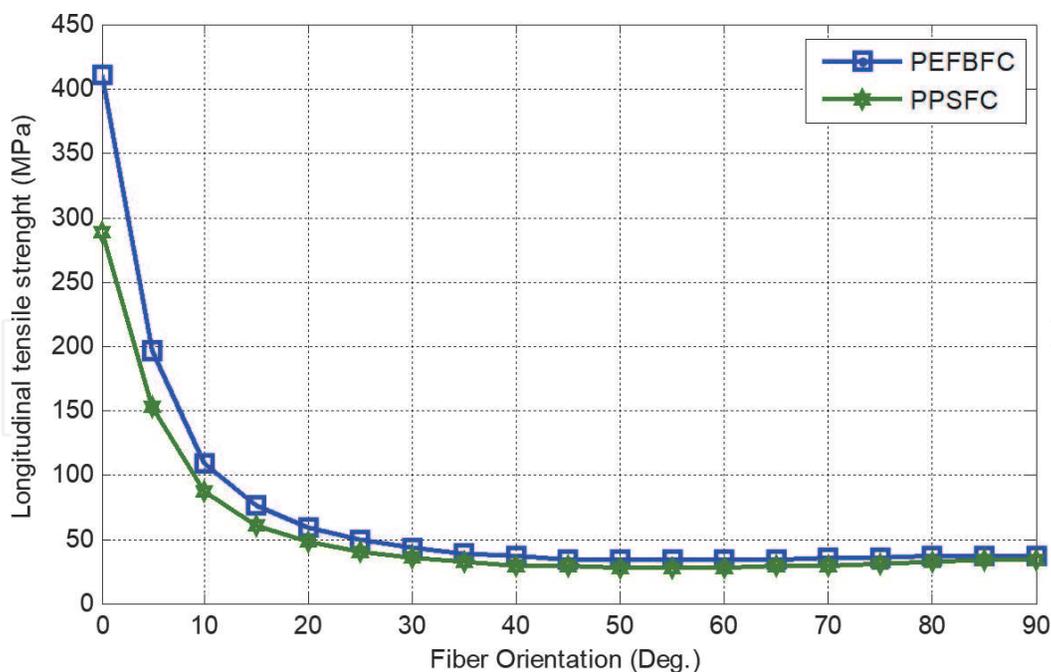
$$\sigma_{x, \text{PPSFC}} = \sqrt{\frac{1}{\left(\frac{\cos^4\theta}{288.10^2} + \frac{\sin^4\theta}{33.1330^2} + \frac{\cos^2\theta \sin^2\theta}{15.5700^2} - \frac{\cos^2\theta \sin^2\theta}{288.10^2}\right)}}$$

Hence the value for  $\sigma_x$  is then calculated for orientation ranging from  $0^\circ$  to  $90^\circ$  as shown in **Table 5**.

The variation of longitudinal tensile strength with fiber orientation for PEFBFC and PPSFC has been presented in **Figure 8**, it can be seen that the tensile strength equals 410.15 and 288.1 MPa which are the longitudinal tensile strength for PEFBFC and PPSFC respectively when fiber orientation angle is  $0^\circ$ ; on the other hand, the tensile strength equals 37.3397 and 33.133 MPa which are the transverse tensile strength for PEFBFC and PPSFC respectively when fiber orientation angle is  $90^\circ$ .

| S/N | Orientation $\theta$ | PEFBFC  | PPSFC   |
|-----|----------------------|---------|---------|
| 1   | 0                    | 410.15  | 288.1   |
| 2   | 5                    | 195.86  | 152.635 |
| 3   | 10                   | 108.786 | 86.8937 |
| 4   | 15                   | 75.4556 | 60.6747 |
| 5   | 20                   | 58.6356 | 47.3142 |
| 6   | 25                   | 48.8262 | 39.5106 |
| 7   | 30                   | 42.6439 | 34.6088 |
| 8   | 35                   | 38.6038 | 31.4352 |
| 9   | 40                   | 35.9607 | 29.4005 |
| 10  | 45                   | 34.3043 | 28.1833 |
| 11  | 50                   | 33.3926 | 27.5977 |
| 12  | 55                   | 33.0716 | 27.5303 |
| 13  | 60                   | 33.2311 | 27.9038 |
| 14  | 65                   | 33.774  | 28.6492 |
| 15  | 70                   | 34.5913 | 29.679  |
| 16  | 75                   | 35.5418 | 30.8595 |
| 17  | 80                   | 36.4447 | 31.9912 |
| 18  | 85                   | 37.0995 | 32.8242 |
| 19  | 90                   | 37.3397 | 33.133  |

