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AVC Using a Backstepping Design Technique

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1. Introduction

This chapter deals with the vibration attenuation or vibration suppression by means of feedback control techniques applied to decrease the dynamic response of a rotor assumed as active magnetic dynamic damping which is common in rotating machinery supported by active magnetic bearings. Position control systems applied on active magnetic bearings are using sometimes nonlinear robust control techniques. Backstepping control algorithms have been successfully applied to control active magnetic bearings in recent industrial applications. Consequently, when such an algorithm is being applied to control the radial shaft position, active vibration control should be performed taking advantage of the use of the same control algorithm. In the proposed methodology it is applied the Backstepping algorithm in cascade with a master conventional PID controller. The main functions of the cascade strategy are summarized as, desired radial shaft trajectory and radial position generation, rotor stabilization and vibration attenuation. Backstepping methodology provides a rather straightforward way to design the slave or cascade controller suitable for an unstable nonlinear system such as a magnetic bearing. Stabilization of the closed-loop system is achieved by incorporating appropriate Lyapunov functions which are inherent to the Backstepping algorithm. The global asymptotic stability is ensured when the derivative of the Lyapunov function is rendered negative definite by the control law. The closed loop damping or vibration attenuation is achieved according requirements by on-line determining and selecting the appropriate gains and parameters for the implemented control strategy as function of the fundamental vibration characteristics.

The aim to continue with research activities on this technologic field after more then three decades of intensive work, obeys to the fact that some modern machines require the characteristics and advantages of applying such technology (Gerhard Schweitzer, Eric H. Maslen Editors, 2009). The main characteristics of AMB based machines where the rotor is supported by radial active magnetic bearings are summarized as follows:

The *unbalance compensation*.- The most relevant characteristic of an AMB deals with the active compensation of shaft disturbances, such vibration due to residual unbalance which can be effectively measured and identified by the AMB control system. The signal is used to either generate counteracting and compensating bearing forces or to shift the rotor axis in such away that the rotor is rotating force-free.

The *positioning precision*.- The radial precision with which the position of the rotor can be controlled, is mainly determined by the precision or quality of the measurement signal within the control loop. Conventional inductive sensors, (eddy current based sensors) for example, have a measurement resolution of about 1/100 to 1/1000 of a millimetre.

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Diagnostics.- On the basis of acquired data inherent to the position and vibration suppression control, diagnostics are readily performed, as the states and dynamic condition of the rotor are measured for the operation of the AMB anyway, and this information can be used to monitor and check operating conditions and performance. Even active diagnostics are feasible, by using the AMB as actuators in model analysis mode for generating well defined test signals simultaneously with their bearing function.

The results of the design technique are evaluated on a vertical test rig where real-time data is analysed and compared with conventional control results.

1.1 The backstepping based AVC background

Active vibration control (AVC) applied on rotating machinery continues being after more than three decades of intensive research an area of primary interest (Tao Yang et al., 2009). AVC applied on active magnetic bearings (AMB) continues also being an important and active research area motivated by the demand of efficiency in the industrial production system. It deals essentially with nonlinear systems and nonlinear control theory, where among a vast range of applied nonlinear control strategies and algorithms, backstepping theory can definitely contribute positively to AVC of AMB.

Nonlinear control theory has been the subject of very strong development during the last two decades (Hassan K. Khalil, 2002), (Krstic, M., I. Kanellakopoulos, & P. Kokotovic, 1995). The existing problems with regard to the control of unstable nonlinear systems, has been the amount of difficulties encountered in achieving a systematic way to ensure closed loop stability (Krstic M., & H. Deng, 1998). The tools developed in this area suddenly made the design and implementation of controllers to be applied on nonlinear systems, significantly more structured and rather straightforward with the incorporation of Backstepping theory. One of the concepts, which are well known today to overcome some of the mentioned difficulties with nonlinear control algorithms, is Backstepping theory. Some interesting applications to AVC have recently been reported. Hence, in (Guang Lia & Amir Khajepour, 2005) a robust controller is developed to regulate both flexural vibrations and rigid body motion of a hydraulically driven flexible arm. The proposed controller combines backstepping, sliding mode, and pole placement techniques to arrive at a controller capable of dealing with a nonlinear system with uncertainties. The sliding mode technique is used to achieve an asymptotic joint angle and vibration regulation. (Qinglei Hu, 2009) proposes an angular velocity bounded robust adaptive control design for attitude maneuver and vibration reduction in the presence of external disturbances and uncertainties in the inertia matrix. (V. Mañosa, F. Ikhoulane, J. Rodellar, 2005) presents a backstepping-based adaptive control designed for a class of one degree-of-freedom uncertain non-linear systems. The efficiency of the approach has been tested by numerical simulations on Duffing oscillators and systems with non-linear and hysteretic stiffness under external loads. In (Francesc Pozo et al., 2006) it is used an adaptive backstepping approach for vibration control of a hybrid seismic control system. In (Tao Yang et al., 2009), a backstepping control approach is applied to solve the active vibration isolation problem using a Stewart platform. They demonstrated that the controller can effectively attenuate low frequency vibrations in six degrees of freedom achieving satisfactory vibration isolation performance.

The work presented in this chapter is focused on the successfully application of the Backstepping theory on a typical unstable nonlinear system such as the active vibration control (vibration attenuation but not vibration suppression) on AMB's.

1.2 The backstepping background

The backstepping algorithm can be applied on control problems where a strict feedback state space model of the plant or process is available. The application presented in this chapter is one of those nonlinear systems, which have been subject to intensive studies in order to find fully stabilizing controllers. The Backstepping theory provides a tool for the recursive design of the control law based on the Lyapunov theory for stabilizing the controlled system (Hassan K. Khalil, 2002) and (Krstic, M., I. Kanellakopoulos, & P. Kokotovic, 1995). Control systems have one main goal to achieve, and that is the stability of the controlled system. An important topic with regard to the stability of dynamical systems concerns to the stability of equilibrium points, which is verified by Lyapunov Stability and LaSalle-Yoshizawa theorems (LaSalle J. P., 1960), (LaSalle, J.P., 1966), (Sontag E. D., A, 1989), (Yoshizawa, T., 1968).

The stability of nonlinear systems is verified by means of the following analytical background:

Theorem 1 (LaSalle-Yoshizawa)

Assuming the system

$$\dot{x} = f(x(t)) \quad (1)$$

with the initial condition $x(0)$, let $x=0$ be an equilibrium point for (1); let $V(x)$ be a scalar, continuously differentiable function of the state x such that

- $V(x)$ is positive definite
- $V(x)$ is radially unbounded
- $\dot{V}(x) = V_x(x)f(x) \leq -W(x)$, where $W(x)$ is positive semi-definite

Then, all solutions of (1) satisfy

$$\lim_{t \rightarrow \infty} W(x(t)) = 0$$

Furthermore, if $W(x)$ is positive definite, then the equilibrium $x = 0$ is globally uniformly asymptotically stable (GUAS). For proof, see (Hassan K. Khalil, 2002) and (Krstic, M., I. Kanellakopoulos, & P. Kokotovic, 1995) and (LaSalle J. P., 1960), (LaSalle, J.P., 1968), (Sontag E. D., A, 1989), (Sontag E.D., & Sussman, 1998), (Yoshizawa, T, 1966), (Yoshizawa, T., 1968).

Note that any equilibrium under investigation can be mapped to the origin by substituting x with $z = x - x_e$. Therefore, there is no loss of generality in standardizing results for the zero solution $z \equiv 0$. But demanding $\dot{V}$ to be negative definite, in order to claim stability, may not perform successfully.

Now that it is stated the foundation of Lyapunov stability, the main question arising is how to find these functions. The theorems above do not provide any systematic method of finding these functions. In the case of electrical or mechanical systems there are natural Lyapunov function candidates like total energy functions. In other cases, it is basically a matter of trial and error.

The Backstepping approach is so far the only systematic and recursive method for constructing a Lyapunov function, along the design of the stabilizing control law. Yet, the system must have a lower triangular structure in order to apply the method. Before we can explore this state-of-the-art technique in control of nonlinear systems, it is convenient extend the systems handled so far to those including a control input.

1.3 Control Lyapunov Functions (CLF)

Since an objective is to develop closed-loop systems with desirably stability properties, let us now add a control input to the considered system

$$\dot{x} = f(x, u), \quad x \in R^n, \quad u \in R, \quad f(0, 0) = 0 \quad (2)$$

It is necessary to introduce an extension of the Lyapunov function concept, the CLF. Given the stability results from the previous section, the objective is to find a control law $u = \alpha(x)$ such that the desired state of the closed-loop system $\dot{x} = f(x, \alpha(x))$ be Globally Asymptotic Stable (GAS) equilibrium point. Once again it is considered the origin to be the goal state for simplicity. It can be chosen a function $V(x)$ as a Lyapunov candidate, and require that its derivative along the solutions of (2) satisfy $\dot{V}(x) \leq -W(x)$, where $W(x)$ is positive definite function. Then closed-loop stability follows from Theorem (1). It is necessary therefore to find $\alpha(x)$ to guarantee that for all $x \in R^n$.

$$\dot{V}(x) = \frac{\partial V}{\partial x}(x) f(x, \alpha(x)) \leq -W(x) \quad (3)$$

The pair V and W must be chosen carefully otherwise (4) will not be solvable. This motivates the following definition, which can be found in (Krstic, M., I. Kanellakopoulos, & P. Kokotovic, 1995).

Definition 1.(CLF)

A smooth positive definite and radially unbounded function $V: R^n \rightarrow R$ is a CLF if for (2) and every $x \neq 0$

$$\dot{V}(x) = V_x(x) f(x, u) < 0 \quad \forall x \neq 0 \text{ and for some } u \quad (4)$$

The significance of this definition concerns to the fact that, the existence of a globally asymptotic stabilizing control law is equivalent to the existence of a CLF. If exists a CLF for the system, then it is certainly possible to find a globally stabilizing control law. The reverse is also true. This is known as Artstein's theorem and can be found in (Sontag E. D., 1989). Now that the concept CLF is defined, it is necessary to move on and explore the Backstepping theory, which is the main tool we must deal with.

1.4 The backstepping algorithm

The main drawback of the CLF concept as a design tool is that for most nonlinear systems the proper CLF is not known. The task of finding an appropriate CLF may be complex as well as that of designing a stabilizing feedback law. The Backstepping procedure solves both problems simultaneously. The standard procedure can be found in (Hassan K. Khalil, 2002), (Krstic, M., I. Kanellakopoulos, & P. Kokotovic, 1995). To spare the reader from the effort to understand the main ideas of Backstepping by a theorem, it helps more by starting from the description of the general procedure, which will clarify such concepts

1.5 General backstepping procedure

Given a SISO nonlinear, non-minimum phase process described under a state feedback state space model, and assuming Y_r to be a tracking reference trajectory, the following sequence is to be performed under a systematic procedure according the generic following steps:

Step 1:

Error step 1:

$$Z_1 = Y_r - X_1 \quad (5a)$$

Lyapunov Function 1st step:

$$V_1 = \frac{1}{2} Z_1^2 \quad (5b)$$

Derivative of V_1 :

$$\dot{V}_1 = Z_1 \dot{Z}_1 = Z_1 (\dot{Y}_r - \dot{X}_1) \quad (5c)$$

Stabilizing function 1st step:

$$\alpha_1 = X_{2d} = \dot{Y}_r - P_1 Z_1 \quad (5d)$$

with $P_1 > 0$

Step 2:

Error step 2

$$Z_2 = X_2 - X_{2d} = X_2 - \alpha_1 \quad (5e)$$

Lyapunov Function 2^d step:

$$V_2 = \frac{1}{2} Z_1^2 + \frac{1}{2} Z_2^2 \quad (5f)$$

With

$$\dot{Z}_1 = \dot{Y}_r - \dot{X}_1 = \dot{Y}_r - X_2 = P_1 Z_1 - Z_2 \quad (5g)$$

erivative of V_2 :

$$\dot{V}_2 = P_1 Z_1^2 - Z_2 (Z_1 + \dot{X}_2 - \dot{\alpha}_1) \quad (5h)$$

$$\dot{V}_2 = P_1 Z_1^2 - Z_2 \left[(1 - P_1^2) Z_1 + P_1 Z_2 + X_3 - \ddot{Y}_r \right] \quad (5i)$$

Stabilizing function 2^d step:

$$\alpha_2 = X_{3d} = (P_1^2 - 1) Z_1 - (P_1 + P_2) Z_2 + \ddot{Y}_r \quad (5j)$$

with $P_2 > 0$

Step i :

Error step i

$$Z_i = X_i - X_{id} = X_i - \alpha_{i-1} \quad (5k)$$

Lyapunov Function i^{th} step:

$$V_i = \frac{1}{2} \sum_{j=1}^i Z_j^2 \quad (5l)$$

With

$$\dot{Z}_{i-1} = Z_i - P_{i-1}Z_{i-1} - Z_{i-2} \quad (5m)$$

Derivative of V_i :

$$\dot{V}_i = -\sum_{j=1}^{i-1} P_j Z_j^2 + Z_i [Z_{i-1} + \dot{X}_i - \dot{\alpha}_{i-1}] \quad (5n)$$

Stabilizing function i^{th} step:

$$\alpha_i = X_{i+1} = -P_i Z_i - Z_{i-1} + \dot{\alpha}_{i-1} \quad (5o)$$

where $P_i > 0$, are positive constants.