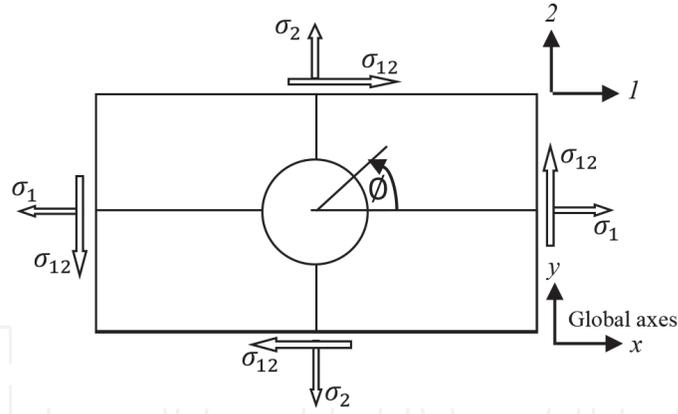
**Table 5.**  
 Longitudinal tensile strength variation with fiber orientation angle.



**Figure 8.**  
 Variation of longitudinal tensile strength with fiber orientation for PEFBFC and PPSFC.

## 5. Variation of tangential stress and modulus around a structural discontinuity

Structural discontinuity arising from holes in reinforced composites created for joining or access purposes causes stress concentration at the point of discontinuity [59].



**Figure 9.**  
 Depiction of hole in the plantain fiber-reinforced composites sample.

Adequate comprehension of stress redistribution pattern and concentrations is helpful for proficient and safe structural designs. Unlike in ductile materials where stress concentration is of no much ado, plantain fiber-reinforced composites may be sufficiently brittle, hence every form of stress concentration and structural discontinuity has to be properly designed. In a typical scenario where a circular hole is created in the composite as shown in **Figure 9**, assuming no interlaminar stresses exist around the free edge of the hole, the ply is nominally stressed by  $\sigma_1$ ,  $\sigma_2$ ,  $\sigma_{12}$  some distance away from the hole as indicated. Lekhnitskii [60] derived various useful expressions for stress distribution around holes in a composite plate, the tangential elastic modulus  $E_\varnothing$  at an angular position  $\varnothing$  is determined using Eq. (20).

$$E_\varnothing = \frac{1}{\left( \frac{\sin^4 \varnothing}{E_1} + \left[ \frac{1}{G_{12}} - \frac{2\nu_{12}}{E_1} \right] \sin^2 \varnothing \cos^2 \varnothing + \frac{\cos^4 \varnothing}{E_2} \right)} \quad (20)$$

Hence the tangential stress  $\sigma_\varnothing$  at the periphery of the hole with an angle  $\varnothing$  is found from Eq. (21).

$$\sigma_\varnothing = \frac{E_\varnothing}{E_1} (A\sigma_1 + B\sigma_2 + C\sigma_{12}) \quad (21)$$

where

$$\begin{aligned} A &= \cos^2 \varnothing + (1+p) \sin^2 \varnothing \\ B &= q \{ (q+p) \cos^2 \varnothing - \sin^2 \varnothing \} \\ C &= (1+q+p)p \sin 2\varnothing \\ p &= \sqrt{2(q - \nu_{12}) + \frac{E_1}{G_{12}}} \\ q &= \sqrt{\frac{E_1}{E_2}} \end{aligned}$$

Using the stress transformation matrix and replacing the axes system 1–2 by radial ( $r$ )-tangential ( $\varnothing$ ), we can resolve the tangential stress  $\sigma_\varnothing$  back into the material axes in Eq. (22) for proper strength evaluation

$$\begin{Bmatrix} \sigma_r \\ \sigma_\varnothing \\ \tau_{r\varnothing} \end{Bmatrix} = \begin{bmatrix} c^2 & s^2 & -2sc \\ s^2 & c^2 & 2sc \\ sc & -sc & (c^2 - s^2) \end{bmatrix} \begin{Bmatrix} \sigma_x \\ \sigma_y \\ \tau_{xy} \end{Bmatrix} \quad (22)$$