The corresponding notation is shown in figure 1, in which it is illustrated a generic process state space representation corrected with stabilizing functions by means of Backstepping procedure.

In order to avoid static control errors for systems type 0, an integrator must be added in series with the plant model. Then, at the end of the design procedure, this integrator is moved from the plant model to the control equation (Hassan K. Khalil, 2002), (Krstic, M., I. Kanellakopoulos, & P. Kokotovic, 1995). An alternative to such generalized technique consists in adding a cascade Backstepping algorithm following the setpoint generated by a feedback conventional controller.

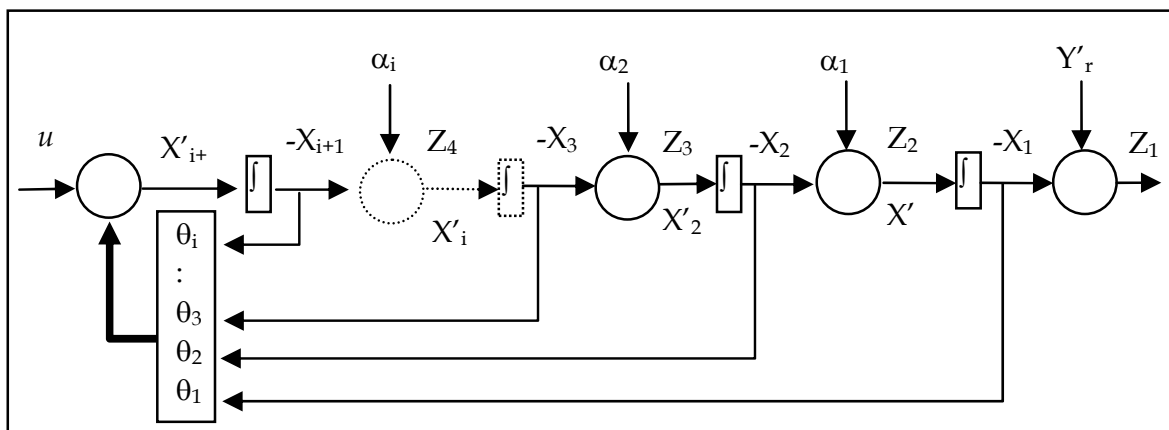


Fig. 1. General process representation stabilized by means of the Backstepping procedure

Assumption 1.

Assuming the system

$$\dot{x} = f(x) + g(x)u, \quad f(0) = 0, \quad (6)$$

where $x \in R^n$ is the state and $u \in R^n$ is the control input, there exists a continuous differentiable feedback control law

$$u = \alpha(x), \quad \alpha(0) = 0, \quad (7)$$

and a smooth, positive definite, radially unbounded function $V: R^n \rightarrow R$ such that

$$\frac{\partial V}{\partial x} [f(x) + g(x)\alpha(x)] \leq -W(x) \leq 0, \quad \forall x \in R \quad (8)$$

where $W: R^n \rightarrow R$ is positive semi-definite.

By means of this assumption, the control (7) applied to the system (6) guarantees global boundedness of $x(t)$.

Let the system (6) be augmented by an integrator according the expression

$$\begin{aligned}\dot{x} &= f(x) + g(x)\xi \\ \dot{\xi} &= u\end{aligned}\quad (9)$$

and suppose that satisfies the above assumption with $\xi \in \mathbb{R}^n$ as its control variable.

Lemma 1

Being $W(x)$ positive definite, then

$$V_a(x, \xi) = V(x) + \frac{1}{2}[\xi - \alpha(x)]^2 \quad (10)$$

is a CLF for the complete system (9). That means, there exists a feedback control $u = \alpha_a(x, \xi)$ which renders $(x, \xi) = (0, 0)$ the GAS equilibrium of (9). Such control results in

$$u = -c(\xi - \alpha(x)) + \frac{\partial \alpha}{\partial x} [f(x) + g(x)\xi] - \frac{\partial V}{\partial x} g(x), \quad c > 0 \quad (11)$$

Up to now it has been introduced the methodology and tools to design a stabilizing control law and determine its stability properties. In the next section a brief description of active magnetic bearings is presented.

2. The AMB control environment

2.1 Background

From a control viewpoint, an AMB is a nonlinear unstable process. The simplest model is represented with figure 2. The application of AMB's is based upon the principle that an electromagnet will attract ferromagnetic material. A ferromagnetic rotor can thus be supported in a magnetic field generated in the bearing electromagnet stator, as shown in the figure 2.

Since the natural tendency of the stator is to attract the rotor until it makes contact, some control action is required to modulate the magnetic field and maintain the rotor in the desired position. The most common type of control involves the feedback of shaft position. This information is then used by the control system to modulate the magnetic field through power amplifiers, so that the desired rotor position is maintained even under changing shaft load conditions. An active magnetic bearing system consists of electromagnet bearing actuators, position sensors, a control system and power amplifiers. The bearing actuators and sensors are located in the machine, while the control system and amplifiers are generally located remotely.

A typical system consists of two radial bearings and a thrust bearing. Each radial bearing has a stator and sensor system mounted over a ferromagnetic rotor installed on the shaft. The rotor consists of a stack of lamination rings mounted on a sleeve that fits onto the shaft. Laminations are used to reduce eddy current losses and to improve the response of the bearing. The stator is made of a stack of lamination rings with poles on the internal diameter. Coils are wound around each pole so that the bearing is divided into four

quadrants. The coils in each quadrant are wound in series making each quadrant function as one electromagnet. Typically on horizontal machines, the quadrants are aligned 45 degrees from vertical. Opposing quadrants constitute an axis and therefore each radial bearing can be described by two axes. A set of sensors that measure shaft position are mounted as close to the bearing as possible.

As the results shown along a couple of years indicate, digital control provides capabilities for adaptive control which can be used to greatly alleviate the unbalance vibration of rotating machinery. This is often the worst vibration problem encountered during operation. The source of this vibration is the discrepancy between the geometric axis of the rotor and its inertial axis. When the rotor is spinning, this imbalance results in a centrifugal force which causes synchronous vibration throughout the machine. This problem is managed on conventional machinery through mechanical balancing by means of the addition or removal of a small amount of mass from the shaft to reduce the residual imbalance. Rotor balancing in the field, unfortunately, is usually time consuming and costly. The down-time incurred can also be very expensive in terms of lost production. Also for some machines where the imbalance changes often during operation, such as centrifuges, mechanical balancing will have a limited benefit.

Magnetic bearings, being active devices, offer the capability to establish new and beneficial relationships between rotor and casing vibration and applied bearing force. This capability has been employed by a considerable number of researchers investigating the control of unbalance response. One method to achieve unbalance response attenuation is through design of the feedback compensation. This has been achieved via the addition of filters to stabilizing controllers (Habermann & M. Brunet, 1994), (Larsonneur & R. Herzog, 1994) or through the addition of pseudo-states in observer based controllers (T. Higuchi, T. Mizuno, & M. Tsukamoto, 1990), (F. Matsumura, M. Fujita, & K. Okawa, 1990). Other researchers (C.R. Burrows & M.N. Sahinkaya, 1983), (C.R. Burrows, M.N. Sahinkaya, & S. Clements, 1989), (T. Higuchi et al., 1990), (R. Larsonneur, 1988), (Larsonneur & R. Herzog, 1994), (B. Shafai et al., 1994), (C.R. Knospe et al., 1993), have employed methods which the authors refer to as *adaptive open loop control*. These methods, as pointed out by (R. Larsonneur, 1988), (Larsonneur & R. Herzog, 1994) and Shafai et. al., 1994), have the advantage that they may be added to feedback controllers that have been designed for optimum transient response without altering system stability or performance. These methods were first employed on a magnetic bearing supported rotor by (C.R. Burrows & M.N. Sahinkaya, 1983) who solved a least-squares-balancing problem for the proper forces to apply using an off-line theoretical model. They later extended this work to obtain an estimate of an influence coefficient matrix through trial forces and the use of a recursive control law (C.R. Burrows, M.N. Sahinkaya, & S. Clements, 1989). (Higuchi et. al., 1990) applied an adaptive open loop method (*periodic learning control*) employing an estimate of the inverse transfer function in a recursive procedure. This method can only be applied on systems with square influence coefficient matrices (number of actuators equals number of vibration sensors). Following references (C.R. Burrows, M.N. Sahinkaya, & S. Clements, 1989), (Higuchi et. al., 1990) are very similar to the convergent control algorithm presented by Knospe et. al., 1993) which uses a look-up table of influence coefficients obtained through off-line testing. (Shafai et. al., 1994) apply a distinct method of adapting the open loop forces to cancel a synchronous signal. In such a method, only one Fourier coefficient of the open loop signal is changed per adaptation cycle in such a mode as to decrease the residual error. This method, originally developed for SISO systems, was extended to square MIMO systems. Stability and performance robustness of

this method (convergence to optimal open loop control) is ensured. This is in contrast to most of the model-based methods where stability and performance robustness is being studied now. The transient performance of the adaptive open loop algorithms to changes in imbalance or rotor speed has to be considered because of its practical importance.

2.2 Modeling a generic AMB

A typical magnetic bearing comprises a set of radially positioned electromagnets located in opposing pairs around a laminated magnetic bearing journal. For instance, for a magnetic bearing with four electromagnets as depicted in figure 2, there is one opposing pair for each perpendicular axis. Each electromagnet consists of a laminated core and one or more coil windings. The force produced by a single two pole electromagnet can be shown to be given by the following equation:

$$F = \frac{\mu_0 AN^2}{4} \frac{I^2}{z^2} \quad (12)$$

where I is the total current in the magnet coils, z is the gap distance, μ_0 is the permeability of free space, A is the pole face area, and N is the number of coil turns

The force in (8) is attractive and increases as the gap decreases. This attractive force produces an unstable system for an open loop magnetic bearing configuration. The net force, F_n produced by an opposing pair of identical two-pole electromagnets on a single shaft is the sum of the forces produced by each electromagnet. Taking account of the sign convention (see Fig. 2), the net force equation is given by:

$$F_n = \frac{\mu_0 AN^2}{4} \left[\frac{I_2^2}{z_2^2} - \frac{I_1^2}{z_1^2} \right] \quad (13)$$

I_i is the current in magnet j , and z_i is the gap distance for magnet j .

A dynamical mathematical model for the AMB is shown in Fig. 2, where disturbances and external forces can be established as follows:

$$m\ddot{x} = \frac{\mu_0 AN^2}{4} \left[\left(\frac{I_2}{X_0 - x} \right)^2 - \left(\frac{I_1}{X_0 + x} \right)^2 \right] + F \quad (14)$$

where

z_2	$X_0 - x$	air gap 2
z_1	$X_0 + x$	air gap 1
m		mass of the rotor (kg);
x		position displacement of the rotor (m);
X_0		nominal air gap (m);
μ_0		permeability of free space H/m;
A		total pole-face area of each electromagnet (m ²);
N		number of turns on each electromagnet coil;
I_1, I_2		electromagnet coil currents (A);
F		some known force acting on the rotor such as load disturbances and/or the rotor weight (N).
mg		the rotor weight

Previously, the equations were given for the static force produced by a magnetic bearing along a single axis. That force is affected dynamically by the rate limit at which current changes in the coils, called the current slew rate limit, which is dependent on the voltage limit, of the power supply and the coil inductance, L .

The general nonlinear electromechanical model of the one degree-of-freedom (DOF) AMB system, for a number of electromagnet coils, can be subdivided into the mechanical subsystem dynamics, the magnetic force equation, and the electrical subsystem dynamics. The mechanical subsystem is governed by

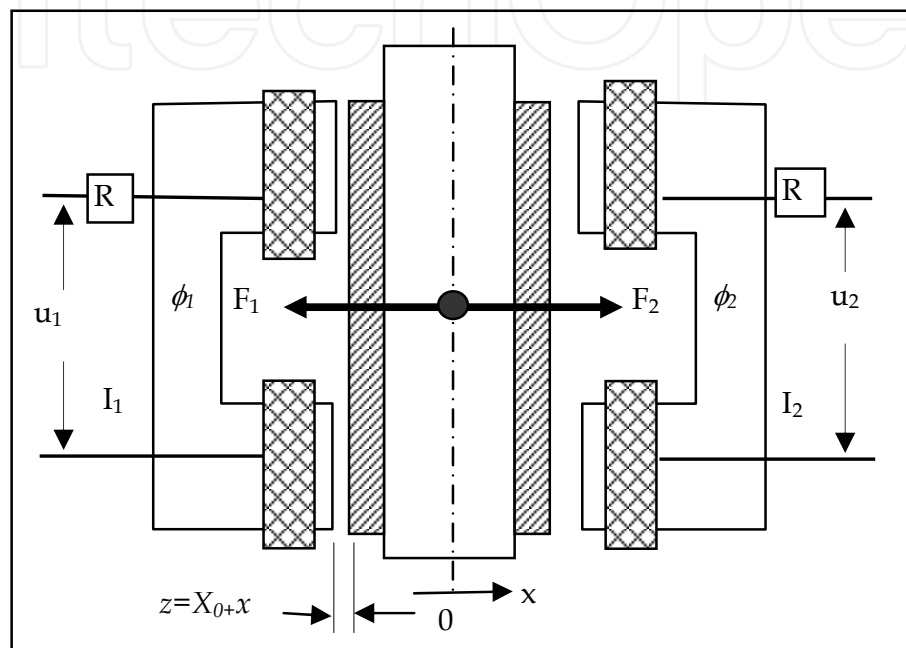


Fig. 2. Active magnetic bearing principle

$$m\ddot{x} = \sum_{i=1}^2 F_i(\Phi_i) + \sum F_D \quad (15)$$

where m is the rotor mass, x represents the position of the rotor centre, Φ_i is the magnetic flux in the i_{th} electromagnet, F_i denotes the force produced by the electromagnet, given by

$$F_i = \frac{(-1)^{i+1} \Phi_i^2}{\mu_0 A}, \quad i = 1, 2 \quad (16)$$

where F_D is the load and disturbance forces.

The electrical subsystem is governed by the equations

$$N\dot{\Phi}_i + R_i I_i = v_i, \quad i = 1, 2 \quad (17)$$

where X_0 is the nominal air gap, u is the input control voltage of the i_{th} electromagnet and I_i is the current in the i_{th} electromagnet which is related to the flux according

$$I_i = \frac{2(X_0 + (-1)^i x) \Phi_i}{\mu_0 AN}, \quad i = 1, 2 \quad (18)$$

3. Backstepping based control strategy

3.1 Introduction

Since Backstepping based control strategies are model-based techniques, one of the first tasks to be carried out concerns to AMB modelling. A practical useful AMB needs at least four pairs of active magnetic coils. Nevertheless, with regard to modelling and analysis tasks, a single pair of active magnetic coils is sufficient without loss of generality. Consequently, starting from (13-14) with reference to figure 2, a strict feedback state space model is achieved, which will be used in the design procedure. The strict feedback state space model of a vertical mechanical shaft equipped with a single pair of magnetic coils, is then developed according to

$$\begin{aligned}\dot{x}_1 &= x_2 \\ \dot{x}_2 &= \frac{C}{m} F_N = \frac{C}{m} I_2^2 \frac{1}{(X_0 - x)^2} - \frac{C}{m} I_1^2 \frac{1}{(X_0 + x)^2}\end{aligned}\quad (19)$$

where a constant parameter C is being defined as $C = 0.25 \cdot \mu_0 \cdot A \cdot N^2$

3.2 Control strategy

The control objective is to determine the manipulated variables MV_1 and MV_2 to supply a stabilizing net force $F_N = F_1 - F_2$ such that the closed loop system yields a stable response under possible load disturbances with an acceptable performance. In order to manipulate a strict feedback state space model, the manipulated variables are selected such that $MV_1 = I_1^2$ and $MV_2 = I_2^2$.

Consequently, (19) is expressed as

$$\begin{aligned}\dot{x}_1 &= x_2 \\ \dot{x}_2 &= \frac{C}{m} MV_2 \frac{1}{(X_0 - x)^2} - \frac{C}{m} MV_1 \frac{1}{(X_0 + x)^2}\end{aligned}\quad (20)$$

If the effect of gravity is considered, then

$$\dot{x}_2 = \frac{C}{m} MV_2 \frac{1}{(X_0 - x)^2} - \frac{C}{m} MV_1 \frac{1}{(X_0 + x)^2} - g \quad \text{or} \quad \dot{x}_2 = \frac{C}{m} F_N - g$$

According the Backstepping procedure shown by the sequence of expressions (5a) to (5i), a CLF is achieved as

$$\dot{x}_2 = \ddot{Y}_r + Z_2(P_1 + P_2) + Z_1(1 - P_1^2) \quad (21)$$

which will render GAS for the equilibrium points according definition 1 and equation (4), where

$$\begin{aligned}Z_1 &= Y_r - x_1 \\ Z_2 &= \dot{Y}_r + P_1 Z_1 - x_2\end{aligned}\quad (22)$$

with $(P_1, P_2) > 0$ will assume real values, which must be selected according required speed and accuracy of the closed loop response. Combining (20) and (21) yields the manipulated variables MV_1 and MV_2 that satisfies the closed loop stability criteria.

$$\frac{C}{m}F_N = \frac{C}{m}MV_2 \frac{1}{(X_0 - x)^2} - \frac{C}{m}MV_1 \frac{1}{(X_0 + x)^2} = \ddot{Y}_r + Z_2(P_1 + P_2) + Z_1(1 - P_1^2) \quad (23)$$

The expression (23) establishes the stabilizing control function which depends on the net force F_N which can be generated by the two manipulated variables MV_1 and MV_2 , consisting in a squared current supplied to the coils by means of appropriate power amplifiers.

According expression (23), such manipulated variables are both interdependent functions, yielding

$$\begin{aligned} MV_1 &= (X_0 + x)^2 \left[-\frac{m}{C} \dot{x}_2 + MV_2 \frac{1}{(X_0 - x)^2} \right] \\ MV_2 &= (X_0 - x)^2 \left[\frac{m}{C} \dot{x}_2 + MV_1 \frac{1}{(X_0 + x)^2} \right] \end{aligned} \quad (24)$$

where $\dot{x}_2$ is defined by (20).

3.3 Scheduling the backstepping controller output signal

The task of generating the stabilizing net force F_N from the manipulated variables MV_1 and MV_2 according the conventional Backstepping algorithm given by expression (24), yields a rather ambiguous results, since it provide only the net force but nothing about how to generate such stabilizing force from the availability of two unknown manipulated variables. In order to implement a deterministic control action, an output signal scheduler is proposed. In order to avoid superfluous current consumption, controller outputs must be scheduled so that only a coil of two is active at any time. Scheduling the controller outputs must be subjected to the condition by which system stability ensured by the Backstepping procedure will not be altered. In order to satisfy such condition, the Backstepping algorithm is modified with an output scheduler based on a split range procedure.

Since (21) is CLF for the controlled AMB, follows that in the setpoint position, winch coincides with equilibrium point, is also GAS. As a direct consequence, from (23) and (24) follows that the net force on the shaft exerted by a set of two opposite coils is defined by the backstepping algorithm as

$$\dot{x}_2 = \frac{C}{m} \left[\frac{I_2^2}{(X_0 - x)^2} - \frac{I_1^2}{(X_0 + x)^2} \right] - g = \ddot{Y}_r + Z_2(P_1 + P_2) + Z_1(1 - P_1^2) \quad (25)$$

and hence, the net force exerted by a unique manipulated variable (NMV), defined as

$$NMV = \frac{C}{m} \left[\frac{I_2^2}{(X_0 - x)^2} - \frac{I_1^2}{(X_0 + x)^2} \right] = \ddot{Y}_r + Z_2(P_1 + P_2) + Z_1(1 - P_1^2) + g \quad (26)$$

is also GAS, where NMV is the net manipulated variable necessary to satisfy (25) which is also GAS and g is the acceleration of local gravity.

Lemma 2.

The total force necessary to stabilize the system is based on the fact by which the net force exerted by a set of two opposite coils is equivalent to the unique force exerted by feeding an independent coil with a current such that

$$\begin{aligned} \text{IF } NMV > 0 \rightarrow \frac{C}{m} \frac{I_{2N}^2}{(X_0 - x)^2} = NMV &= \frac{C}{m} \left[\frac{I_2^2}{(X_0 - x)^2} - \frac{I_1^2}{(X_0 + x)^2} \right] = \\ &= \ddot{Y}_r + Z_2(P_1 + P_2) + Z_1(1 - P_1^2) + g \end{aligned} \quad (27)$$

which means that $I_1^2 = 0$, $\frac{I_1^2}{(X_0 + x)^2} = 0$

$$\begin{aligned} \text{IF } NMV < 0 \rightarrow \frac{C}{m} \frac{I_{1N}^2}{(X_0 + x)^2} = NMV &= \frac{C}{m} \left[\frac{I_2^2}{(X_0 - x)^2} - \frac{I_1^2}{(X_0 + x)^2} \right] = \\ &= \ddot{Y}_r + Z_2(P_1 + P_2) + Z_1(1 - P_1^2) + g \end{aligned} \quad (28)$$

meaning that

$$I_2^2 = 0, \quad \frac{I_2^2}{(X_0 - x)^2} = 0 \quad (29)$$

where I_{iN} in (36) and (24) is the net current to the coil i , with $i = 1, 2$. Consequently, from (27) and (28) follows that

$$\text{For } NMV > 0, I_{2N}^2 = \frac{m}{C} \cdot NMV \cdot (X_0 - x)^2 \text{ with } I_1 = 0 \quad (30)$$

which yields the final result as

$$I_{2N}^2 = \frac{m}{C} \cdot [\ddot{Y}_r + Z_2(P_1 + P_2) + Z_1(1 - P_1^2) + g] \cdot (X_0 - x)^2 \quad (31)$$

$$I_{1N}^2 = \frac{m}{C} \cdot [\ddot{Y}_r + Z_2(P_1 + P_2) + Z_1(1 - P_1^2) + g] \cdot (X_0 + x)^2 \quad (32)$$