At the edge of the hole, only the tangential stress  $\sigma_{\varnothing} > 0$ , thus  $\sigma_r = \sigma_{r\varnothing} = 0$  in Eq. (22), therefore

$$\sigma_1 = \sigma_x = \sigma_{\varnothing} \sin^2 \varnothing \quad (23)$$

$$\sigma_2 = \sigma_y = \sigma_{\varnothing} \cos^2 \varnothing \quad (24)$$

$$\sigma_{12} = \sigma_{xy} = -\sigma_{\varnothing} \cos \varnothing \sin \varnothing \quad (25)$$

Using the maximum stress criterion, the material will fail when any stress value in the material axes exceeds their respective ultimate strength. Such that

$$\left| \frac{\sigma_1}{S_{u1}} \right| < 1 \quad (26)$$

$$\left| \frac{\sigma_2}{S_{u2}} \right| < 1 \quad (27)$$

$$\left| \frac{\sigma_{12}}{\tau_{max}} \right| < 1 \quad (28)$$

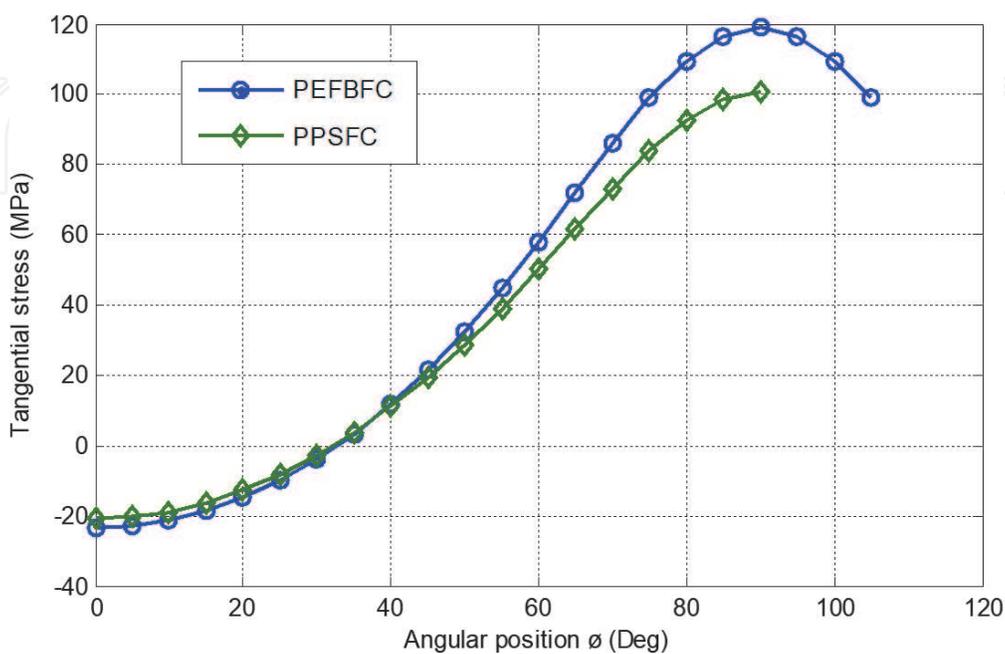
| S/N | $E_{\theta}$ | $\sigma_{\theta}$ | $\sigma_1$ | $\sigma_2$ | $\sigma_{12}$ | F.I. <sub>1</sub> | F.I. <sub>2</sub> | F.I. <sub>12</sub> | Stress conc. |
|-----|--------------|-------------------|------------|------------|---------------|-------------------|-------------------|--------------------|--------------|
| 0   | 7030.962     | -23.338           | 0.000      | -23.338    | 0.000         | 0.000             | 0.625             | 0.000              | -0.69        |
| 5   | 7053.373     | -22.807           | -0.173     | -22.634    | 1.980         | 0.000             | 0.606             | 0.103              | -0.67        |
| 10  | 7121.323     | -21.211           | -0.640     | -20.571    | 3.627         | 0.002             | 0.551             | 0.188              | -0.62        |
| 15  | 7236.950     | -18.542           | -1.242     | -17.300    | 4.636         | 0.003             | 0.463             | 0.240              | -0.55        |
| 20  | 7403.786     | -14.786           | -1.730     | -13.056    | 4.752         | 0.004             | 0.350             | 0.246              | -0.43        |
| 25  | 7626.692     | -9.917            | -1.771     | -8.146     | 3.799         | 0.004             | 0.218             | 0.197              | -0.29        |
| 30  | 7911.712     | -3.903            | -0.976     | -2.927     | 1.690         | 0.002             | 0.078             | 0.088              | -0.11        |
| 35  | 8265.787     | 3.303             | 1.087      | 2.217      | -1.552        | 0.003             | 0.059             | 0.080              | 0.10         |