Since the range of application of I_2 and I_1 is such that

$$0 \leq I_1 \leq I_{1LIM} \quad \text{AND} \quad 0 \leq I_2 \leq I_{2LIM} \quad (33)$$

where I_{1LIM} and I_{2LIM} are the maximum allowable current to the coils, follows that the set of control outputs is restricted by

$$\begin{aligned} (I_1 = 0 \text{ AND } 0 < I_2 < I_{2LIM}) \text{ OR} \\ (I_2 = 0 \text{ AND } 0 < I_1 < I_{1LIM}) \end{aligned} \quad (34)$$

constraints that satisfy the conditions established with regard to GAS in the equilibrium point. From expressions (27-34) follows that the manipulated variables must actuate alternatively under a logic exclusive OR function, instead of actuate simultaneously in opposition to each other. Consequently, in order to schedule the manipulated variables in such a way that any active variable could not actuate in opposition to each other, it is necessary to propose and schedule the controller outputs according the following restrictions.

$$\begin{bmatrix} I_{1N}^2 \\ I_{2N}^2 \end{bmatrix} = \begin{bmatrix} NMV < 0 & NMV > 0 \end{bmatrix} \begin{bmatrix} (X_0 + x)^2 \\ (X_0 - x)^2 \end{bmatrix} \frac{C}{m} NMV \quad (35)$$

which yields definitely

$$\begin{bmatrix} I_{1N}^2 \\ I_{2N}^2 \end{bmatrix} = \begin{bmatrix} NMV < 0 & NMV > 0 \end{bmatrix} \begin{bmatrix} (X_0 + x)^2 \\ (X_0 - x)^2 \end{bmatrix} \frac{C}{m} [\ddot{Y}_r + Z_2(P_1 + P_2) + Z_1(1 - P_1^2) + g] \quad (36)$$

The amplifiers structure that satisfy the current needs to each pair of opposite coils specified by the expression (36) is depicted in figure 3.

According figure 3, when the controller output value (Vcontrol) is positive, ($0 < V_{\text{control}} < 10 \text{ Vcc}$), then the coil L1 is active and the coil L2 is inactive, and when Vcontrol is negative ($0 > V_{\text{control}} > -10 \text{ Vcc}$), then the coil L2 is active and L1 is inactive.

The strategy of keeping active or energized only one coil at same time has the potential advantage of saving some energy. There is, however, a very serious drawback in terms of controllability since it is completely lost at zero current. In practice, the stiffness and bandwidth of the active magnetic bearing is greatly improved by activating both coils. Using only one coil at a time can achieve similar performance only if very high bandwidth, high voltage amplifiers are used to overcome the inherently high inductive impedance. Energy savings are only meaningful in the case of irrelevant disturbances. In practice, overcoming persistent, periodic disturbances such as rotor imbalance is more easily achieved by energizing both magnet coils. Consequently, in order to improve the control performance a properly selected bias current should be applied by the amplifiers. Such mentioned bias current doesn't affect obviously the rotor stability since it must be applied symmetrically to both opposite coils.

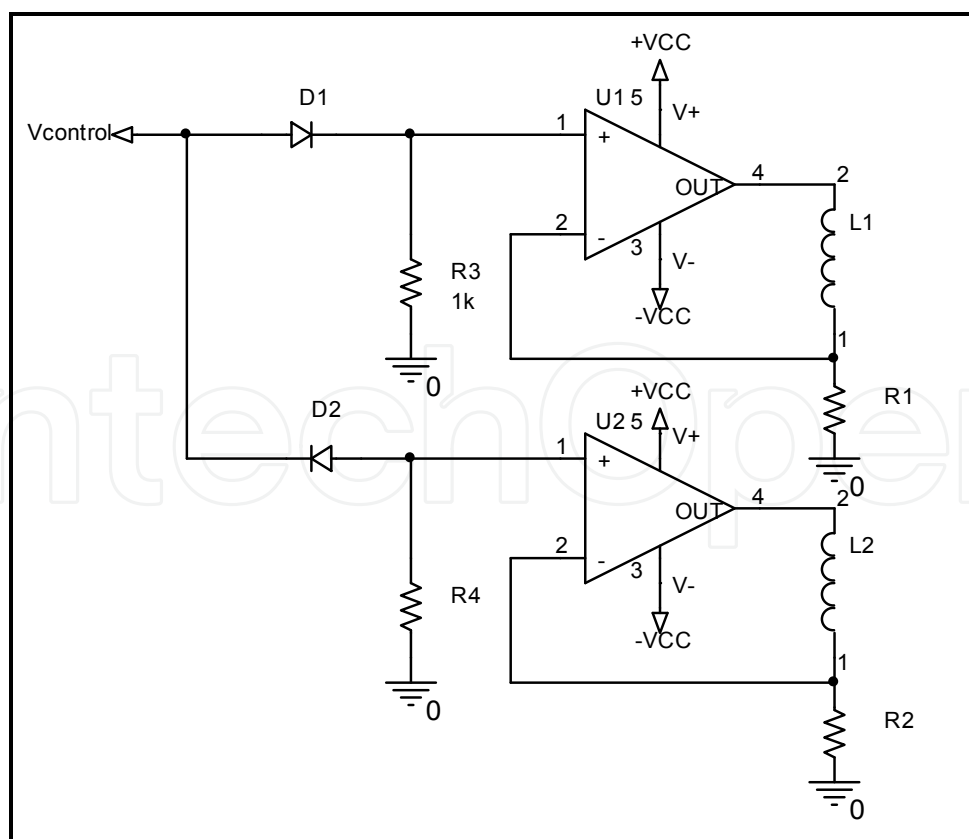


Fig. 3. The current amplifiers structure for two opposite coils

4. Implementation task

4.1 System description

AVC is studied along the work to compensate the vibration effect caused mainly by the unbalance disturbances on the machine rotor. Unbalance is considered as the unequal radial weight distribution of the rotor which consists in a condition where the mass centerline (principal inertia axis) does not coincide with the geometric centerline of the rotor. A direct consequence of unbalance in absence of some other disturbances is a vibration response of the rotor with a fundamental vibration frequency. Such fundamental vibration frequency of given amplitude should be attenuated as much as possible by means of the implemented control algorithm. In the same way, vibration frequencies near the fundamental frequency should be also attenuated.

The proposed and implemented strategy is based on the beneficial effects of conventional cascade control. While the Backstepping algorithm is responsible for the forward control loop stabilization, contributing with a robust performance yet under large load variations, the master PID controller is responsible for the fixed setpoint control.

Such proposed cascade structure is depicted in figure 4. The PID controller output variable plays the necessary role demanded by the Backstepping controller which consists in the determination and subsequent application of the reference trajectory to the Backstepping algorithm. The Backstepping controller output is then applied to the electromagnets by means of current amplifiers. Four control loops are necessary to control the shaft under two degrees of freedom, which means two control loops applied in each shaft end.

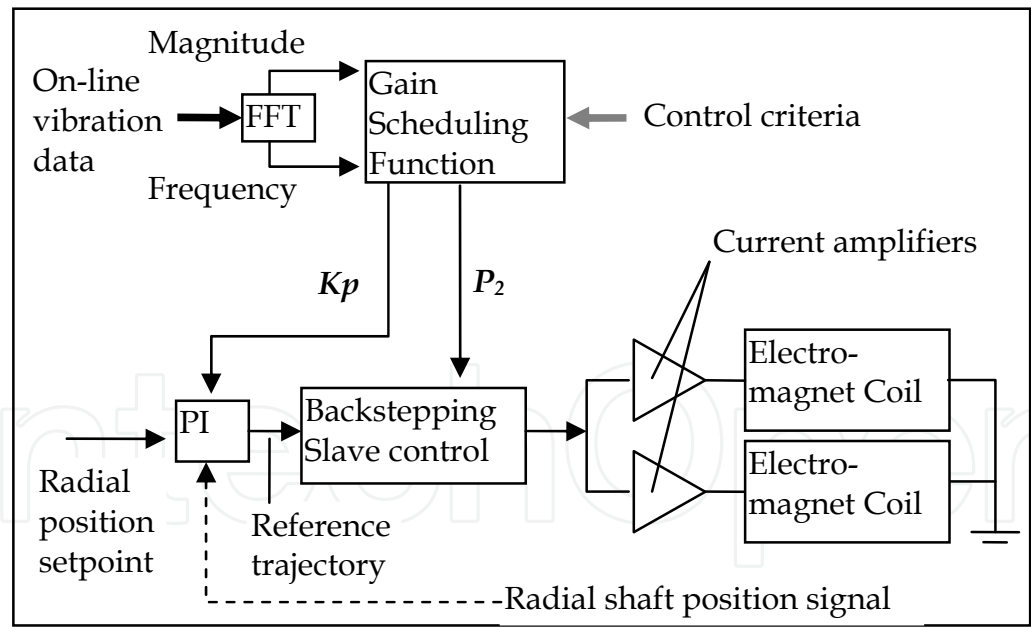


Fig. 4. The structure of the cascade strategy for a one degree of freedom control loop.

The gain scheduler based adaptive method operates with relevant information regarding to the rotor dynamics such as the magnitude and frequency of radial shaft vibration, or alternatively, with the amplitude (amplitude is on-line computed in time domain from the radial displacement measurements) and rotation speed of the shaft. Such data is applied to determine the parameters K_p and P_2 of the PID and Backstepping controllers respectively from the look-at-tables properly achieved.

Since the backstepping control algorithm is a model based technique, modelling errors are present when the values of parameters are not precisely determined. As consequence, the system control implementation must be performed under the set of selected model parameters matching the values of the test rig parameters. Such values are shown in table 1. The values selected for such set of model parameters are closely approached from the test rig data.

Large modelling error parameter values yields dramatic results in terms of rotor stabilization and active vibration control performance. Applied backstepping theory is robust under no relevant modelling errors. Consequently, the rotor mass and inertia moment as well as magnetic field parameters must be acquired and applied to the control algorithm as much accurately as possible.

Parameter/Notation	Value/Unit
Nominal air gap (X_0)	0.001m
Number of turns of each coil (n)	400
Coils resistance (R)	2 Ohms
Cross sectional area of air gap (A)	0.000625m ²
Rotor mass (m)	11 kg
Initial position of rotor (X_0)	-0.0008 m
Magnetic permeability of air gap (μ_0)	1.256E-6

Table 1. Backstepping model parameters

As shown in figure 4, the closed loop system is controlled by means of a master PID controller, followed by the slave cascade Backstepping controller. Thus, the types of disturbances for which the combination of a cascade with a PID feedback control system exhibit effectiveness, are those generated by the unbalance effect of the rotor, the impeller or turbine shaft assembled to the rotor, which operates producing an abnormal radial force. Such radial force will be accurately detected measured and compensated. Consequently, such events will be compensated by the control current scheduled by the cascade Backstepping controller.

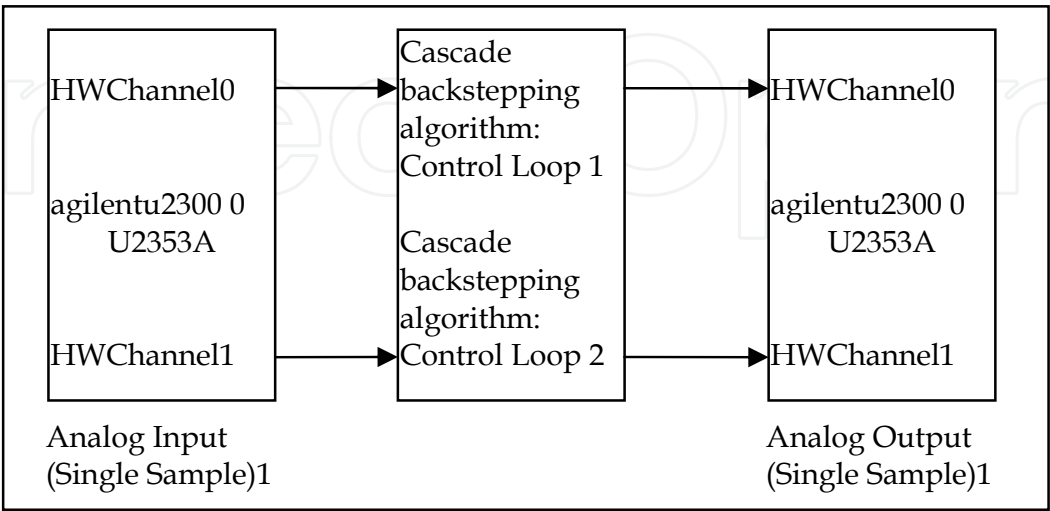


Fig. 5. The controller algorithm based on Agilent data acquisition hardware implemented under real time Matlab-Simulink software.

The implemented control type is based on a decentralized control structure (also called “side-by side” or “local” control). In such type of control structure, every degree of freedom to be controlled requires a feedback control loop. The control system applies the force commands to attenuate shaft vibration while keeping the shaft into the desired radial position, commonly symmetrically centred. The implementation of a shaft end vibration and position control scheme is shown in figure 5. It consists of Agilent Technologies based I/O hardware programmed under Matlab-Simulink.

The implemented test rig is considered as the traditional Jeffcott rotor as shown in figure 6 (a). The shaft turns around the bearing centreline and all rotating elements are concentric. This condition is depicted in detail (b) of figure 6. At very low speeds, unbalance forces are negligible. As rotor speed increases, the straight shaft will deflect into the predictable mode shape according to expression (37).

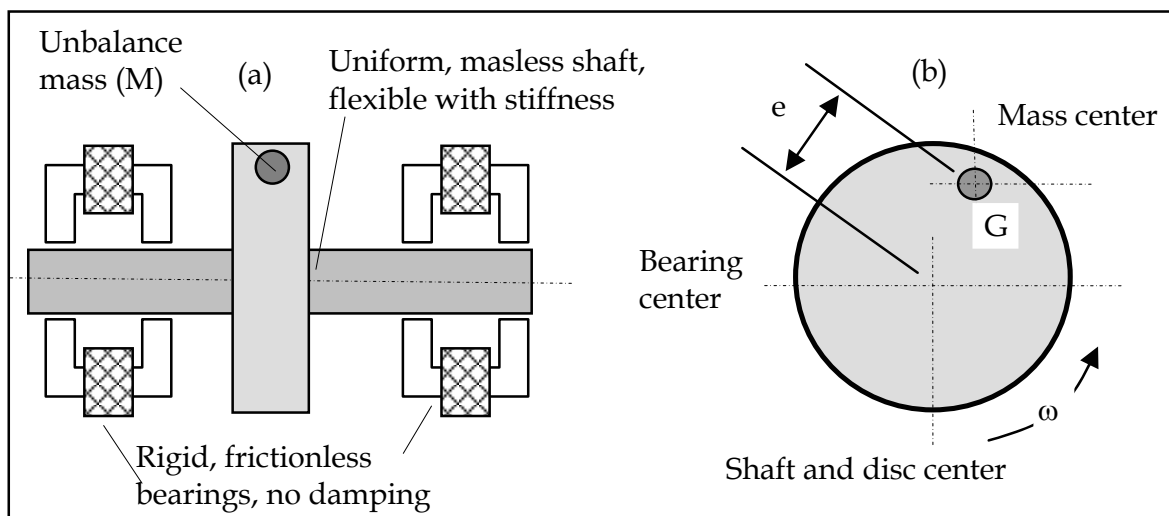


Fig. 6. The Jeffcott type rotor of the test rig: (a) rotor disk with unbalanced mass (M). (b) mass eccentricity (e) on the disc.

The only driving force in the system is the centrifugal force F_c due to the unbalance mass M , located at a radial distance e . The maximum bending deflection of the shaft is identified by r and the mass eccentricity by e . By inspection of the figure 6 it can be noted that the shaft and disk are rotating at the operating speed ω . Simultaneously, the deflected shaft is whirling in the magnetic bearings at this speed. The mechanism driving this whirl is the centrifugal force generated by the eccentric mass on the disc. As rotor speed increases, the outward force increases in accordance with the normal centrifugal force F_c equation

$$F_c = M \cdot (r + e) \cdot \omega^2 \quad (37)$$

With regard to expression (37), the total radius of the mass unbalance M is composed of the shaft bending r , and the eccentricity of the mass with respect to the shaft centreline e . Such centrifugal forces will be attenuated by the active magnetic forces developed by the control algorithm. Into the range of experimental rotating speeds, ($0 < \omega < 50$ rad/sec.) the bending deflection is considered negligible and the only centrifugal force is due to the mass eccentricity e . The unbalance characteristics for tests purposes consists of an unbalance mass M of 1 kg, radially located with an eccentricity of 0.1 m.

The general aspect of the vertical test rig is shown in figure 7. It consists of a vertical shaft supported by two radial AMB of the homopolar magnet type structure. The proposed design result is a substantial reduction of field variation around the circumference of the rotor so that the eddy current loss due to rotor rotation is considerably reduced. A detail of the homopolar type structure is depicted with figure 8.

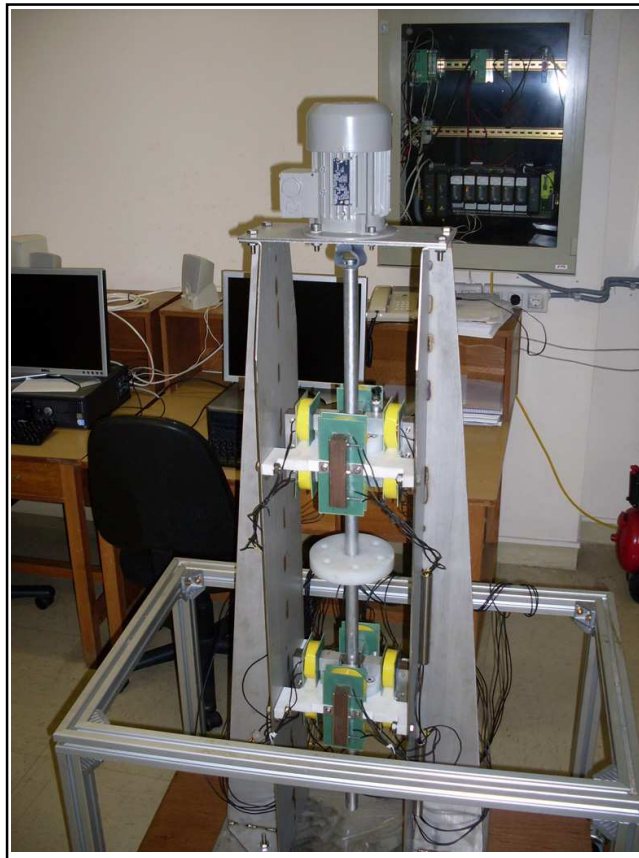


Fig. 7. The aspect of the vertical type test rig

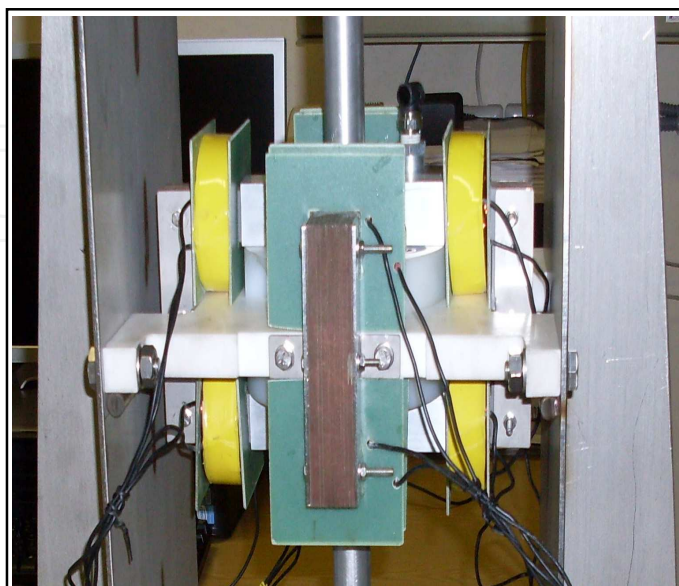


Fig. 8. Detail of the upper radial homopolar active magnetic bearing.

A detail of the upper radial magnetic bearing is shown in figure 8. The homopolar structures, being more complicated and expensive, exhibit the advantage that it produces much lower rotational losses since the rotor experiences less field variation when spinning and consequently has lower induced eddy currents. This property is of great importance in vacuum applications because any heat generated on the rotor must be removed by radiation transfer to the housing (rather than by convection as in non-vacuum AMB systems or conduction as in rolling element bearing systems): there is a high premium on rotor losses. The advantage of four-pole radial bearings, as illustrated in figures 7 and 8, is the fact that two pole pairs each can be assigned to the Cartesian coordinates x and y which are often used in mechanics. To drive the test rig, an electric motor is assembled at the upper shaft end, driven by a variable speed drive in order to test the AVC system at different rotation speeds.

4.2 AVC performance

The implemented control algorithm under the structure depicted in figure 4 consists of a cascade control loop where the master controller is a PID and the slave is a backstepping algorithm. Such adaptive cascade structure is based in the gain scheduling technique for which two parameters are taken into account. The PID gain K_p of the master controller and the backstepping parameter P_2 shown in figures 9 and 10 respectively. The on-line selection of such mentioned parameter values, which are applied on updating the control algorithm, obeys to the fact that the values of both parameters are sensible to rotor speed changes. For low rotating speeds, it has been experimentally determined a set of values as function of the shaft rotation speed under a satisfactory performance criterion on the basis of an accepted dynamic response of the control system at different speeds into the operational range of $(0 < \omega < 50 \text{ rad/sec.})$. In order to illustrate the dynamic performance of the vibration attenuation controller, some results among a lot of them are selected. The time response of the shaft under some tolerable unbalance is presented. The tests have been carried out at different speeds under the same conditions.

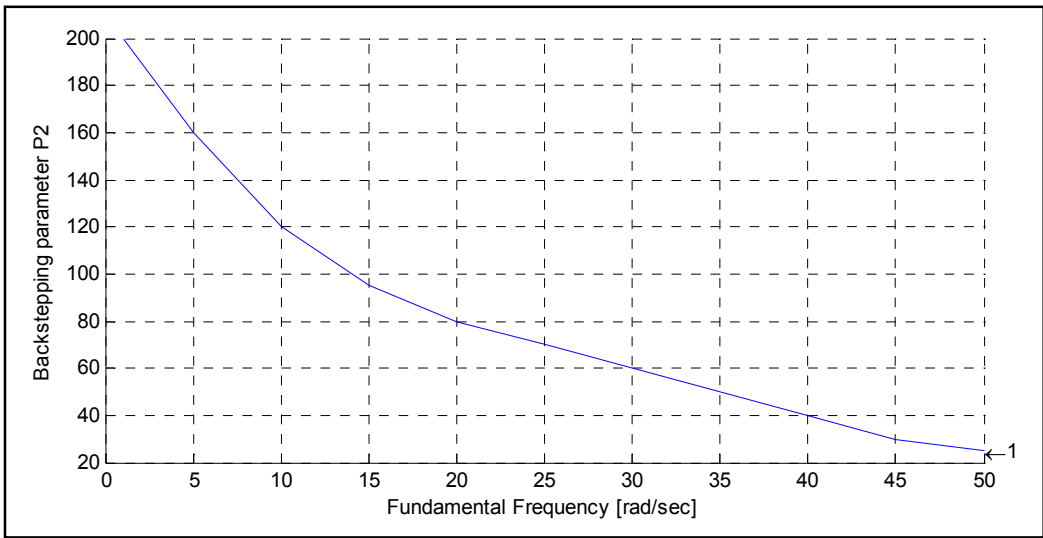


Fig. 9. The set of acceptable values for parameter P_2 of the backstepping algorithm as function of the fundamental vibration frequency located near the measured radial magnetic bearing.