| 40  | 8696.213     | 11.751            | 4.855      | 6.896      | -5.786        | 0.012             | 0.185             | 0.300              | 0.35         |
| 45  | 9209.655     | 21.484            | 10.742     | 10.742     | -10.742       | 0.026             | 0.288             | 0.556              | 0.63         |
| 50  | 9810.462     | 32.515            | 19.080     | 13.434     | -16.010       | 0.047             | 0.360             | 0.829              | 0.96         |
| 55  | 10497.994    | 44.784            | 30.050     | 14.733     | -21.042       | 0.073             | 0.395             | 1.090              | 1.32         |
| 60  | 11262.726    | 58.103            | 43.577     | 14.526     | -25.159       | 0.106             | 0.389             | 1.303              | 1.71         |
| 65  | 12081.304    | 72.076            | 59.203     | 12.873     | -27.607       | 0.144             | 0.345             | 1.430              | 2.12         |
| 70  | 12911.622    | 86.025            | 75.962     | 10.063     | -27.648       | 0.185             | 0.269             | 1.432              | 2.53         |
| 75  | 13690.476    | 98.951            | 92.323     | 6.628      | -24.738       | 0.225             | 0.178             | 1.281              | 2.91         |
| 80  | 14337.671    | 109.599           | 106.294    | 3.305      | -18.742       | 0.259             | 0.089             | 0.971              | 3.22         |
| 85  | 14769.765    | 116.668           | 115.782    | 0.886      | -10.130       | 0.282             | 0.024             | 0.525              | 3.43         |
| 90  | 14922.000    | 119.152           | 119.152    | 0.000      | 0.000         | 0.291             | 0.000             | 0.000              | 3.50         |
| 95  | 14769.765    | 116.668           | 115.782    | 0.886      | 10.130        | 0.282             | 0.024             | 0.525              | 3.43         |
| 100 | 14337.671    | 109.599           | 106.294    | 3.305      | 18.742        | 0.259             | 0.089             | 0.971              | 3.22         |
| 105 | 13690.476    | 98.951            | 92.323     | 6.628      | 24.738        | 0.225             | 0.178             | 1.281              | 2.91         |