Figures 11, 12 and 13 shows the control current applied to the magnetic coils scheduled by the adaptive procedure as function of the shaft rotation speed. Such control currents are scheduled by the cascade or Backstepping control algorithm. In figures 14, 15 and 16 it is shown the spectrum analyzer layout for the same rotation speeds, and in figures 17, 18 and 19 it is shown the shaft radial position as function of the rotation speed.

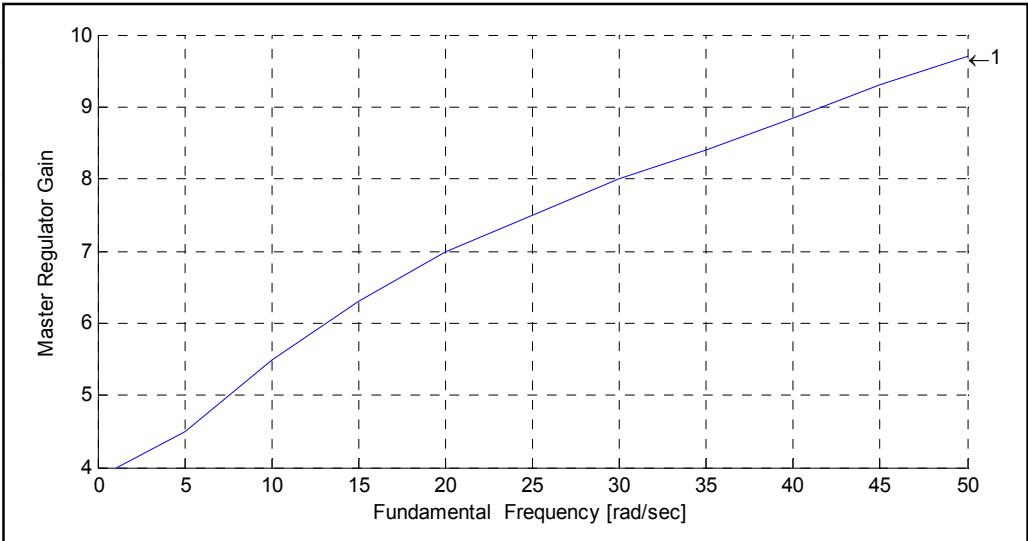


Fig. 10. The set of acceptable values for parameter K_p of the Master controller as function of the fundamental vibration frequency.

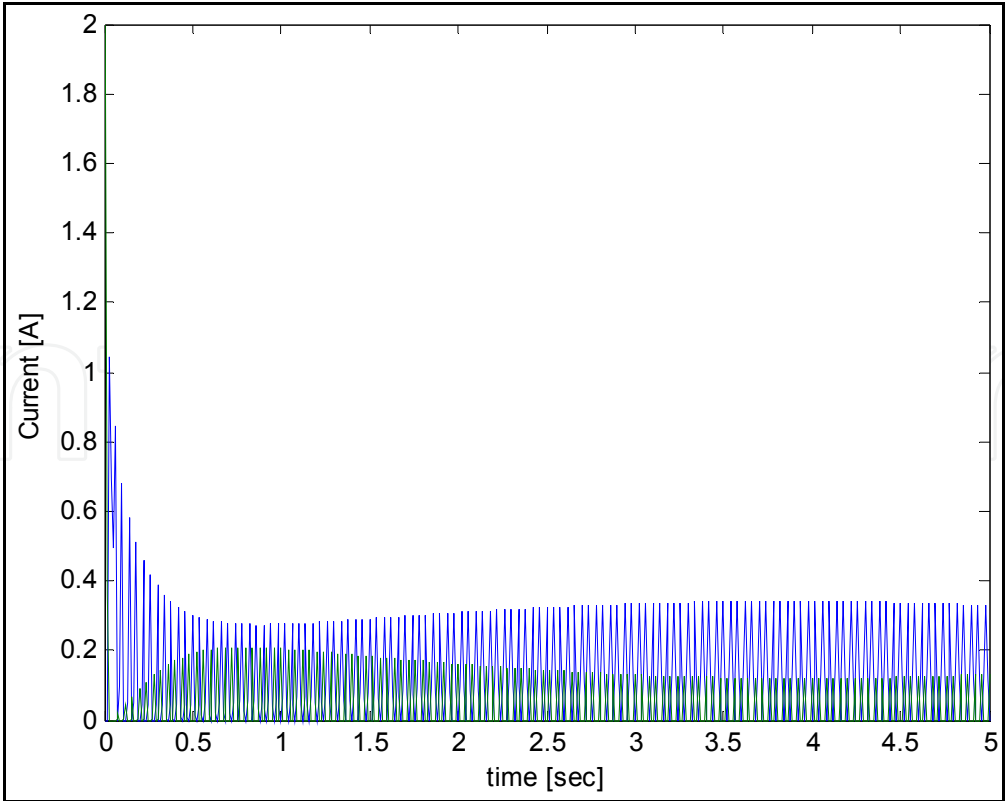


Fig. 11. Control current at $\omega=6.28$ rad/sec

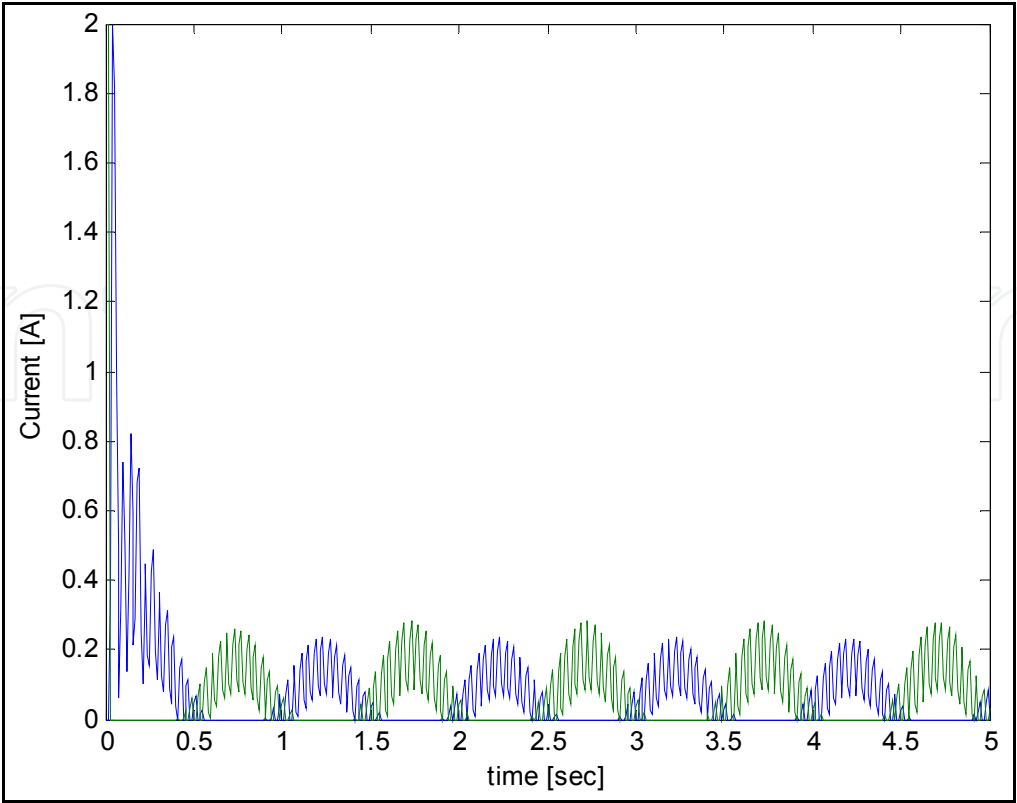


Fig. 12. Control current at $\omega=25.12$ rad/sec

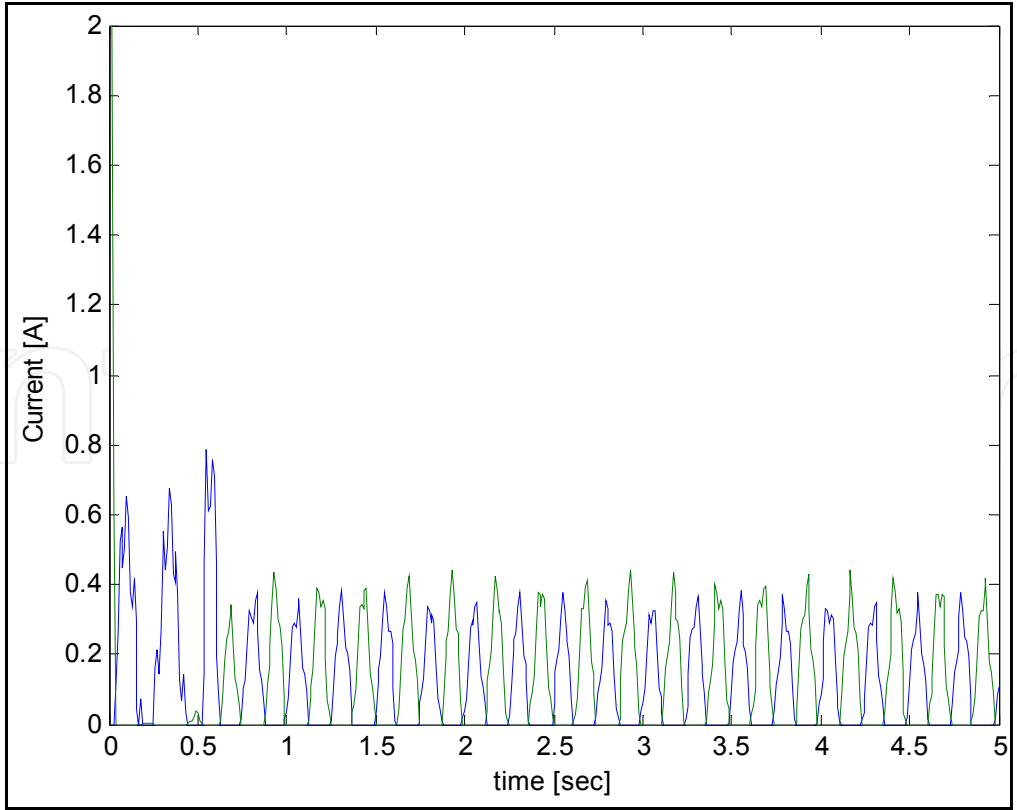


Fig. 13. Control current at $\omega=50.24$ rad/sec

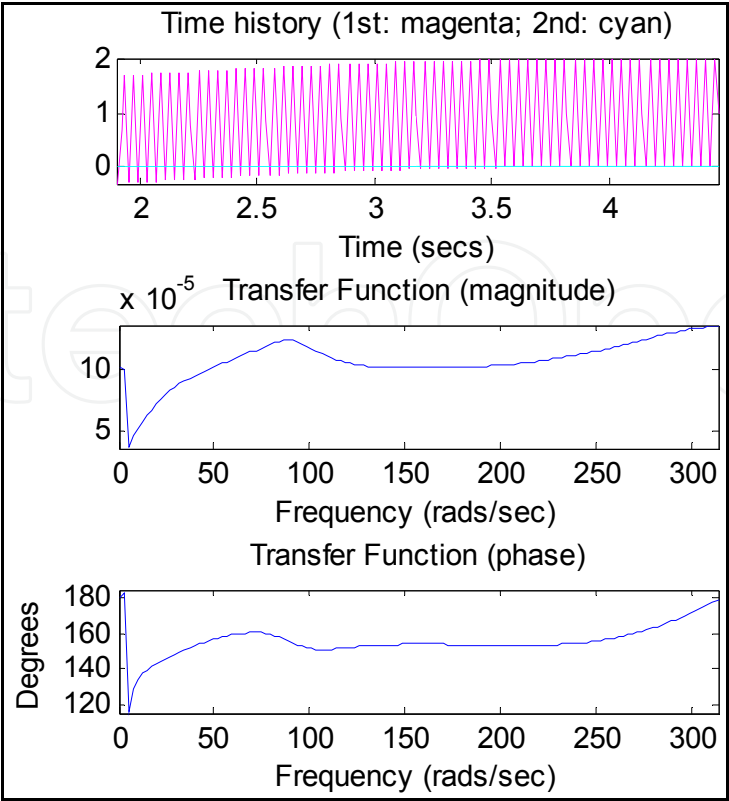


Fig. 14. Spectrum analyzer layout with $\omega=6.28$ rad/sec

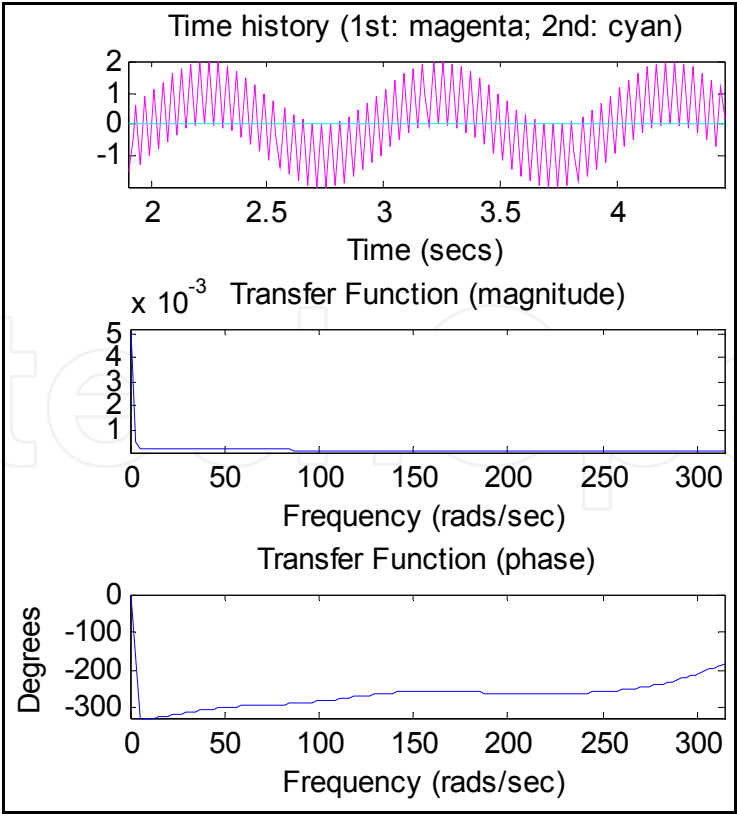


Fig. 15. Spectrum analyzer layout with $\omega=25.12$ rad/sec

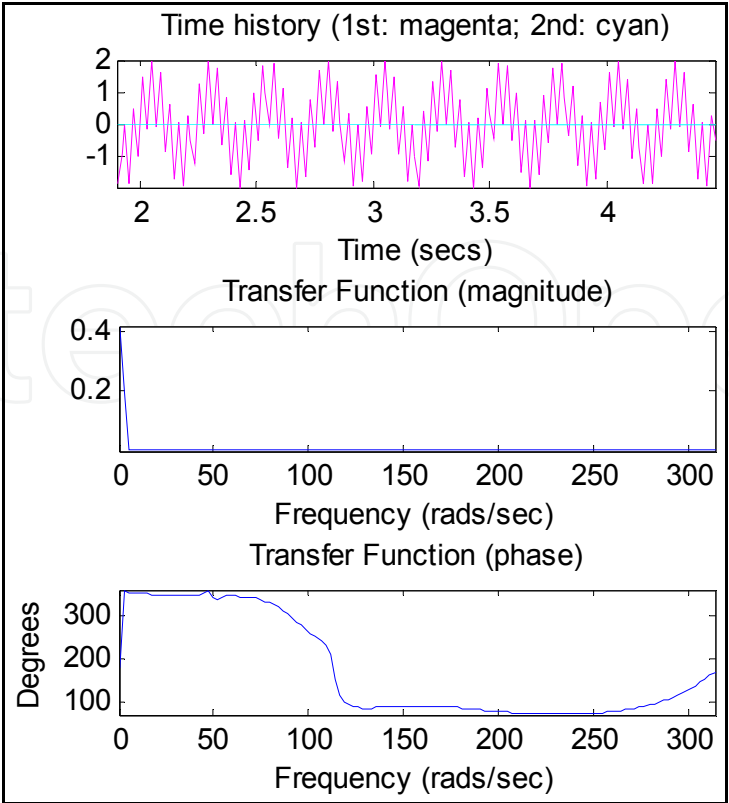


Fig. 16. Spectrum analyzer layout with $\omega=50.24$ rad/sec

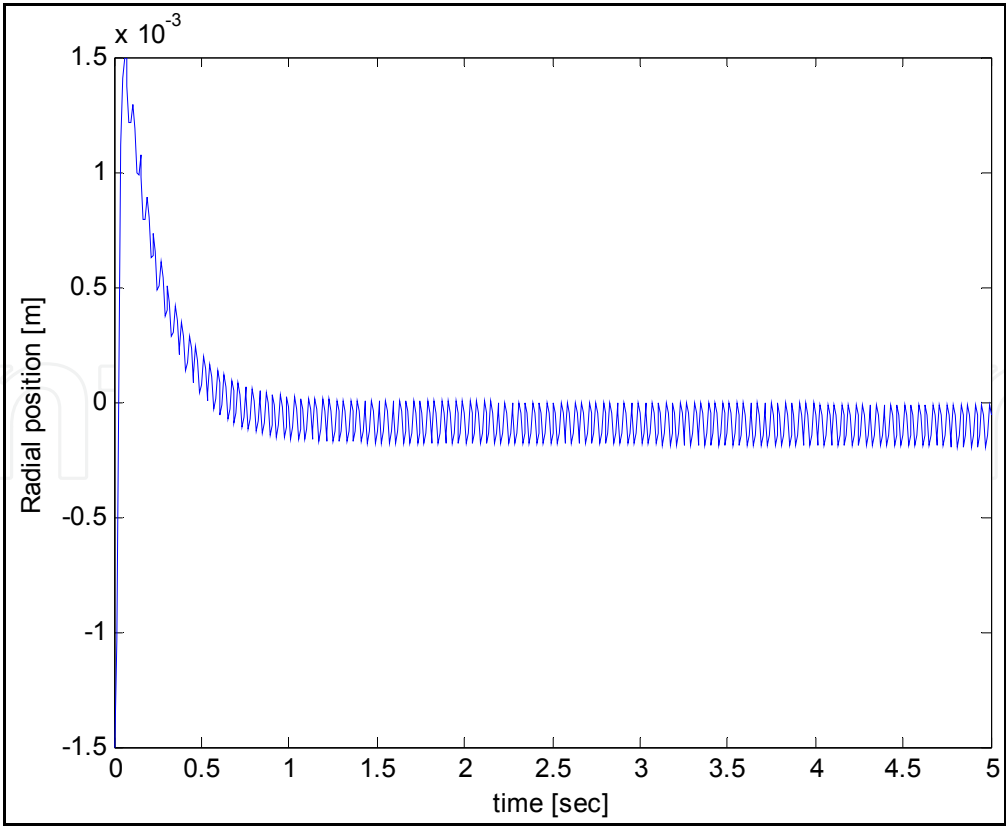


Fig. 17. Shaft radial position at $\omega=6.28$ rad/sec

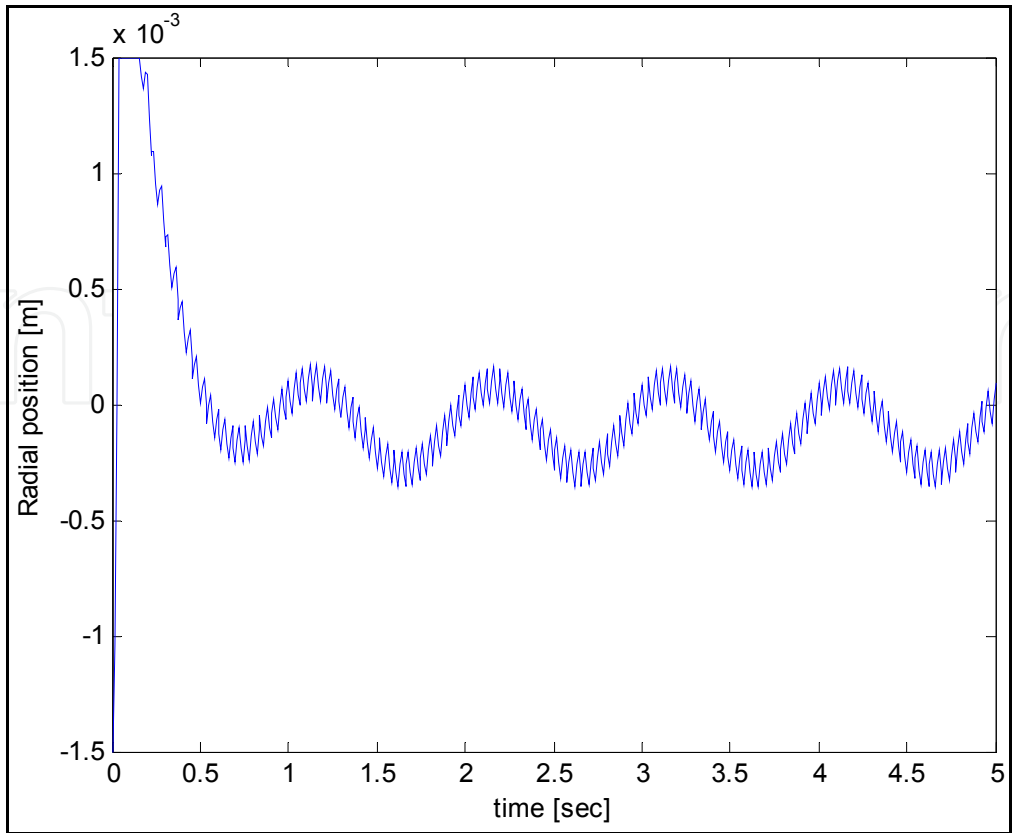


Fig. 18. Shaft radial position at $\omega=25.12$ rad/sec

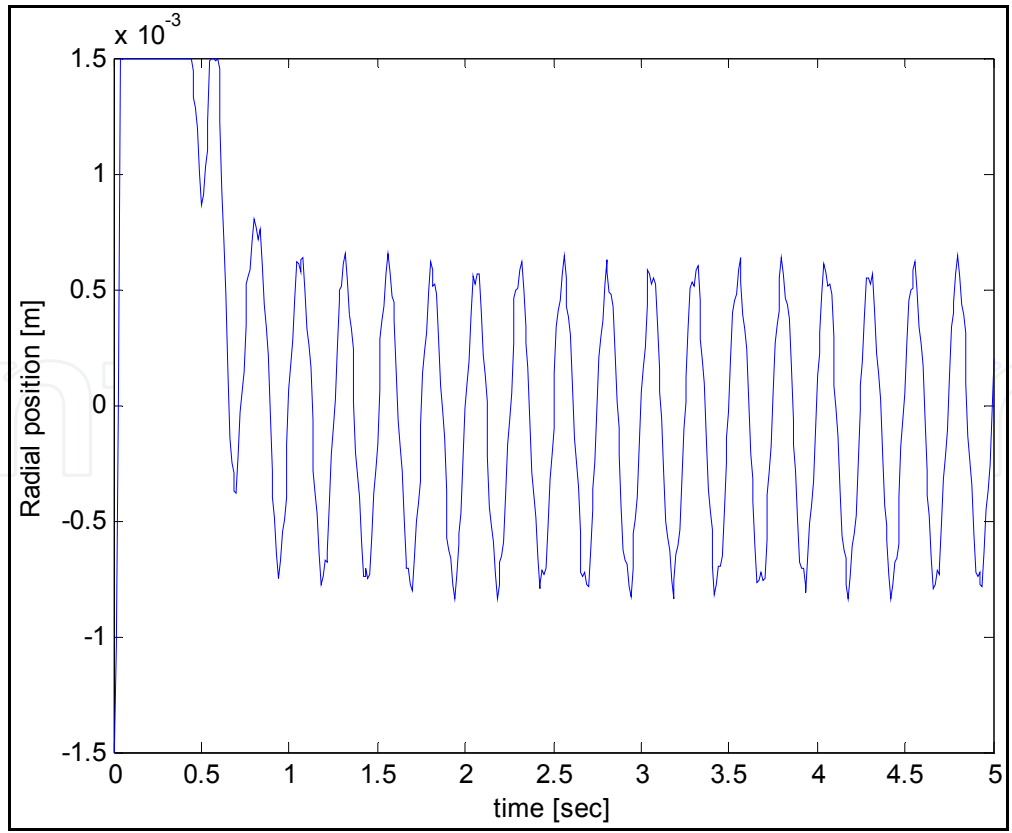


Fig. 19. Shaft radial position at $\omega=50.24$ rad/sec

4.2 Discussion of results

In spite of the fact that Backstepping design techniques has the drawbacks inherent to model based techniques, the most relevant characteristic of such control strategy is the inherent capacity to reject load disturbances under some tolerable modelling error. Furthermore, it has been shown by simple inspection of the results that the capacity of the control strategy to disturbances rejection, increases as function of the proper adjustment values of the parameter K_p at the PID controller and parameter P_2 of the Backstepping algorithm. Parameter P_1 doesn't exhibit such property. In fact, the influence on the value of P_1 on the vibration attenuation is irrelevant. On the basis of the developed work, the coupled dynamics of the test rig which includes the bed plate or platform and the Jeffcott type rotor, a robust backstepping controller for vibration isolation is derived as results of the experimental work. The results of the analysis of the achieved information show that the control strategy can effectively attenuate low frequency vibrations in two DOF. Meanwhile, to vibrations with time-varying parameters in different directions, vibration isolation performance can also be improved. The actual values of the payload through vibration isolation are greatly impacted by the parameter P_2 of the backstepping algorithm and the master controller gain K_p in the case of a cascade structure. Therefore, in order to enhance the vibration isolation performance, the gain K_p and the parameter P_2 should be carefully chosen in order to satisfy the required performance under different operating conditions. According to such idea, a gain scheduling strategy has been successfully applied. The range of useful values for K_p and P_2 experimentally determined, are such that $4 < K_p < 10$, and $25 < P_2 < 220$ as shown respectively in figures 9 and 10. The validity of such results is into the range of low rotational speeds, which for this test rig approaches a maximum speed of 50 rad/sec.

Some important influence factors of vibration isolation are considered in the cascade backstepping design procedure, such as the inclination of the test rig, the rotational speed changes, the inherent uncertainties including modelling errors and the base plate vibration conditions obviously restricted to some limits experimentally determined. Thus, the robust backstepping control method can fulfil the requirements of a vibration isolation alternative for a variety of practical applications.

4.3 Conclusions

A feedback control under a cascade structure composed by a gain scheduling based adaptive PID master controller associated to a gain scheduling based adaptive Backstepping controller has been implemented. In such a cascade control structure, the PID master controller is responsible for the reference or desired trajectory generation and the radial position, while the slave backstepping controller contributes to the rotor global stabilization and vibration suppression or attenuation.

Such a control strategy fulfils the two following objectives:

- a. Radial position control of the shaft by means of active magnetic bearings, and
- b. Vibration attenuation by active vibration control using the same actuators as for active magnetic bearing control.

With regard to the designed test rig mechanical structure, it must be taken into account that the absorbed vibration is transferred by the actuators to the base plate or stator. Consequently, in order to absorb the shaft vibration modes into the range of operational

speeds, the stator mass should be several times greater (in this case, ten times the mass of the stator bed plate) than the rotor mass.

Gain scheduling based adaptation as function of vibration frequency and amplitude contributes effectively to the vibration attenuation of rotor dynamics into the range of low rotation speeds $0 < \omega < 50$ rad/sec.

It has been shown experimentally that the vibration reduction is significant for rotors with low external damping. However, in heavy rotating machines, very large forces would be required and electromagnet based actuators under such conditions are not effective.

Gain scheduling adaptation as function of the vibration characteristics is very effective at low rotation speeds, and outside the range of resonant frequencies. Although it can be applied to attenuate resonant frequencies, obviously it is not so effective, because centrifugal forces are very large, and actuators have not been designed to compensate so large forces. To avoid resonant induced vibration, the rig structure must be designed so that resonant frequencies are outside of the operational rotation speeds.

Since a great variety of control algorithms have been applied along the last three decades of practical implementations, the experiences show that the effectiveness of a single PD or PID is comparable to sophisticated control algorithms such the backstepping one.