**Table 6.**  
 Variation of tangential stress, material axis stress and tangential modulus at the edge of material discontinuity in PEFBFC.

The left hand side of Eqs. (26)–(28) represents the failure indices (FI). The maximum failure index (FI) for the applied stress is factored in to obtain the load factor. Due to the inherent material orthotropy, the failure zone of the plantain

| S/N | $E_{\theta}$ | $\sigma_{\theta}$ | $\sigma_1$ | $\sigma_2$ | $\sigma_{12}$ | F.I. <sub>1</sub> | F.I. <sub>2</sub> | F.I. <sub>12</sub> | Stress conc. |
|-----|--------------|-------------------|------------|------------|---------------|-------------------|-------------------|--------------------|--------------|
| 0   | 6817.175     | -20.978           | 0.000      | -20.978    | 0.000         | 0.000             | 0.633             | 0.000              | -0.72        |
| 5   | 6830.651     | -20.459           | -0.155     | -20.304    | 1.776         | 0.001             | 0.613             | 0.114              | -0.71        |
| 10  | 6872.014     | -18.909           | -0.570     | -18.339    | 3.234         | 0.002             | 0.554             | 0.208              | -0.65        |
| 15  | 6944.024     | -16.346           | -1.095     | -15.251    | 4.086         | 0.004             | 0.460             | 0.262              | -0.56        |
| 20  | 7051.119     | -12.791           | -1.496     | -11.295    | 4.111         | 0.005             | 0.341             | 0.264              | -0.44        |
| 25  | 7199.198     | -8.269            | -1.477     | -6.792     | 3.167         | 0.005             | 0.205             | 0.203              | -0.29        |
| 30  | 7395.333     | -2.793            | -0.698     | -2.095     | 1.209         | 0.002             | 0.063             | 0.078              | -0.10        |
| 35  | 7647.394     | 3.635             | 1.196      | 2.439      | -1.708        | 0.004             | 0.074             | 0.110              | 0.13         |
| 40  | 7963.509     | 11.024            | 4.555      | 6.469      | -5.428        | 0.016             | 0.195             | 0.349              | 0.38         |
| 45  | 8351.207     | 19.391            | 9.695      | 9.695      | -9.695        | 0.034             | 0.293             | 0.623              | 0.67         |
| 50  | 8816.012     | 28.736            | 16.863     | 11.873     | -14.150       | 0.059             | 0.358             | 0.909              | 0.99         |
| 55  | 9359.192     | 39.014            | 26.179     | 12.835     | -18.331       | 0.091             | 0.387             | 1.177              | 1.35         |
| 60  | 9974.406     | 50.087            | 37.565     | 12.522     | -21.688       | 0.130             | 0.378             | 1.393              | 1.73         |
| 65  | 10643.308    | 61.651            | 50.640     | 11.011     | -23.614       | 0.176             | 0.332             | 1.517              | 2.13         |
| 70  | 11330.958    | 73.175            | 64.615     | 8.560      | -23.518       | 0.224             | 0.258             | 1.510              | 2.52         |
| 75  | 11983.277    | 83.856            | 78.239     | 5.617      | -20.964       | 0.272             | 0.170             | 1.346              | 2.89         |
| 80  | 12530.185    | 92.667            | 89.873     | 2.794      | -15.847       | 0.312             | 0.084             | 1.018              | 3.20         |
| 85  | 12897.622    | 98.526            | 97.778     | 0.748      | -8.554        | 0.339             | 0.023             | 0.549              | 3.40         |
| 90  | 13027.500    | 100.587           | 100.587    | 0.000      | 0.000         | 0.349             | 0.000             | 0.000              | 3.47         |

**Table 7.** Variation of tangential stress, material axis stress and tangential modulus at the edge of material discontinuity in PPSFC.



**Figure 10.** Tangential stress distribution at a hole edge for PEFBFC and PPSFC.

fiber-reinforced composite as a result of structural discontinuity may not necessarily occur at the point of maximum stress concentration, therefore it is important to assess the extent of variation of the tangential stress around the hole edge and the failure index using maximum stress theory at other points aside the point of maximum stress concentration. Also in the present consideration we take a simplified scenario where  $\sigma_2 = \sigma_{12} = 0$  such that the ply of dimensions  $150 \times 19.05 \times 3.2$  mm with a circular hole at the center is subjected to only nominal axial stress  $\sigma_{PEFBFC} = 34$  MPa and  $\sigma_{PPSFC} = 29$  MPa. **Tables 6** and **7** depict the values of tangential stress, material axis stress and tangential modulus as computed using Eq. (20)–(25).

Tangential stress distribution at hole edge for PEFBFC and PPSFC are shown in **Figure 10**, the maximum stress value of 119.15 and 100.587 MPa was attained at angular position  $\theta = 90^\circ$  for PEFBFC and PPSFC respectively. However, considering various failure indices in **Tables 5** and **6**, failure will be initiated at  $\theta = 70^\circ$  for PEFBFC with stress concentration factor of 2.53 and  $\theta = 65^\circ$  for PPSFC with stress concentration factor of 2.13 which are less than the stress concentration around the peak stress when angular position is  $90^\circ$ .

## 6. Conclusions

The utilization of plantain fiber-reinforced composites in structural applications empowers architects to acquire huge accomplishments in the usefulness, security and economy of development. These materials have high proportion of strength-to-density ratio, can be tailored to possess certain mechanical properties. The elastic constants of plantain fiber-reinforced composites depend greatly on fiber orientation with notable anisotropic characteristics which makes it less attractive for applications involving lugs and fittings. The present report amplified some notable design procedures in handling such limitations in plantain fiber-reinforced composites using relevant failure theories. Both plantain EFBFRC and PSFRC showed similar trends in response to the design scenario considered. Be that as it may be, a proficient utilization of plantain fiber-reinforced composites in structural applications requires a cautious assessment of all influential factors.

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