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6. References

- B. Shafai, S. Beale, P. LaRocca, and E. Cusson, (1994), "Magnetic Bearing Control Systems and Adaptive Forced Balancing", *IEEE Control Systems*, Volume 14, No. 2, pp. 4-13.
- C.R. Burrows and M.N. Sahinkaya, (1983), "Vibration Control of Multi-Mode Rotor-Bearing Systems", *Proceedings of the Royal Society of London*, Vol. 386, pp. 77-94.
- C.R. Burrows, M.N. Sahinkaya, and S. Clements, (1989) "Active Vibration Control of Flexible Rotors: an Experimental and Theoretical Study", *Proceedings of the Royal Society of London*, Vol. 422, pp. 123-146.
- Francesc Pozo, Fayçll Ikhoulane, Gisela Pujol, José Rodellar, (2006), "Adaptive Backstepping Control of Hysteretic Base-Isolated Structures", *Journal of Vibration and Control*. 2006; 12: 373-394
- F. Matsumura, M. Fujita, and K. Okawa, (1990), "Modeling and Control of Magnetic Bearing Systems Achieving a Rotation Around the Axis of Inertia", *Proceedings of the 2nd International Symposium on Magnetic Bearings*, July 12-14, 1990, Tokyo, Japan.
- Gerhard Schweitzer, Eric H. Maslen Editors, (2009), "Magnetic Bearings: Theory, Design, and Application to Rotating Machinery", DOI 10.1007/978-3-642-00497-1, Springer Dordrecht Heidelberg London New York
- Guang Lia, Amir Khajepour, (2005), "Robust control of a hydraulically driven flexible arm using backstepping technique", *Journal of Sound and Vibration* 280, 759 - 775

- Hassan K. Khalil (2002). *Nonlinear Systems*. Prentice-Hall, third edition, ISBN: 0-13-067389-7, Chap 4, pp 111-174.
- H. Habermann and M. Brunet, (1984), "The Active Magnetic Bearing Enables Optimum Damping of Flexible Rotors", ASME Paper 84-GT-117, 1984.
- Knospe C. R., R.W. Hope, S.J. Fedigan, and R.D. Williams, (1993), "Adaptive On-Line Rotor Balancing Using Digital Control", *Proceedings of MAG '93 Magnetic Bearings, Magnetic Drives, and Dry Gas Seals Conference*, Technomic Publishing, Lancaster, PA, July 1993.
- Krstic, M., I. Kanellakopoulos, and P. Kokotovic, (1995). *Nonlinear and Adaptive Control Design*. John Wiley & Sons, Inc. New York, NY, USA, (1995).
- Krstic M., and H. Deng (1998). *Stabilization of Nonlinear Uncertain Systems*, (Springer Verlag, Berlin).
- LaSalle J. P., (1960), "Some extensions of Liapunov's second method". *IRE Trans. Circuit Theory*, Vol. 7, pp. 520-527.
- LaSalle J. P., (1968), "Stability theory for ordinary differential equations", *Journal of Differential Equations* vol. 4, , 57-65.
- Qinglei Hu, (2009), "Robust adaptive backstepping attitude and vibration control with L2-gain performance for flexible spacecraft under angular velocity constraint", *Journal of Sound and Vibration* 327 , 285-298
- R. Larssonneur and R. Herzog, (1994), "Feedforward compensation of Unbalance: New Results", IUTAM Symposium, Bath, UK, September 1994.
- R. Larssonneur, (1998), "Design and Control of Active Magnetic Bearing Systems for High Speed Rotation", PhD Thesis, Swiss Federal Institute of Technology, ETH Zurich, Switzerland, June, 1998.
- Sontag E. D., (1989), "A 'universal' construction of Artstein's theorem on nonlinear stabilization". *Systems and Control Letters*, Vol.13 (2), pp.117-123, 1998.
- Sontag E.D., and Sussman, (1998) "Further comments on the stabilization of the angular velocity of a rigid body", *Systems and Control Letters*, Vol. 12, pp. 213-217, 1998.
- T. Higuchi, M. Otsuka, T. Mizuno, and T. Ide, (1990), "Application of Periodic Learning Control with Inverse Transfer Function Compensation in Totally Active Magnetic Bearings", *Proceedings of the 2nd International Symposium on Magnetic Bearings*, July 12-14, 1990, Tokyo, Japan.
- T. Higuchi, T. Mizuno, and M. Tsukamoto, (1990), "Digital Control System for Magnetic Bearings with Automatic Balancing", *Proceedings of the 2nd International Symposium on Magnetic Bearings*, July 12-14, 1990, Tokyo, Japan.
- Tao Yang, Jia Ma, Zeng-Guang Hou, Min Tan (2009), "Robust backstepping control of active vibration isolation using a Stewart platform", *2009 IEEE Int. Conf. on Robotics and Automation*, Volume , Issue , 12-17 May 2009 Page(s):1788 - 1793, 978-1-4244-2789-5/09/\$25.00 ©2009 IEEE, Digital Object Identifier:10.1109/ROBOT.2009.5152486, Kobe, Japan, May 12-17, 2009.
- V. Mañosa, F. Ikhoulane, J. Rodellar, (2005), "Control of uncertain non-linear systems via adaptive backstepping", *Journal of Sound and Vibration* 280 657-680

- Yoshizawa, T., (1966), "*Stability theory in Liapunov's second method*", Mathematical Society of Japan, <http://www.ams.org/mathscinet-getitem?mr=MR0208086>
- Yoshizawa, T., (1966), "Stability and existence of a periodic solution", *J. Differential Equations*, Vol. 1 (1968), 121-129, <http://www.ams.org/mathscinet-getitem?mr=MR0222396>

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Vibrations are a part of our environment and daily life. Many of them are useful and are needed for many purposes, one of the best example being the hearing system. Nevertheless, vibrations are often undesirable and have to be suppressed or reduced, as they may be harmful to structures by generating damages or compromise the comfort of users through noise generation of mechanical wave transmission to the body. the purpose of this book is to present basic and advanced methods for efficiently controlling the vibrations and limiting their effects. Open-access publishing is an extraordinary opportunity for a wide dissemination of high quality research. This book is not an exception to this, and I am proud to introduce the works performed by experts from all over the world.

How to reference

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